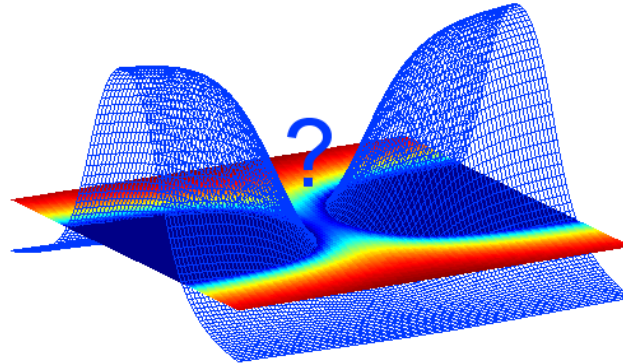


Electron interactions in quantum point contacts

Investigation of the 0.7 and zero-bias anomalies by scanning gate microscopy



Boris Brun¹, F. Martins², S. Faniel², B. Hackens², V. Bayot²,
D. Mailly⁴, U. Gennser⁴, S. Huant¹, M. Sanquer³, **Hermann Sellier**¹

¹Institut Néel (CNRS/UJF), Grenoble (France)

²IMCN/NAPS (UCL), Louvain-la-Neuve (Belgium)

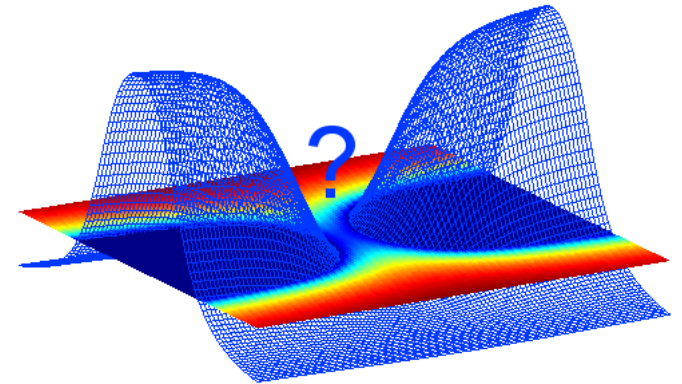
³Institut Nanosciences et Cryogénie (CEA), Grenoble (France)

⁴Laboratoire de Photonique et de Nanostructures (CNRS), Marcoussis (France)

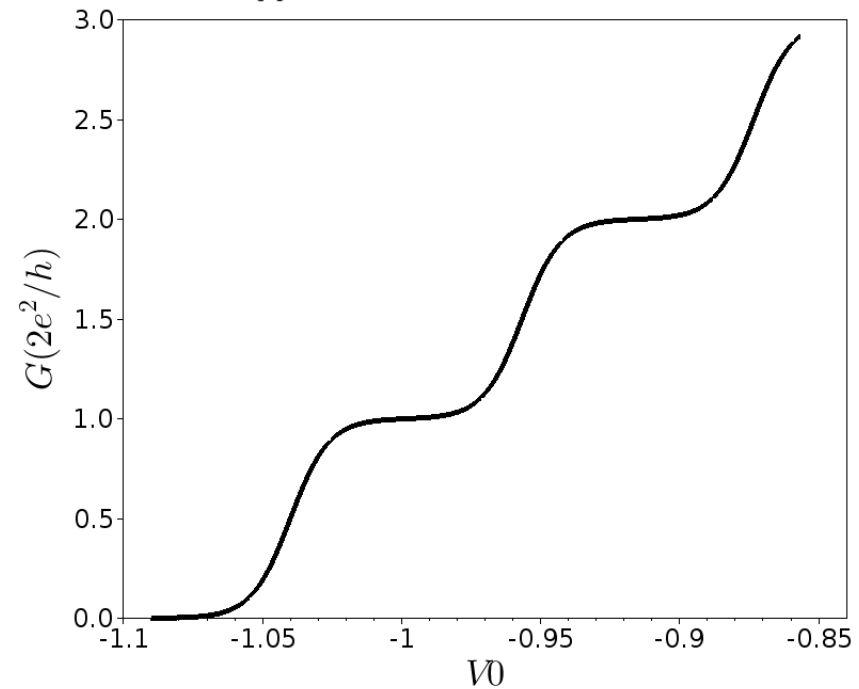
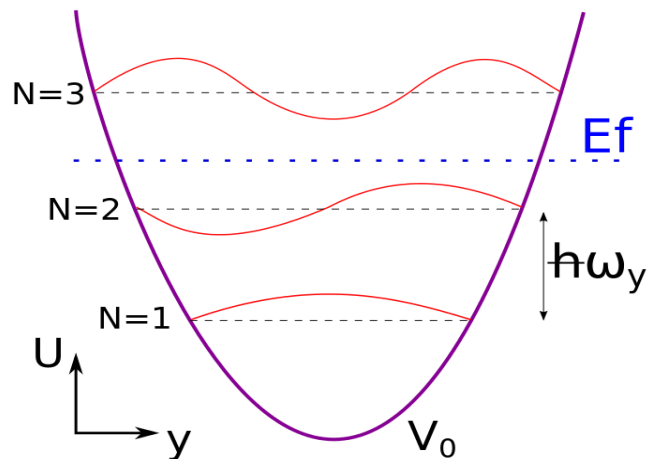
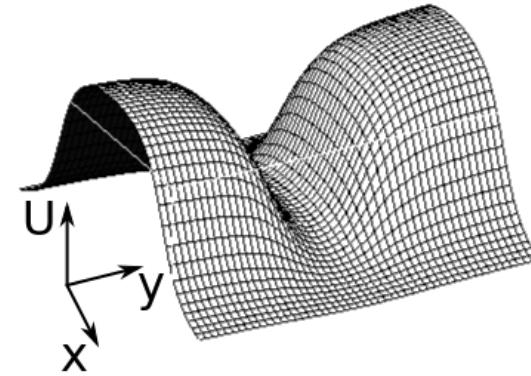
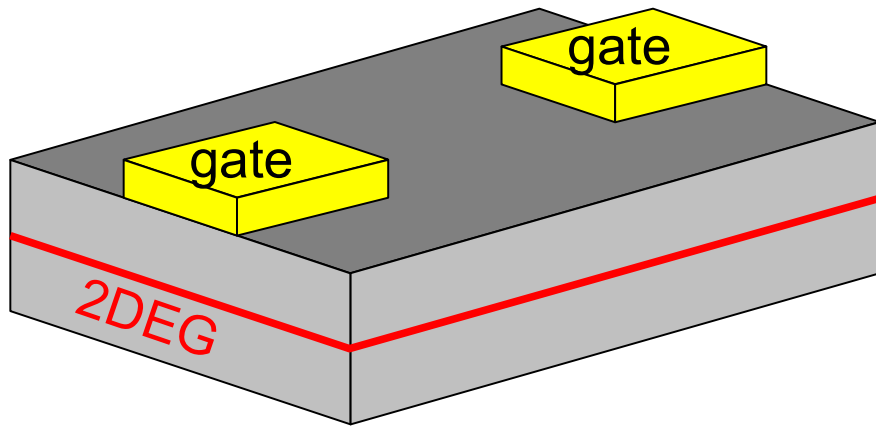
See arXiv:1307.8328

Outline

- Conductance anomalies
- Theoretical models
- Tunable-in-length experiment
- **Scanning gate experiment**
- **Interferometers**
- Conclusion

