

Spin devices II

FM PAN

Maciej Urbaniaka

2017

Poznańska

Spin devices II

- Magnetic semiconductors
- Spin injection
- Spin transistors

FM PAN

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Metals, half-metals, etc.

Quantum electronics

Energy bands in various types of materials



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Heusler compounds

Ferromagnetic (or ferrimagnetic etc.) properties are usually associated with transition metals **Fe, Co, Ni** and their alloys/compounds.

The family of compounds XYZ (half-Heusler) or X₂YZ (**full-Heusler**) with X,Y typically transition metals and Z main group element can be tailored to show ferromagnetism, superconductivity or insulating properties [3]. Some of Heusler compounds display half-metallicity with potential for applications in **spintronics**. Spin polarization of a material:

 $P_0 = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$, N_{\uparrow} , N_{\downarrow} - density of states, at Fermi energy, for majority/minority electrons

In 3d ferromagnets the positive spin polarization is associated with more mobile 4s electrons which are polarized by hybridization with 3d states [4]



- NiMnSb, NiMnV₂[4], Mn₂VAl, Co₂TiSn, Co₂FeSi [5] etc. - half metallic Heusler compounds
- Heuslers are attractive because of their relatively high Curie temperature in relation to other half-metals [5]
- Half-metals can be considers hybrid between metals and semiconductors electrons with one spin display metallic behavior the others act like in a semiconductor [5]

Giant TMR - example

Quantum electronics

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The highest amplitude to-day tunneling magnetoresistance amplitude was obtained using half metallic Heusler Co₂MnSi compound



FIG. 2. Typical TMR curves at 4.2 K and 290 K for a Co₂MnSi MTJ consisting of (from the lower side) Co₂MnSi lower electrode (3 nm)/MgO barrier (2.4 nm)/Co₂MnSi upper electrode (3 nm) grown on a CoFe-buffered MgO(001) substrate with Mn-rich Co₂Mn_{1.35}Si_{0.88} electrodes (MTJ-B). The magnetoresistance was measured with a magnetic field applied along the [1-10] axis of the Co₂MnSi film using a dc four-probe method. The bias voltages were 1 mV at 4.2 K and 5 mV at 290 K.

MgO(001)/MgO(10nm)/CoFe(30nm)/Co₂Mn Si/MgO/Co₂MnSi MgO buffered MgO(001) - MgO deposited on MgO crystal $T_{c} = 985K$ room temperature (290K) TMR≈340% image from: M. Urbaniak *et al.*, Physica Status Solidi A **199**, 284 (2003) Compare with *old* "metallic" TMR: 50 40 TMR[%] 30 20 10 -50 -100 50 0 -150 H [kA/m] Fig. 6 The room temperature TMR curve of $Cu(30 \text{ nm})/Ni_{80}Fe_{20}(4 \text{ nm})/Mn_{83}Ir_{17}(15 \text{ nm})/Co_{70}Fe_{30}$ 2017 $(2 \text{ nm})/\text{Al}(1.4 \text{ nm}) + \text{Ox}/\text{Ni}_{80}\text{Fe}_{20}(4 \text{ nm})/\text{Ta}(3 \text{ nm})/$ Cu(55 nm)/Au (20 nm) multilayer.

Diluted magnetic semiconductors

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There is an ongoing search for materials displaying both magnetic and semiconductor properties.

Most magnetically doped semiconductors and semiconductor oxides, that display ferromagnetic features, can be grouped into two main classes [1]:

• **uniform systems** with randomly distributed transition metals cations (Mn,Fe,Co,Ni) where spin-spin interactions are mediated by holes [eg. (Ga,Mn)As]



- In_{1-x}Mn_xAs epilayers [2]
- Mn implantation (100keV) followed by pulsed laser melting on InAs (001) substrates
- ferromagnetism, low saturation field, T_c=82K at x=0.105
- perpendicular magnetic anisotropy (field parallel to [001] axis) – due to strain induced by the Mn ion substitution

image from: Y. Yuan et al., Journal of Physics D Applied Physics 48, 235002 (2015) [2]

Figure 1. (a) Magnetization of $In_{1-x}Mn_xAs$ samples measured at 5 K in the out-of-plane geometry: the Mn concentrations are: x = 0.019 (triangle), 0.042 (circle) and 0.069 (square); (b) remanent magnetization as a function of temperature measured under a magnetic field of 20 Oe after the samples were saturated by applying 1000 Oe along the perpendicular direction for the three samples. The inset shows the plots of Mr(T)/Mr(5 K) as a function of $T/T_{\rm C}$.

Diluted magnetic semiconductors

There is an ongoing search for materials displaying both magnetic and semiconductor properties.

Most magnetically doped semiconductors and semiconductor oxides, that display ferromagnetic features, can be grouped into two main classes [1]:

heterogeneous systems with non-random distribution of magnetic elements – ferromagnetic-like properties are determined by **nanoregions** with high concentration of magnetic cations



"The element-semiconductors silicon and germanium are widely used, but nowadays binary, ternary, and even quaternary semi- conductors such as GaN,GaP_{1-x}As_x, or $Cu(GaIn)Se_2$ play an important role in electronics and materials for energy conversion. More elements allow for more degrees of freedom such as band-gap tuning and multi*functionality.*" - C. Felser et al. M. Urbaniak

Spin-injection

- an unpolarized current (both spin channels carrying equal current) is flowing under the action of an EelecrtoMotoricForce into left ferromagnet (electrode, LE)
- the current experiences polarization and enters the middle, non-ferromagnetic (NM) conductor
- the surplus spin is not dissipated at once but increases magnetic moment at the interface – spin accumulation [10]. Its extent is determined by an *equilibrium* between spin injection rate and spin-flip rate in NM



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- the spins injected into NM experience scattering and after some time τ_{t1} , on average their magnetization is zero. They travel in that time a **spin diffusion length**
- only if spin diffusion length is longer than the conductor connecting the ferromagnetic electrodes the magnetic state of the left electrode can influence the state of right one



Einstein relation*

Consider electron gas at 0K: drift current and diffusion currents at steady state must be equal [11]. We have then

 $\vec{j}_e + \vec{j}_D = \sigma \vec{E} + e D \nabla n$, *D*-diffusion constant, *n*-particle density [m^{-3}], σ -conductivity

Electrochemical potential is defined as

 $\mu = -eV + E_F \text{ and its gradient can be written as}$ $\nabla \mu = e\vec{E} + \nabla E_F = e\vec{E} + \frac{dE_F}{dn} \nabla n = e\vec{E} + \frac{1}{D(E_F)} \nabla n$

inserting gradient of n (Eq.1) into the above equation gives

$$\nabla \mu = e \vec{E} - \frac{1}{D(E_F)} \frac{\sigma \vec{E}}{De} = \left(e - \frac{1}{D(E_F)} \frac{\sigma}{De} \right) \vec{E}$$

$$\nabla \mu = 0$$

Because electrochemical potential is spatially constant at thermal equilibrium [11] and E is arbitrary we get*

$$\sigma = e^2 D(E_F) D$$

G = U - TS + pV -Gibbs energy; formerly free energy or free enthalpy [13]

 $\vec{j} = -D\nabla n$ -Fick's first law

 $\mu_B = \left(\frac{\partial G}{\partial n_B}\right)_{t=0,0,0,0,0}$

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*for electrons. Classical Einstein relations for Brownian motion at equilibrium relates proportionality factor between terminal velocity under the action of force in viscous liquid and that force with diffusion constant [12]

(1)

 $D(E_F) = \left(\frac{dn}{dE}\right)_{E_F} \rightarrow \frac{dE_F}{dn} = \frac{1}{D(E_F)}$

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We analyze separately both spin channels (\uparrow and \downarrow). The current density is proportional to a gradient of the electrochemical potential:

$$\frac{\partial \mu^{\uparrow,\downarrow}}{\partial x} = \frac{-e j^{\uparrow,\downarrow}}{\sigma^{\uparrow,\downarrow}} \qquad \vec{j}_e = \sigma \vec{E} \rightarrow \vec{E} = \frac{j_e}{\sigma} \rightarrow \text{ electric force: } \vec{F}_e = e \vec{E} = \frac{e j_e}{\sigma}, \quad -\frac{\partial \mu^{\uparrow,\downarrow}}{\partial x} = \text{force} \qquad (2)$$
The spin diffusion equation, in 1D, reads (this comes from the second Fick's law)

$$\frac{\mu^{\uparrow} - \mu^{\downarrow}}{\tau_{sf}} = D \frac{\partial^2 (\mu^{\uparrow} - \mu^{\downarrow})}{\partial x^2} \qquad \text{this is written in a relaxation time approximation - } \tau_{\tau_1} \qquad \frac{\partial C}{\partial t} = D \nabla^2 C C_{c-concentration}$$
The general solution of the above equation is

$$\mu^{\uparrow} - \mu^{\downarrow} = C_1(t) e^{\frac{x}{\sqrt{D\tau_{sf}}}} + C_2(t) e^{-\frac{x}{\sqrt{D\tau_{sf}}}}, \text{ where } \sqrt{D\tau_{sf}} \text{ is a spin diffusion length}$$