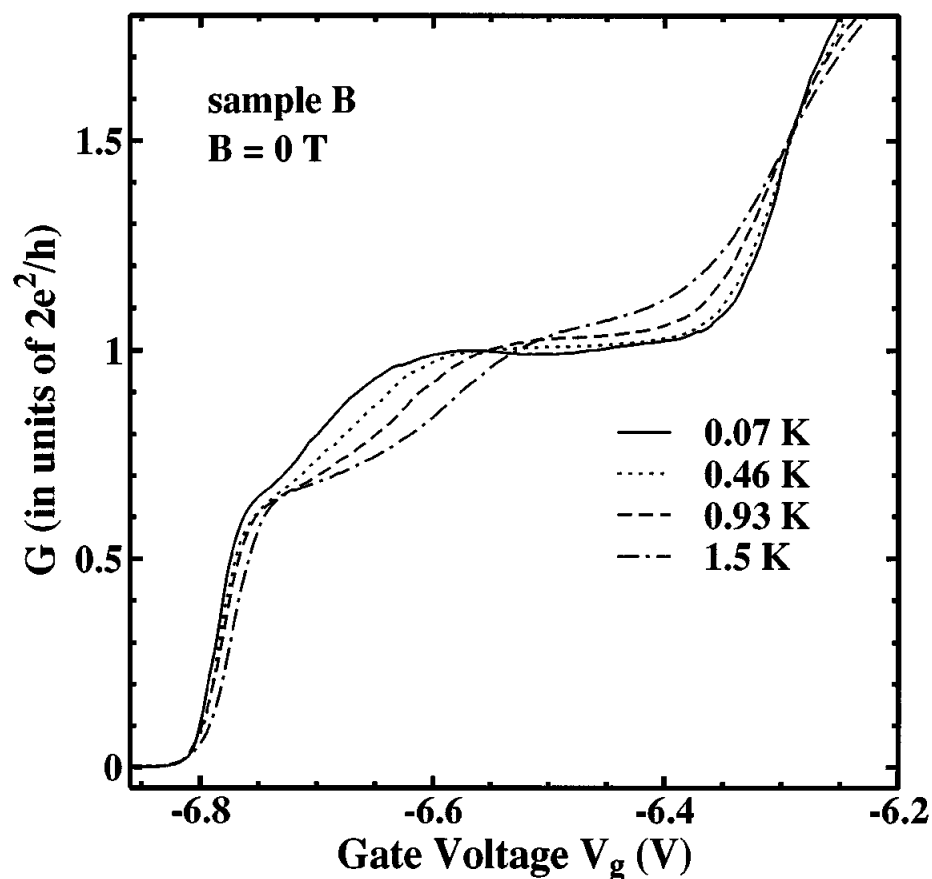
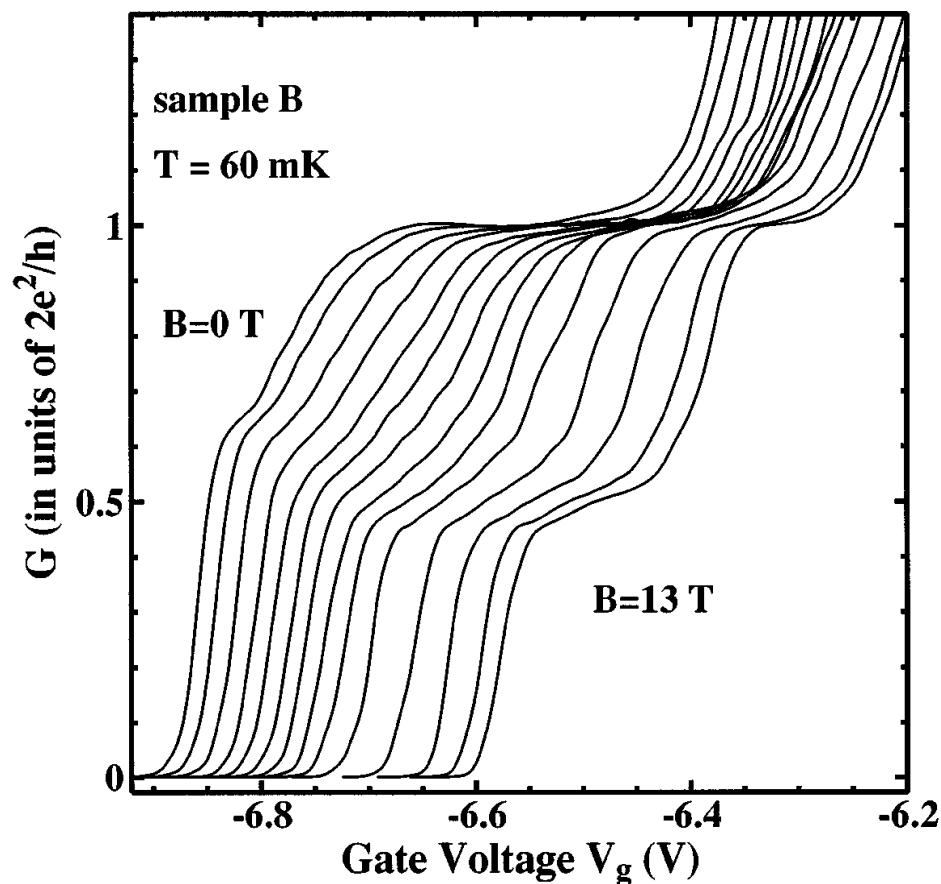


1 – Conductance anomalies : introduction



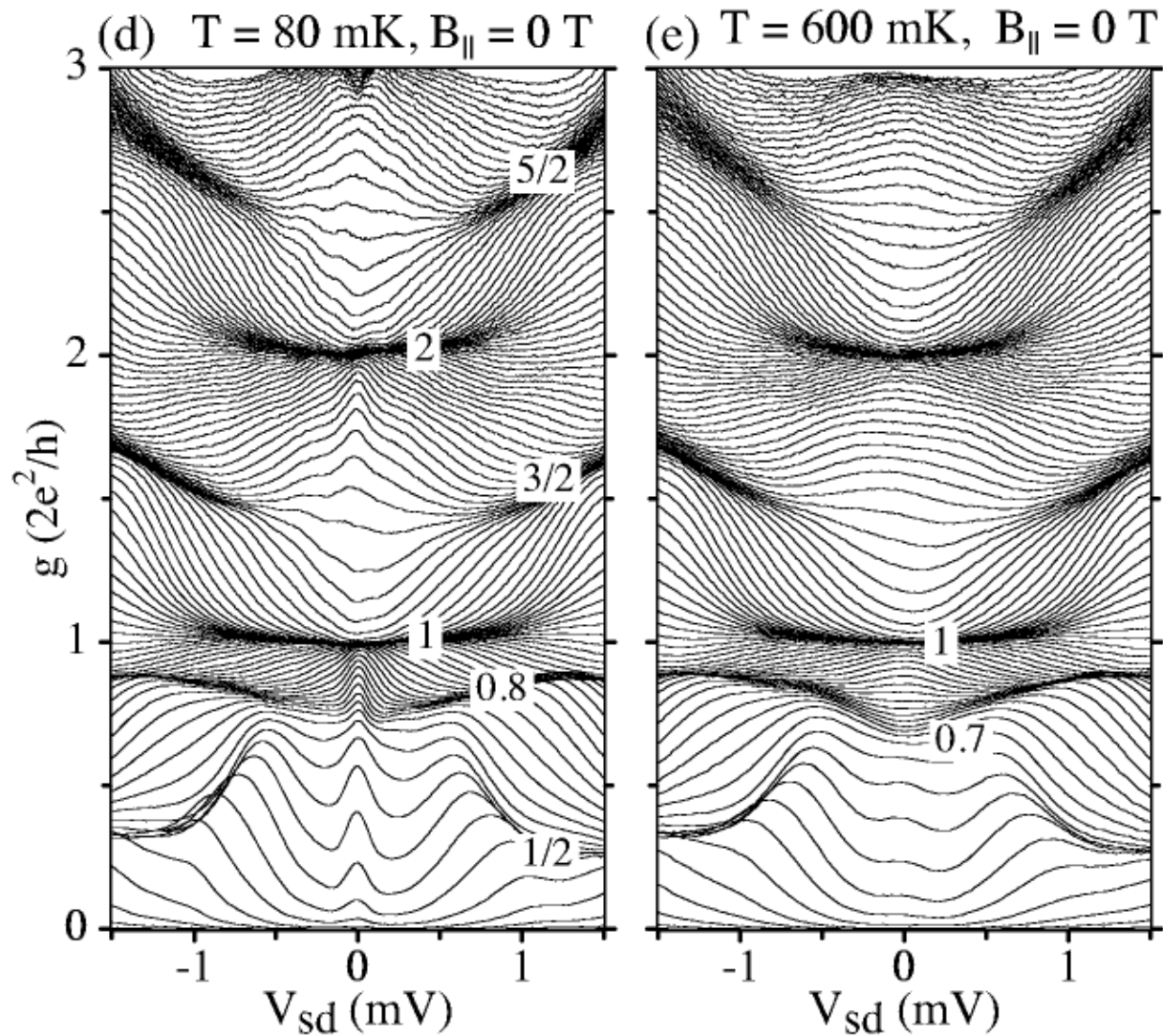
A split-gate defines a quasi-one-dimensional channel in a 2DEG. Quantization of transverse motion \Rightarrow Quantization of conductance.

1 – Conductance anomalies : the 0.7 feature



Thomas, *et al.*, Phys. Rev. Lett. **77**, 135 (1996)

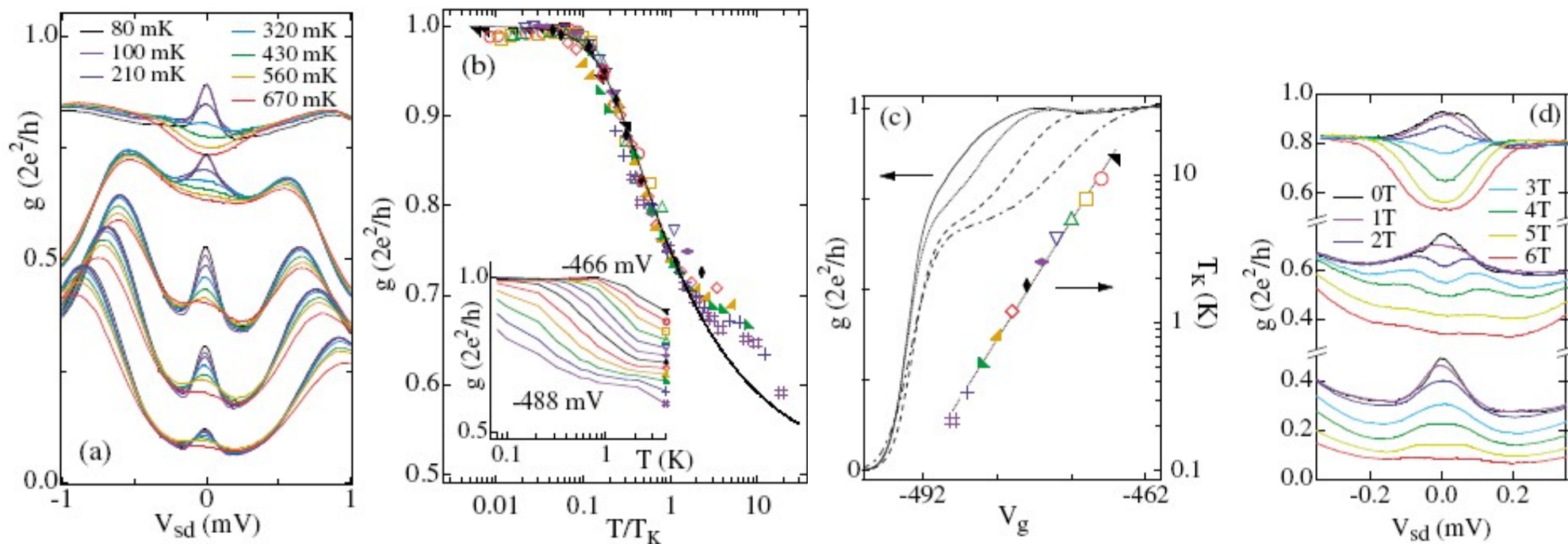
1 – Conductance anomalies : the zero-bias peak



Cronenwett, *et al.*, Phys. Rev. Lett. **88**, 226805 (2002)

1 – Conductance anomalies : the zero-bias peak

Kondo scaling



Cronenwett, *et al.*, Phys. Rev. Lett. **88**, 226805 (2002)

2 – Theoretical models : a long debate

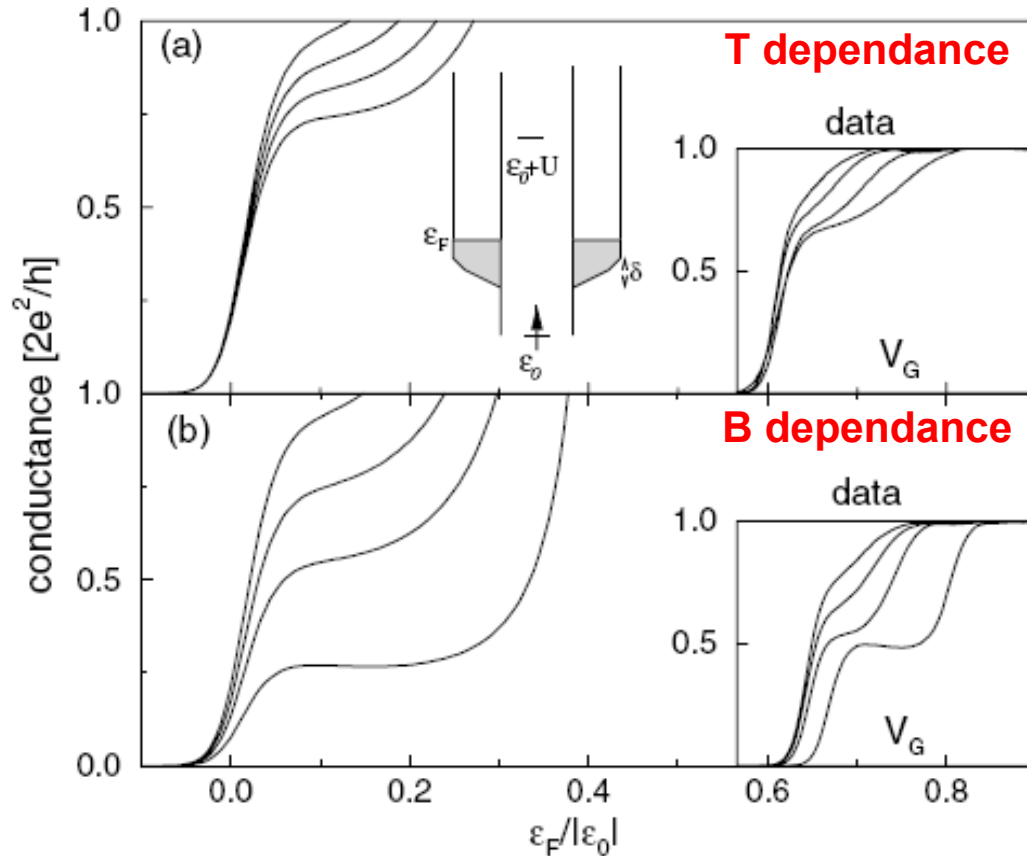
List of models describing the anomalies :