• Spin diffusion length is a typical length scale on which the spin information is lost



Quantum electronics

The expression for the spin polarization, using the Einstein relation, can be written as

$$\beta = \frac{\sigma_{FM}^{\uparrow} - \sigma_{FM}^{\downarrow}}{\sigma_{FM}^{\uparrow} + \sigma_{FM}^{\downarrow}} \qquad \qquad \sigma = e^2 D(E_F) D \qquad P_0, \beta = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}} = \frac{D_{\uparrow}(E_F) - D_{\downarrow}(E_F)}{D_{\uparrow}(E_F) + D_{\downarrow}(E_F)}$$

In non-ferromagnetic semiconductor the conductivity does not depend on spin

$$\sigma_{SC}^{\uparrow,\downarrow} = \frac{1}{2} \sigma_{SC} \rightarrow \beta = 0$$

We want to find the profile of the electrochemical potential in the vicinity of the ferromagnet/ semiconductor interface. The general solutions of the diffusion equation are [11]



Quantum electronics

We obtain the current density inserting the solution for the ferromagnet into equation (2)

We assume that the total current density at $x=-\infty$ and at x=0 is the same. We have then

$$j(-\infty) = j^{\dagger}(-\infty) + j^{\dagger}(-\infty) = -\frac{\sigma_{FM}^{\dagger}}{e}(a+0) - \frac{\sigma_{FM}^{\dagger}}{e}(a+0)$$
$$j(0) = j^{\dagger}(0) + j^{\dagger}(0) = -\frac{\sigma_{FM}^{\dagger}}{e}\left(a + \frac{c^{\dagger}}{\lambda_{FM}}\right) - \frac{\sigma_{FM}^{\dagger}}{e}\left(a + \frac{c^{\dagger}}{\lambda_{FM}}\right)$$

Equating both currents we get

$$\frac{\sigma_{FM}^{\uparrow}}{e}\frac{c^{\uparrow}}{\lambda_{FM}} + \frac{\sigma_{FM}^{\downarrow}}{e}\frac{c^{\downarrow}}{\lambda_{FM}} = 0 \quad \Rightarrow \quad c^{\uparrow} = -c^{\downarrow}\frac{\sigma_{FM}^{\downarrow}}{\sigma_{FM}^{\uparrow}}$$

We assume that spin-diffusion length in ferromagnet is the same for both spin channels

Analogous calculations can be performed for semiconductor side (x>0) and since both spin channels have equal conductivity we have

$$d^{\uparrow} = -d^{\downarrow} \frac{\sigma_{SM}^{\flat}}{\sigma_{SM}^{\uparrow}} = -d^{\downarrow} \frac{\sigma_{SM}/2}{\sigma_{SM}/2} \quad \Rightarrow \quad d^{\uparrow} = -d^{\downarrow}$$

The electrochemical potential is continuous everywhere, and in particular at x=0:

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Spin diffusion

The coefficients d and μ_{off} are thus given by

From the limits $x=-\infty$ and $x=\infty$, for ferromagnet and semiconductor respectively, we obtain

$$j_{FM}(-\infty) = j_{FM}^{\dagger}(-\infty) + j_{FM}^{\dagger}(-\infty) = -\frac{(\sigma_{FM}^{\dagger} + \sigma_{FM}^{\dagger})a}{e} = -\frac{\sigma_{FM}a}{e}$$

$$j_{SC}(+\infty) = j_{SC}^{\dagger}(+\infty) + j_{SC}^{\dagger}(+\infty) = -\frac{(\sigma_{SC}^{\dagger} + \sigma_{SC}^{\dagger})b}{e} = -\frac{\sigma_{SC}b}{e}$$
and since $j_{FM}(-\infty) = j_{SC}(+\infty) := j$ we have
$$a = -\frac{ej}{\sigma_{FM}} b = -\frac{ej}{\sigma_{SC}}$$
From the continuity of up current at x=0 we get <
$$j^{\dagger}(0)_{FM} = -\frac{\sigma_{FM}^{\dagger}}{e} \left(a + \frac{c^{\dagger}}{\lambda_{FM}}\right) = -\frac{\sigma_{SC}/2}{e} \left(b - \frac{d^{\dagger}}{\lambda_{SC}}\right) = j^{\dagger}(0)_{SC}$$
which transforms to
$$c^{\dagger} = -c^{\star} \frac{\sigma_{FM}^{\dagger}}{\sigma_{FM}^{\dagger}}$$

$$-\frac{\sigma_{FM}^{\dagger}}{e} \left(a + \frac{c^{\dagger}}{\lambda_{FM}}\right) = -\frac{\sigma_{SC}/2}{e} \left(b - \left(\frac{c^{\dagger} - c^{\star}}{2}\right)\frac{1}{\lambda_{SC}}\right) \Rightarrow \frac{\sigma_{FM}^{\dagger}}{e} \left(a + \frac{c^{\dagger}}{\lambda_{FM}}\right) = \frac{\sigma_{SC}}{2e} \left(b - c^{\dagger} \left(1 + \frac{\sigma_{FM}^{\dagger}}{\sigma_{FM}^{\dagger}}\right)\frac{1}{2\lambda_{SC}}\right) <$$