- spontaneous spin polarization: Wang *et al.*, PRB (1998)
- charge density wave: Sushkov, PRB (2001)
- **Kondo effect on a localized state**: Meir *et al.*, PRL (2002)
- electron-phonon scattering: Seelig *et al.*, PRL (2003)
- **one-dimensional Wigner crystal**: Matveev, PRL (2004)
- ...
- van Hove singularity: Bauer *et al.*, Nature (2013)

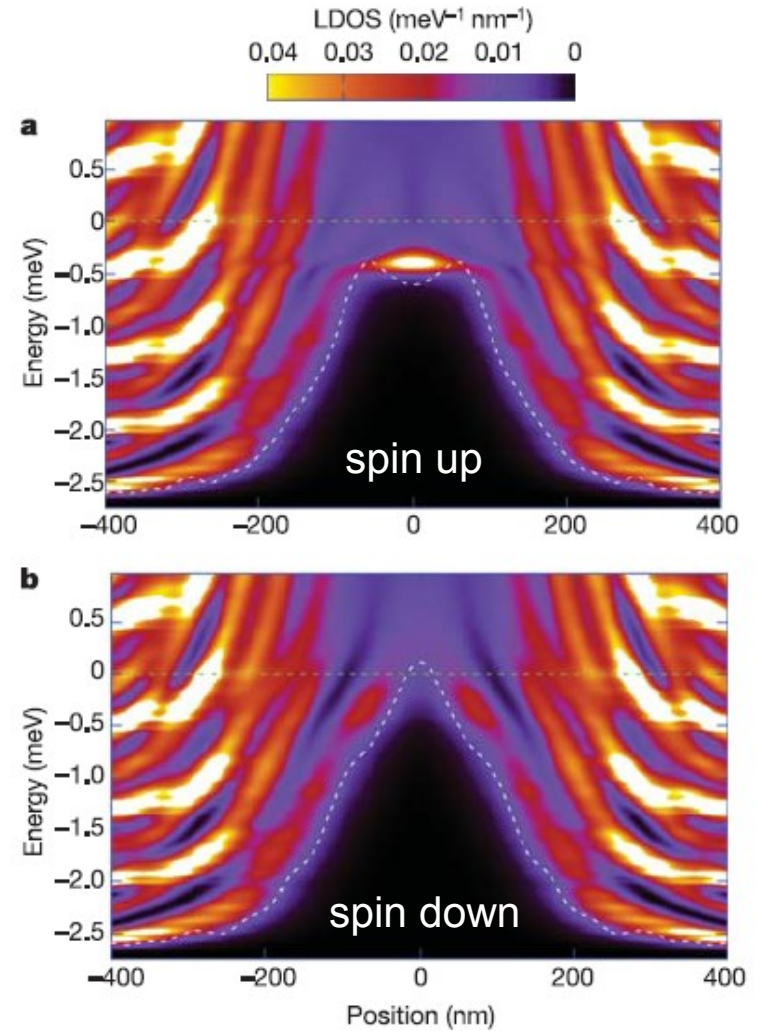
A nice review can be found in :

Micolich, *J. Phys.: Condens. Matter* **23**, 443201 (2011)

2 – Theoretical models : Kondo

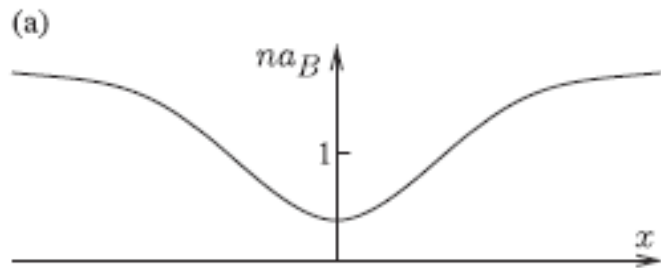
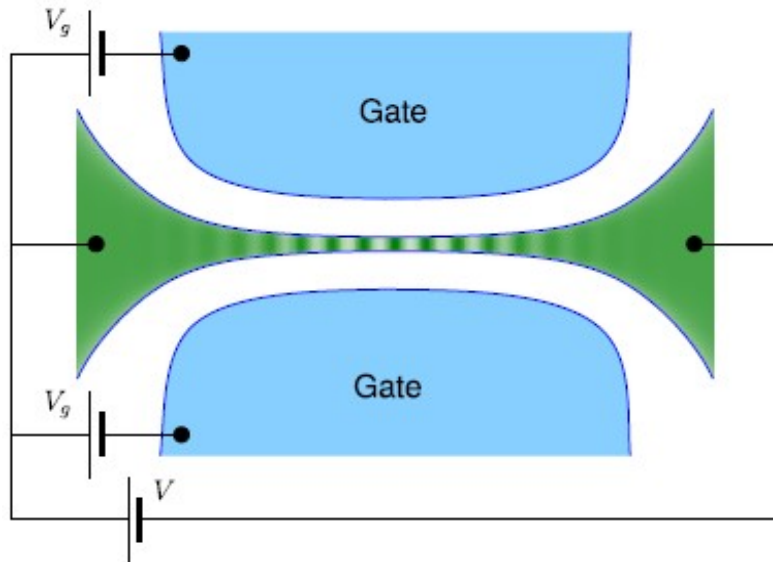


Meir, Hirose, and Wingreen,
Phys. Rev. Lett. **89**, 196802 (2002)

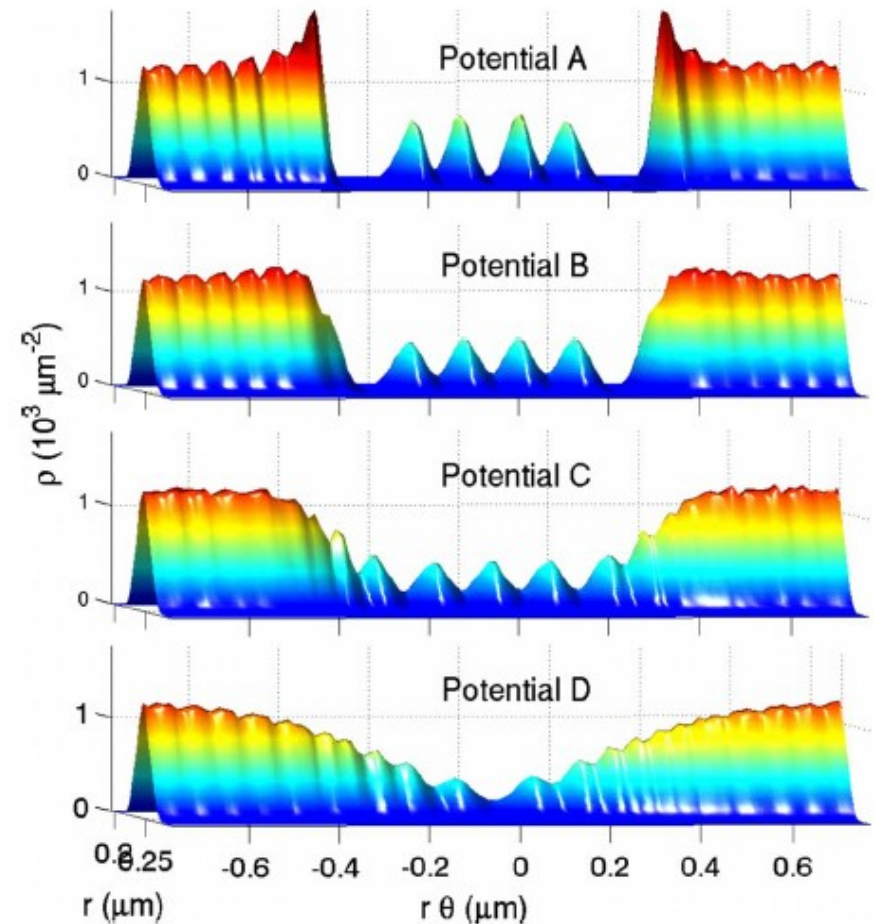


Meir and Rejec,
Nature **442**, 900 (2006)

2 – Theoretical models : Wigner



Matveev,
Phys. Rev. Lett. **92**, 106801 (2004)



Güçlü, *et al.*,
Phys. Rev. B **80**, 201302R (2009)

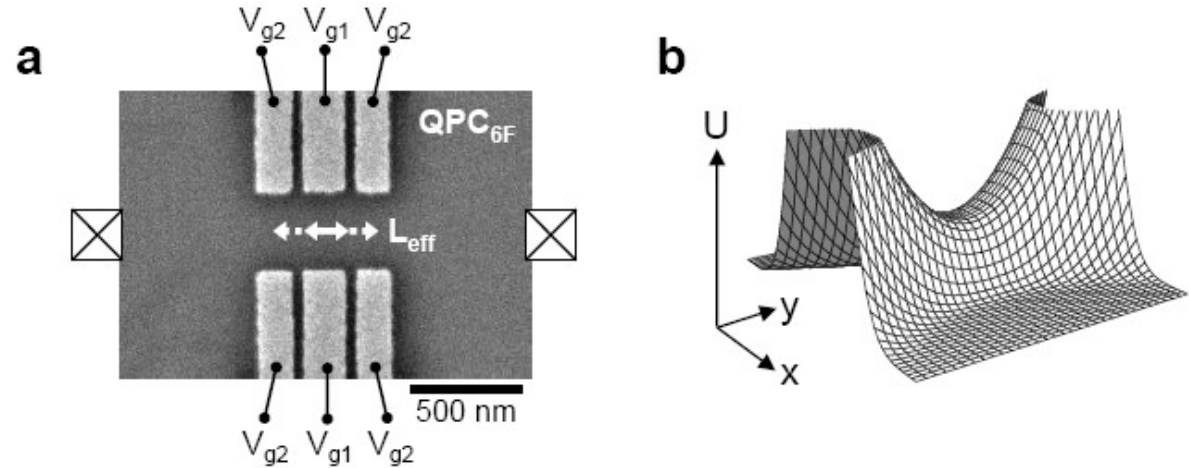
3 – Tunable length experiment

University of Gröningen (NL) : group of **Caspar van der Wal**

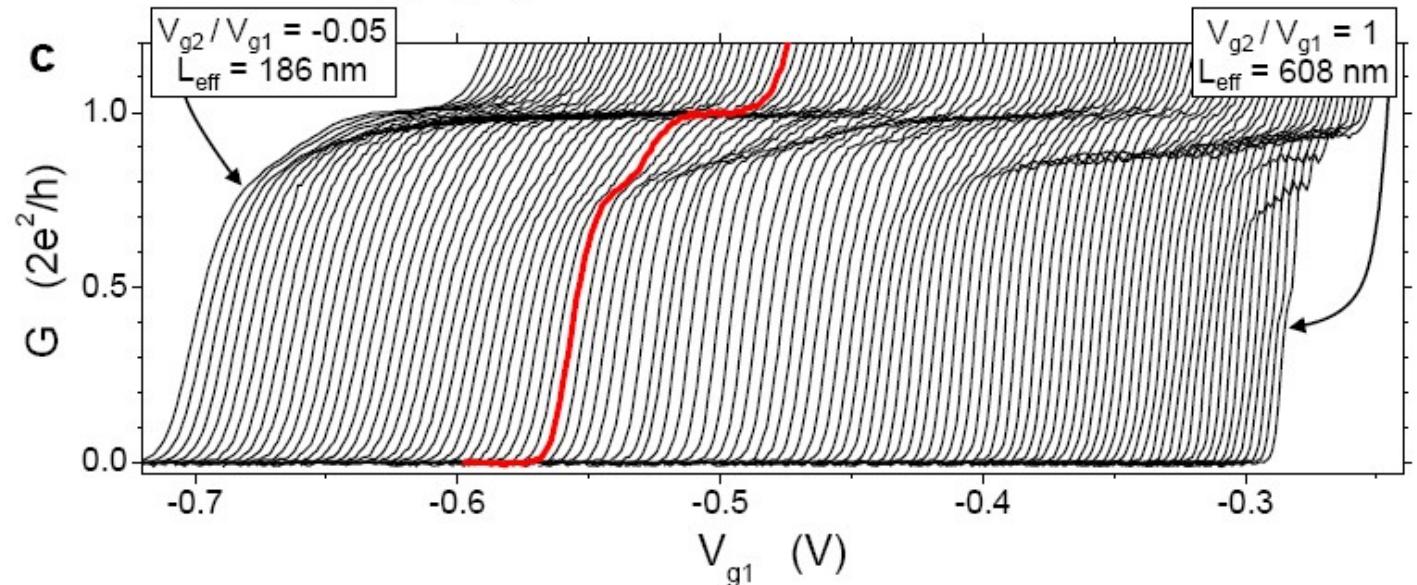
Odd and even Kondo effects from emergent localization in quantum point contacts

Iqbal, et al., Nature **501**, 79 (28 August 2013)

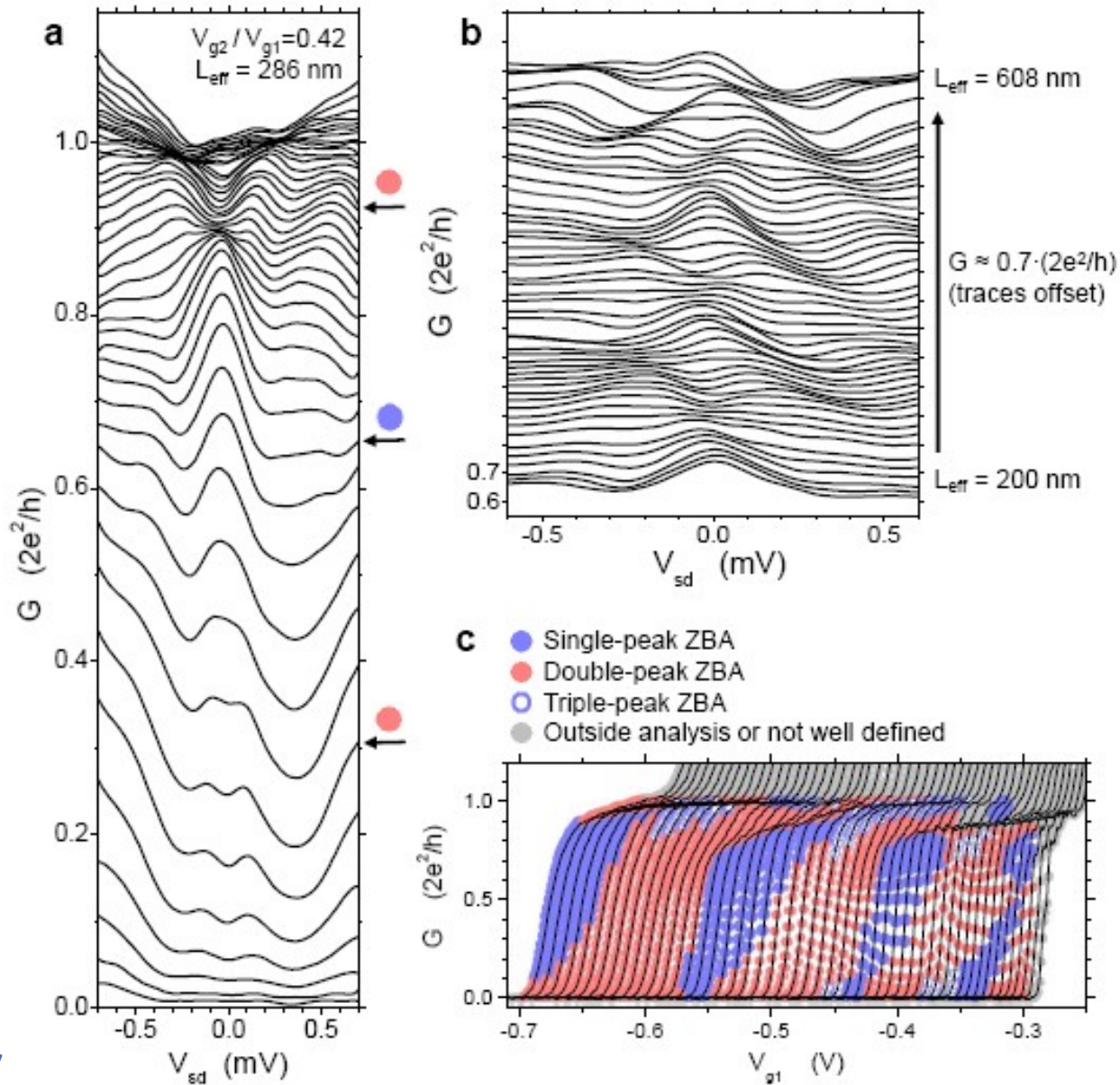
QPC channel length continuously tunable from 200 to 600 nm