Using expressions for *a* and *b* we can relate the above equation entirely to properties of the system (i.e. without arbitrary constants)

$$\frac{\sigma_{FM}^{\uparrow}}{e} \left(-\frac{e j}{\sigma_{FM}} + \frac{c^{\uparrow}}{\lambda_{FM}} \right) = \frac{\sigma_{SC}}{2 e} \left(-\frac{e j}{\sigma_{SC}} - c^{\uparrow} \left(1 + \frac{\sigma_{FM}^{\downarrow}}{\sigma_{FM}^{\uparrow}} \right) \frac{1}{2 \lambda_{SC}} \right)$$

- The equation contains only materials parameters of ferromagnet and semiconductor and "experimental" variable – current
- it allows finding $c^{\scriptscriptstyle \uparrow}$

Heaving found c[†] we can obtain the values of all coefficients of solution of the problem. The coefficients* are (the exact form of expressions is taken verbatim from T. Schäpers [11])

$$c^{\dagger} = -\frac{\lambda_{SC}}{\sigma_{SC}} \frac{e j \beta (1-\beta)}{1 + \frac{\lambda_{SC}}{\lambda_{FM}} \frac{\sigma_{FM}}{\sigma_{SC}} (1-\beta)^2} \qquad c^{\dagger} = +\frac{\lambda_{SC}}{\sigma_{SC}} \frac{e j \beta (1+\beta)}{1 + \frac{\lambda_{SC}}{\lambda_{FM}} \frac{\sigma_{FM}}{\sigma_{SC}} (1-\beta)^2} \qquad \beta = \frac{D_{\dagger}(E_F) - D_{\downarrow}(E_F)}{D_{\dagger}(E_F) + D_{\downarrow}(E_F)}$$

$$d^{\dagger} = -d^{\bullet} = -\frac{\lambda_{SC}}{\sigma_{SC}} \frac{e j \beta}{1 + \frac{\lambda_{SC}}{\lambda_{FM}} \frac{\sigma_{FM}}{\sigma_{SC}} (1 - \beta)^2} \qquad \mu_{off} = +\frac{\lambda_{SC}}{\sigma_{SC}} \frac{e j \beta^2}{1 + \frac{\lambda_{SC}}{\lambda_{FM}} \frac{\sigma_{FM}}{\sigma_{SC}} (1 - \beta)^2} \qquad a = -\frac{e j}{\sigma_{FM}} \qquad b = -\frac{e j}{\sigma_{SC}}$$

Using these coefficients the electrochemical potential for both spin channels, both in ferromagnet and in semiconductor, can be calculated

Using coefficients from previous slide we can plot the electrochemical potential in the ferromagnet and in the semiconductor $\mu^{*,*}(x) = \mu_0^{FM} + a x + c^{*,*}e^{x}$



$$\mu^{\uparrow,\downarrow}(x) = \mu_0^{FM} + a x + c^{\uparrow,\downarrow} e^{x/\lambda_{FM}} \quad \text{for } x \le 0$$

$$\mu^{\uparrow,\downarrow}(x) = \mu_0^{SC} + b x + d^{\uparrow,\downarrow} e^{-x/\lambda_{SC}} \quad \text{for } x > 0$$

- Conductivity of the ferromagnet **10** times higher than that of the semiconductor
- The same spin-diffusion length both in the ferromagnet and in the semiconductor

$$\beta = 0.5$$

$$\lambda_{SC} = 10$$

$$\lambda_{FM} = 10$$

$$\frac{\sigma_{FM}}{\sigma_{SC}} = 10$$

Not that different slopes of μ versus x in both regions reflects different conductivities

Mathematica 9 code to get the plot

Lfm=10; Ssc=1;

FMup and SCup,FMdown and SCdown)

Pidl[Piecewise[[-(e])Sfm) x +cuple], B,Lsc,Lim,Ssc,Sfm]*ExplviLfm] x <=0], (mu0[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x +dup[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x +dup[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x +dup[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x = 0.5 (mu0[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x +dup[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x = 0.5 (mu0[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x +dup[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc) x = 0.5 (mu0[e], B,Lsc,Lim,Ssc,Sfm]*(e])/Ssc)

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Using coefficients from previous slide we can plot the electrochemical potential in the ferromagnet and in the semiconductor $\mu^{\uparrow, \downarrow}(x) = \mu_0^{FM} + a x + c^{\uparrow, \downarrow} e^{x/\lambda_{FM}}$



- electrons from up and down spin channels have different electrochemical potential roughly within spin diffusion length from the ferromagnet/semiconductor interface.
- within the bulk of the semiconductor the potentials are equal.

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Using coefficients from previous slide we can plot the electrochemical potential in the ferromagnet and in the semiconductor $u^{\uparrow,\downarrow}(x) = u^{FM} + a x + c^{\uparrow,\downarrow} a^{TM}$



 Lower conductivity mismatch results in higher difference between μ⁺ and μ⁺ at the interface

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Knowing electrochemical potential and the conductivities (different for both spin channels) we can calculate the currents (the expression here is for a ferromagnet)



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Knowing electrochemical potential and the conductivities (different for both spin channels) we can calculate the currents (the expression here is for a ferromagnet)

$$j^{\uparrow,\downarrow} = -\frac{\sigma_{FM}^{\uparrow,\downarrow}}{e} \frac{\partial \mu^{\uparrow,\downarrow}}{\partial x} = -\frac{\sigma_{FM}^{\uparrow,\downarrow}}{e} \left(a + \frac{c^{\uparrow,\downarrow}}{\lambda_{FM}}e^{x/\lambda_{FM}}\right)$$

note that coefficient c depends only on the total conductivity of ferromagnet and not on channel conductivities (σ^{\dagger} and σ^{\downarrow})



Transport regimes

The characteristic, material, length scales for electron transport are [11]:

- mean free path (both elastic* and inelastic)
- phase-coherence length distance covered before the phase is randomized scattering on phonons
- spin-diffusion length

Size of the sample *L* in relation to characteristic transport lengths determines the transport regime

Diffusive	Classical	λ_{F} ,I $_{\phi}$, I $_{e}$ \ll L
	Quantum	λ_{F} ,I $_{e}$ \ll L <i<math>_{\phi}</i<math>
Ballistic	Classical	λ _F ≪L <i<sub>φ, I_e</i<sub>
	Quantum	$\lambda_{F}, L < I_{e} < I_{\phi}$

 λ_F -Ferrmi wavelength l_{ϕ} -phas-coherence length l_e -mean free path (mfp)



*no energy transfer, e.g., scattering on charged impurity

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Two dimensional electron gas (2DEG)



- the negative voltage applied to a metal gate induces n-type region in its vicinity (inversion layer) that is rich in electron carriers
- in MOSFET transistors this creates a conducting channel between n-type source and drain

"*magnetoelectric effects are precluded from bulk ferromagnetic* metals due to the very short screening length, in films thinner than a few nanometers, spin-dependent charge screening and band level shifting can lead to pronounced electric field-driven changes to magnetic properties." [23]

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InGaAs/InPt heterostructure - two dimensional electron gas (2DEG)



- the electric field in 2DEG is oriented perpendicularly to its plane
- electrons moving from the source to the drain experience the effective magnetic field given by Lorentz transformation [16]:

$$B'_{\parallel} = B \qquad \qquad B'_{\perp} = \frac{(\vec{B} - (\vec{v}/c^2)) \times \vec{E} \perp}{\sqrt{(1 - v^2/c^2)}} \rightarrow B'_{\perp} = \frac{(\vec{v}/c^2) \times \vec{E}}{\sqrt{(1 - v^2/c^2)}}$$

we assume that there is no external magnetic field

• the magnetic field experienced by the electrons is oriented perpendicularly ($\vec{v} \times \vec{E}$) to the plane described by their velocity and the electric field



- charged plates are the source of a magnetic field experienced by moving electrons
- the electrons/spins precess in the magnetic field



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• the effect is analogous to spin orbit coupling responsible for the magnetocrystalline anisotropy (there the electric field is due to the charge of the nucleus)

The Hamiltonian of the interaction can be written as [11]:

 $\hat{H}_{Rashba} = \alpha_R \hat{z} \; (\vec{\sigma} \times \vec{k}),$ $\vec{k} = \vec{p}/\hbar$ -wave vector of the electron α_{R} - Rashba parameter - strength of the coupling

The Rashba parameter depends not only on the mesoscopic electric field acting on electrons in 2DEG but also on the potential gradients due to electron orbitals of the atoms forming the crystal [11_{p.153}, 19].

The greater atomic number the higher α_{R} (example indium or antimony).