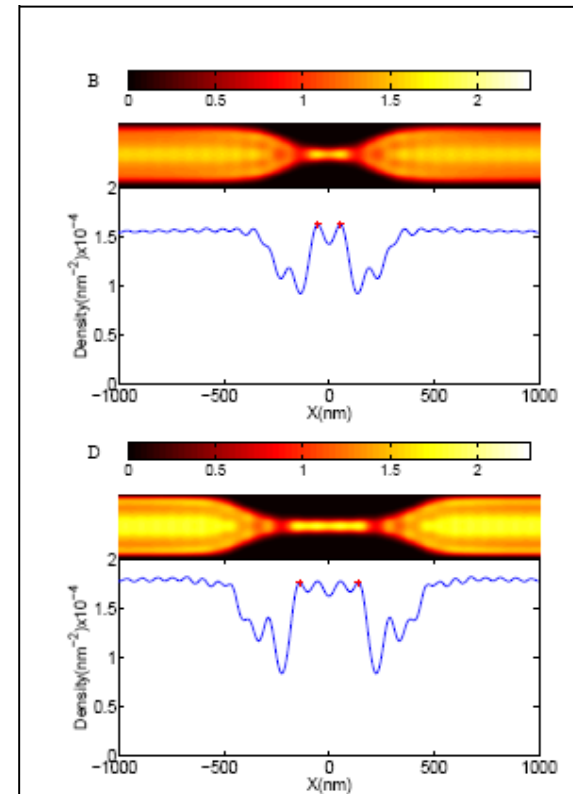
Successive appearances of the 0.7 anomaly versus channel length



3 – Tunable length experiment



Successive ZBA splittings :
- versus gate voltage
- versus channel length



Theoretical model :
Ygal Meir

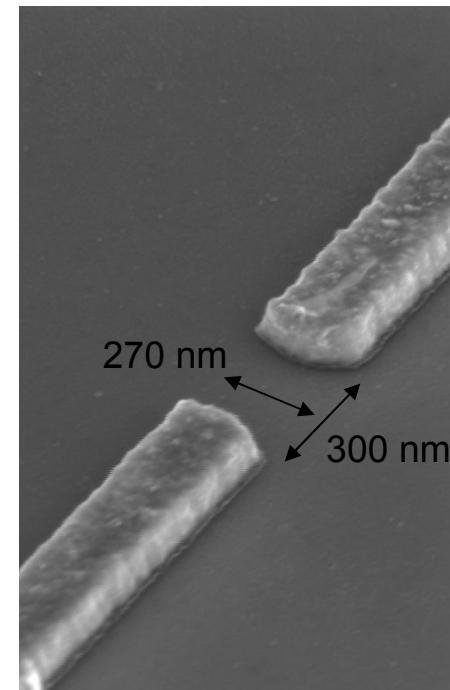
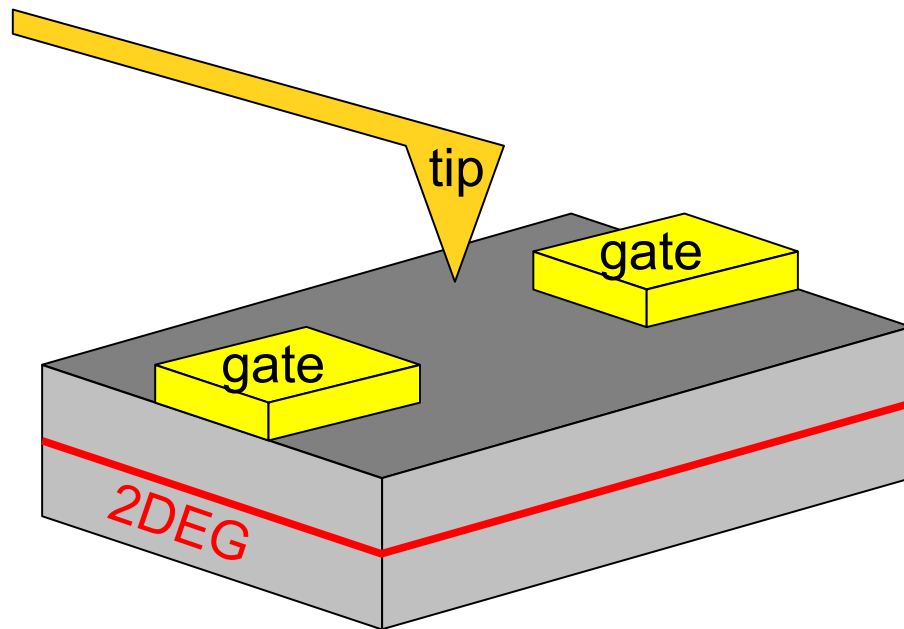
4 – Scanning gate experiment

NEEL, Grenoble (France) : **B. Brun, H. Sellier**

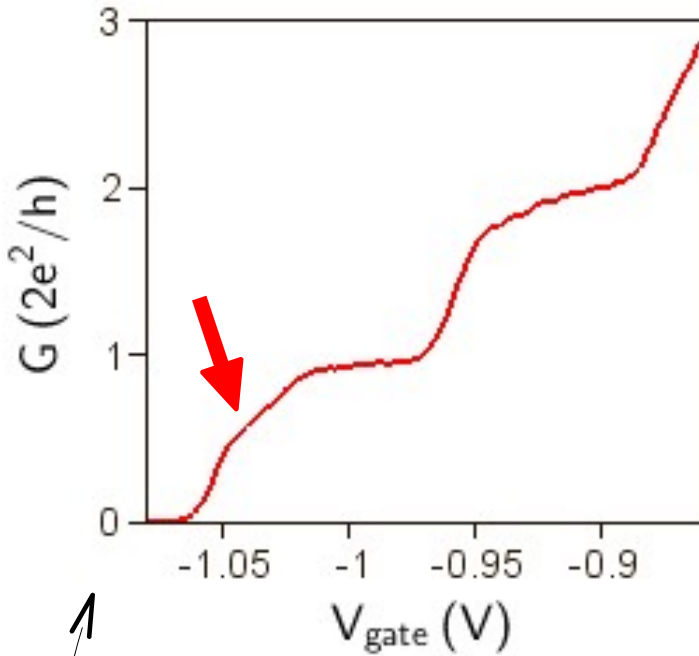
INAC, Grenoble (France) : M. Sanquer : 100 mK transport experiments