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The energy splitting of the electrons in the Rashba magnetic field is [11]: $E_R = \pm \alpha_R |\vec{k}|$

For fixed energy (here Fermi energy) the wave vector difference is given by [11]:

 $\Delta k_{R} = \frac{2m^{*}\alpha_{R}}{\hbar^{2}}$

constant effective mass m^* assumed



Gate control of the spin-orbit interaction

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- MBE grown structures
- the gate electrode was made on the top of the 100-nm-thick SiO₂ insulating layer which covers the hall bar



"We have experimentally demonstrated that α can be controlled by the interface electric field **because the Rashba mechanism is dominant**. This result suggests that the precession of the injected polarized spin can be controlled by the gate voltage. This is the first step for realizing the spin-polarized field effect transistor."



FIG. 5. Gate voltage dependence of the spin-splitting energies Δ_R and the spin-orbit interaction constant α . Circles are the spin-orbit interaction parameters, and triangles are the spin-splitting energy. The open circles and triangles were obtained by fitting the first node positions. The filled symbols were obtained by fitting the second node positions.

images from J. Nitta, T. Akazaki, H. Takayanagi, and T. Enoki, Phys.Rev.Lett. 78, 1335 (1997) [17]

Gate control of the spin-orbit interaction – switching off the coupling?

Asymmetric quantum well (QW) (eg. $Ga_{0.47}In_{0.53}As$ (well), $AI_{0.48}In_{0.52}As$ (left barrier), and $AI_xGa_{1-x}As_ySb_{1-y}$ (right barrier))



FIG. 4. Rashba coefficient α as a function of the external force $F_z = -eE_z^{\text{ex}}$ for three combinations of interfaces: LL, SS, and LS (see text). (a) The well-width (W) dependence for LS. (b) The electron-sheet-density (N_s) dependence for LS. The dimensionless Rashba coefficient is defined by $\tilde{\alpha} = (\alpha/\eta)/(\text{Ry}^*/a_B^*)$. For the definition of other quantities, see the caption of Fig. 3.



FIG. 1. A quantum-well structure consisting of three different semiconductors with the zinc-blende structure, S_B^L , S_W , and S_B^R . $V_{bo}^c(z)$ is the potential due to the conduction-band offset.

- the Rashba coefficient α, which depends on the band offset, can be tuned to be zero by adjusting the Al fraction in the right barrier
- the α coefficient in composition adjusted asymmetric QW can be switched on by changing the polarity of the external field (theory!)
- required field > 10^7 V/m for 20nm thick QW \rightarrow **0.2** V

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images from H. Akera, H. Suzuura, and Y. Egami, Phys. Rev. B 95, 045301 (2017) [18]

Spin relaxation in semiconductors

- "In a diffusive 2DEG, the momentum direction of electron changes frequently, and hence so does the direction of B_{eff}**" [19_{p18}]
- if $\delta \phi$ is the typical spin precession angle between the scattering events and there was N uncorrelated steps then the standard deviation of the precession angle is given by:

 $\sigma(\phi) = \delta \phi \sqrt{N}$

 $N = \frac{t}{\tau}$

- spin relaxation time τ_s is a time after which the standard deviation becomes 1 - the time scale on which spin loses its memory

There are several basic mechanisms responsible for spin relaxation in semiconductors:

- Elliott-Yafet (EY)
- D'yakonov-Perel' (DP)
- Bir–Aronov–Pikus (BAP)
- hyperfine interaction

Elliott–Yafet (EY) - a spin relaxation process caused by scattering via phonons, impurities, boundaries and so on.

- in semiconductors, the spin-up and spin-down states are **mixed by the spin-orbit interaction** of the constituent elements of the host material
- the spin state contains a small component of the opposite spin
- spin polarized electrons can thus flip after each scattering events although the probability of the spin flip might not be so high

Spin relaxation in semiconductors*

 $\vec{k} = \vec{p}/\hbar$ -wave vector of the electron

 α_{p} - Rashba parameter - strength of the coupling

D'yakonov–Perel' (DP) - a spin relaxation process caused by precession in the magnetic field that is due to spin-orbit coupling** $\hat{H}_{Rauble} = \alpha_B \hat{z} \ (\vec{\sigma} \times \vec{k}),$

- in compound semiconductors without a center of inversion symmetry
- the spin degeneracy is lifted by the spin-orbit interaction
- precession starts again after each scattering in a randomly changed field** –
- spin relaxation rate is proportional to the momentum relaxation time

 $\frac{1}{\tau_{spin}} \propto \tau_{momentum}$

-,i.e., the shorter the momentum relaxation time is, the lower the spin relaxation rate is



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Spin control with Rashba effect*