UCL, Louvain-la-Neuve (Belgium) : B. Hackens, V. Bayot : 20 mK SGM experiments

LPN, Marcoussis (France) : U. Gennser, D. Mailly : 2DEG and QPC fabrication

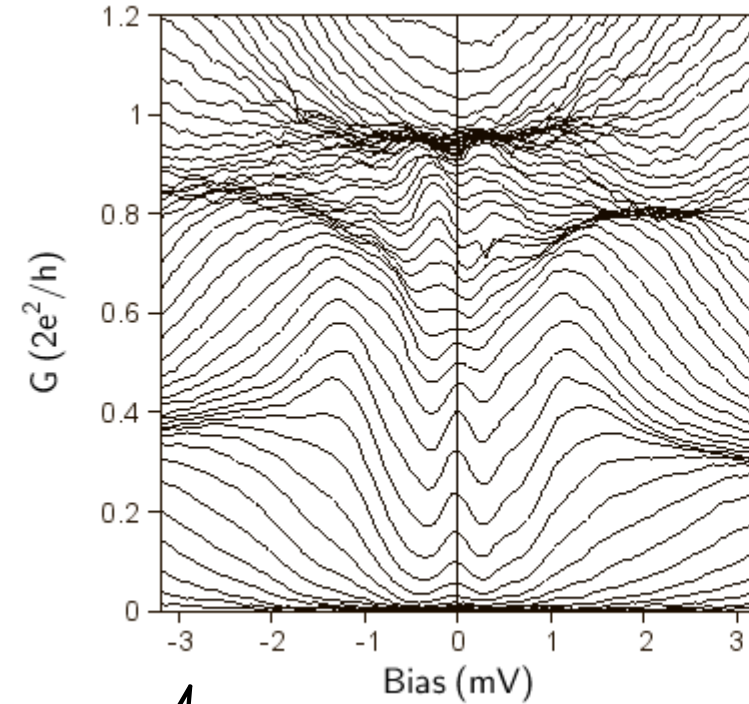
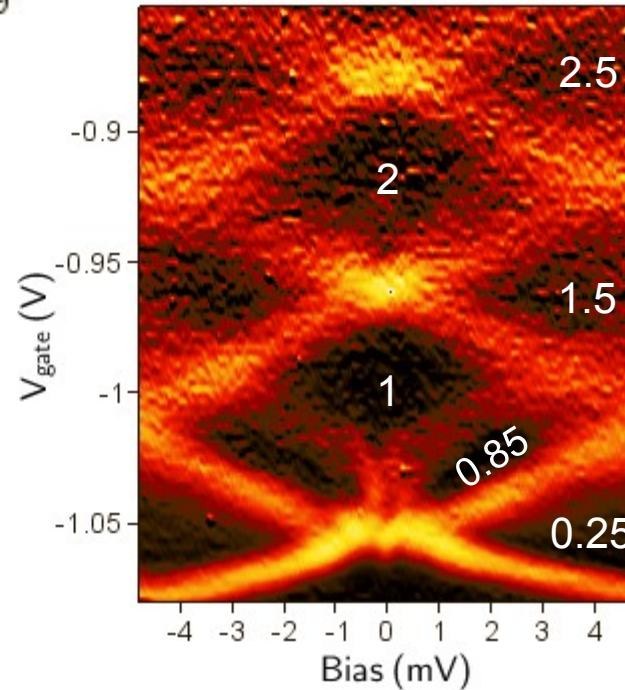


4 – Scanning gate experiment : transport



T = 20 mK
for all the data
(transport and SGM)

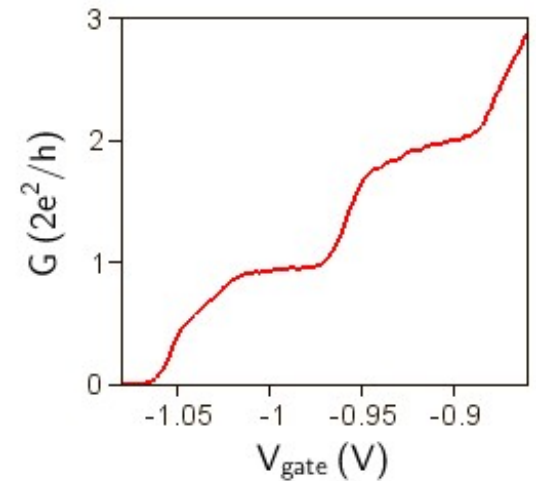
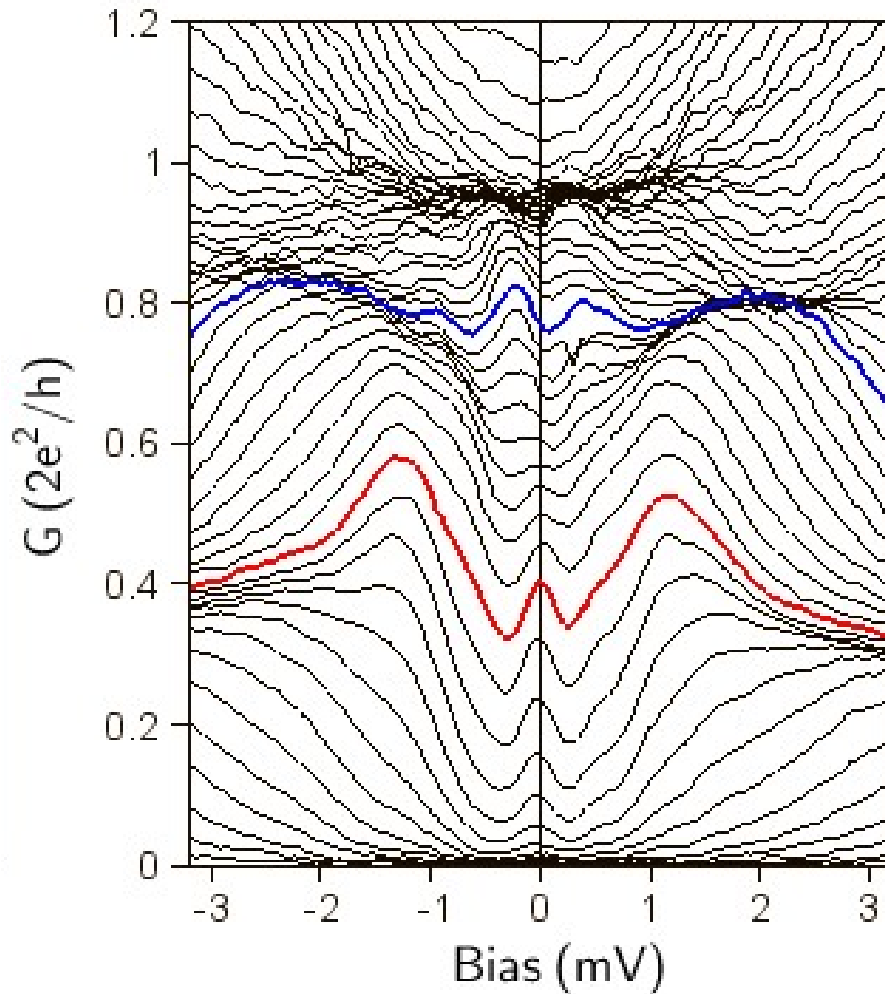
↑
Linear conductance :
0.7 anomaly