- spin orbit coupling is negligible for non-relativistic particles in vacuum but in semiconductors the spin-orbit interactions is enhanced by about six orders [19]
 Spin FET the key idea is that the spin orientation can be controlled by gate voltage instead of the external magnetic field
- because of the spin relaxation the electron loses its spin memory after certain number of scattering events



In spite of the **known** orientation of the spin entering the channel the orientation of the spin leaving the channel is **not known**

• if the transport through the channel is ballistic the Rashba effect can be used for deterministic control of the spin precession



known orientation of the spin entering the channel and the **known** orientation of the spin leaving the channel Spin control with Rashba effect

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For diffusive (and ballistic) transport the so called **persistent spin helix** (PSH) [11,19] can be used **to suppress DP relaxation**.

PSH: the Rashba spin-orbit interaction strength α is equal to linear Dresselhaus spin-orbit interaction β [19]

- "In this PSH condition, spin polarization is conserved even after scattering events" [19]
- in PSH condition the effective spin-orbit coupling magnetic field is independent of electron's momentum and is directed along (x,-y,0) direction
- the spin precession angle in PSH condition is given by [19]:

$$\Delta \phi = \frac{2 \alpha m^*}{\hbar^2} L$$

L - channel length

persistent spin helix condition*:



known orientation of the spin entering the channel and the **known** orientation of the spin leaving the channel independent of the path of the electron

*"This conservation is predicted to be robust against all forms of spin-independent scattering, including electronelectron interaction, but is broken by spin-dependent scattering and cubic Dresselhaus term" [19] Datta and Das FET spin transistor

• change of the spin precession angle can be used to match the spin orientation of the electrons leaving the "Rashba channel" to the magnetization direction of the drain electrode



image based on Fig. 7.1 of T. Schäpers Semiconductor Spintronics, De Gruyter 2016 [11]

Datta and Das FET spin transistor

 change of the spin precession angle can be used to match the spin orientation of the electrons leaving the "Rashba channel" to the magnetization direction of the drain electrode



Voltage control of perpendicular magnetic anisotropy

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- the perpendicular magnetic anisotropy controlled by the applied voltage
- voltage affects only the interface anisotropy of the CoFeB/oxide interface since the CoFeB film is thick enough in comparison with electrical screening length in metals [21]



- the application of negative (-8V) voltage to Ru induces perpendicular magnetic anisotropy of CoFeB
- the negative bias decreases electron density at interfaces



FIG. 3. Magnetization characteristics of $Co_{0.6}Fe_{0.2}B_{0.2}/MgO/Al_2O_3$ stack with $t_{CoFeB} = 12A$ in a perpendicular magnetic field, observed by polar Kerr measurements. The voltage biases -8 V, 0 V, and +6 V were applied on the top Ru electrode, with the $Co_{0.6}Fe_{0.2}B_{0.2}$ layer grounded.

Spin transistor by anisotropy control - concept

- three terminal device with magnetic tunnel junction (MTJ)
- buffer layers/CrB(2.5nm)/thick-MgO*/CoFeB(2nm)/thin-MgO/ CoFeB(2.2nm)/CoFe(0.8nm)/Ru(0.85nm)/CoFe(2.5nm)/PtMn(15nm)/cap layers on thermally oxidized Si substrates using magnetron sputtering
 *1.7 MΩ•µm²

(b)

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(c)

(d)

Fig. 2. (a) Diagram of the three-terminal structure we fabricated. (b) Scanning electron micrograph of the drain and source junctions after the third stage of the microfabrication process. (c) Scanning electron micrograph of top electrodes to contact the drain and source junctions after the fourth stage of the microfabrication process. (d) Optical micrograph of the completed three-terminal structure. Insets in (b)–(d): magnified image of the region enclosed in dotted lines.

Spin transistor by anisotropy control - **concept**

- three terminal device with magnetic tunnel junction (MTJ) •
- buffer layers/CrB(2.5nm)/thick-MgO*/CoFeB(2nm)/thin-MgO/ • CoFeB(2.2nm)/CoFe(0.8nm)/Ru(0.85nm)/CoFe(2.5nm)/PtMn(15nm)/cap layers on thermally oxidized Si substrates using magnetron sputtering *1.7 MΩ•µm²

SHIOTA et al.: THREE-TERMINAL DEVICE FOR REALIZING A VOLTAGE-DRIVEN

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result of applying V_{GS}."

junction resistance)



image from Y. Shiota et al., IEEE TRANSACTIONS ON MAGNETICS 51, 4200304 (2015)

Magnetoelectric charge trap memory - **concept**

 "a charge-trapping layer integrated into the gate dielectric can provide the missing nonvolatility to the magnetoelectric effect and enhances its efficiency by an order of magnitude" [23]



note the small thickness of Fe layers \rightarrow the screening of electric field in metals

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Magnetoelectric charge trap memory - concept

- charge retained at the MgO/ZrO₂ interface creates a electric field that disturbs the electron density distribution in Fe layer
- this leads to the changes of the effective perpendicular magnetic anisotropy
- Fe layers of a certain thickness, that would be "above" phase reorientation transition without the presence of the electric field can retain in-plane orientation of the magnetic moments as long as there is enough charge on the interface



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Magnetoelectric charge trap memory - concept

- the charges are supplied through an optically assisted process [23]: ITO electrode is a • probable source for hole injection
- MOKE measurements show that the changes in magnetic properties (coercive fields, • remanence) persist at least 24h after the external bias voltage; retention times of several days were observed
- addition of the blocking layer to the dielectric stack (MgO/ZrO₂/InTO) should allow, • according to the authors, for retention times in excess of **10 years**



image (part) from U. Bauer, M. Przybylski, J. Kirschner, and G. S. D. Beach, Nano Lett. 12, 1437 (2012)

- switching of MTJ without magnetic field can be achieved by charge and spin current injection
- the operational speed is limited fundamentally by the spin-precession time to many picoseconds [22]



FIG. 1. All-optical switching of Gd(Fe,Co) films. (a) Schematic of Gd(Fe,Co) film structures. Tantalum layers are used as a buffer and capping to prevent film oxidation. (b) The MOKE image of single bubble domains created via AOS by scanning single subpicosecond laser pulses across the boundary between two large magnetic domains in the sample. (c) The coercivity H_c (blue symbols) and saturated magnetization M_s (red symbols) of Gd(Fe,Co) samples versus their Gd composition (x_{Gd}). Samples with Gd composition in the purple-shadowed region (22%–26%) show AOS behavior. The solid lines are used to guide the eyes.

not patterned

- perpendicularly magnetized Gd(Fe,Co) free layer
- Gd(Fe,Co) cosputtered from Fe₉₀Co₁₀ and Gd targets
- 1.55µm wavelength laser; pulse width 400fs; spot diameter 20µm; fluence 5.8mJ/cm²
- AOS independent of laser polarization (the linear used).
- Laser pulse always reverses the magnetization* (for both orientations of magnetizations – up and down domains)
- Hall effect measurement show almost 100% remanence – rectangular loop

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 to demonstrate the applicability of the system for AOS in realistic spintronic devices MTJ for TMR readout was designed



patterned

*Gd_x(Fe₉₀Co₁₀)_{100-x} layers for x=22 to 26% display AOS [22]

image adapted from Fig. 3 of Jun-Yang Chen, Li He, Jian-Ping Wang, and Mo Li, Phys.Rev. Appl. 7, 021001 (2017) M. Urbaniak

2017

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image adapted from Fig. 3 of Jun-Yang Chen, Li He, Jian-Ping Wang, and Mo Li, Phys.Rev. Appl. 7, 021001 (2017) M. Urbaniak 🗄

fragment of the image



FIG. 3. AOS of an MTJ with subpicosecond single laser pulses without external magnetic field. (a) Schematic of the MTJ structure used in the experiment. (b) Optical microscope image of a typical MTJ device with ITO electrode on the top for TMR measurement. (c), (d) The MOKE images of the MTJ pillar before and after AOS by a single laser pulse, showing the Gd(Fe,Co) layer is completely switched. The pillar diameter is 12 μ m. (e) The $R_{\text{TMR}}(H)$ minor loop measured by sweeping a perpendicular magnetic field, which switches the Co/Pd layers. The red line is the smoothing of the raw data (open circles). (f) R_{TMR} of the MTJ device measured during AOS by 0.4-ps single laser pulses at 0.5-Hz repetition rate. The changes of R_{TMR} in (e) and (f) have the same value of ~0.6 ± 0.05 Ω , indicating the Gd(Fe,Co) layer has been completely switched.

- **0.4ps** long laser pulses are able to switch magnetic moments of Gd(Fe,Co) layers
- the picosecond scale switching mode is 2 orders of magnitude faster than other switching methods [22] but one needs laser etc.
- on a Hall effect device it was demonstrated that 1MHz repetition rate; the system needs more than 10ps to relax to equilibrium
- the authors argue that the ultimate switching rate of AOS device could be higher than • tens of GHz as "subsequent switching can be performed sooner than the system reaches equilibrium" [22]
- the energy required for switching scales inversely with the device area; "for an AOS • device with subwavelength dimensions [...], femtojoule pulse energy should be sufficient to switch it." [22]

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