↑
Non-linear conductance :
zero-bias anomaly

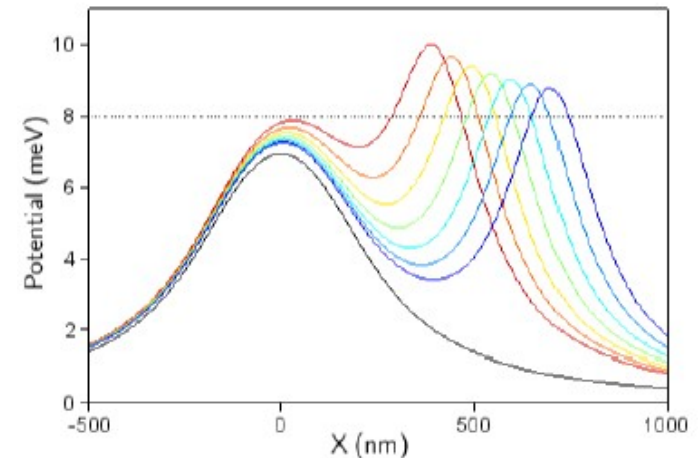
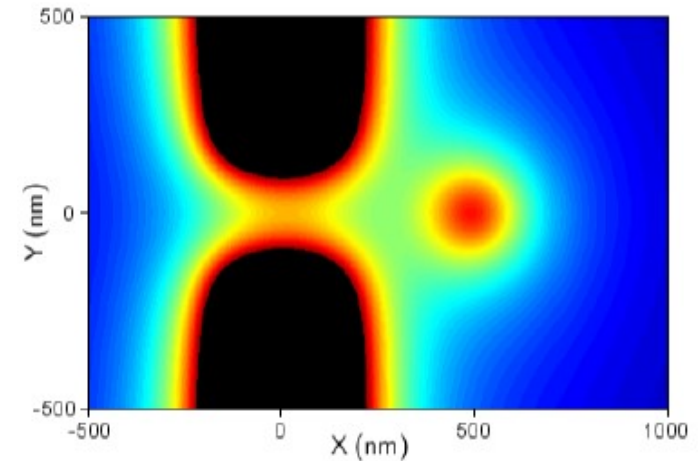
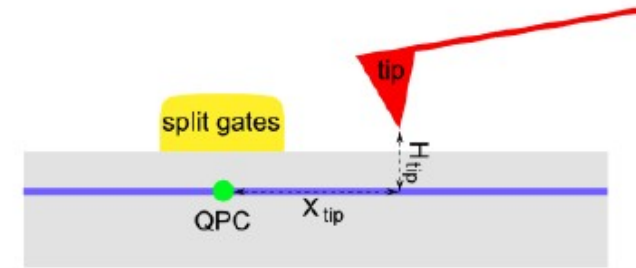
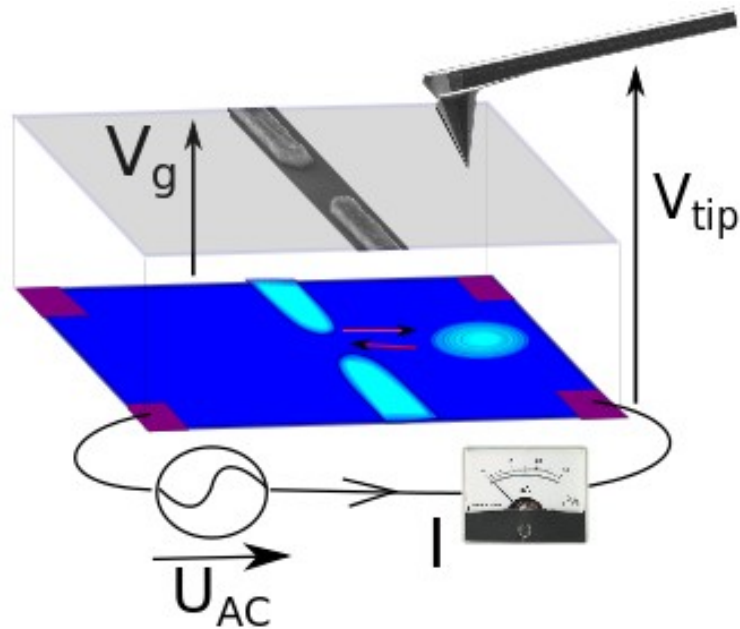
4 – Scanning gate experiment : transport

The **zero-bias peak** splits into **finite-bias peaks** versus gate voltage.



4 – Scanning gate experiment : principle

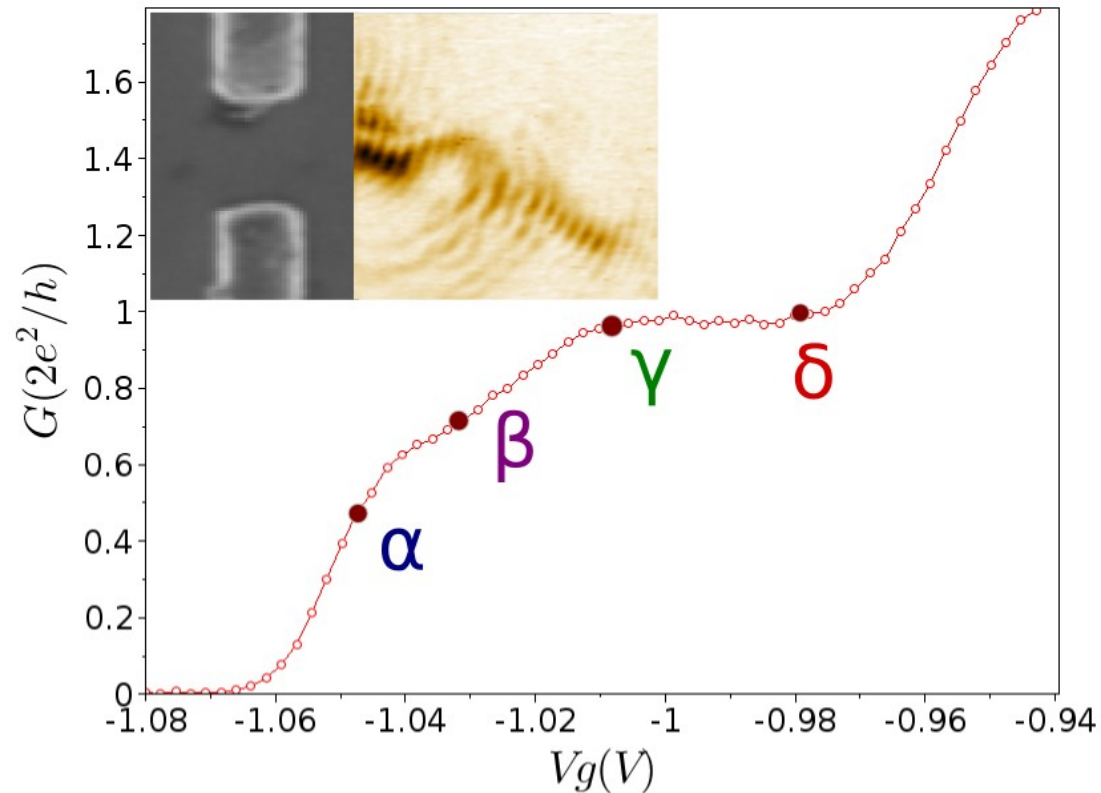
- gate voltage V_g
- tip voltage V_{tip}
- tip position X_{tip} Y_{tip} Z_{tip}
- device bias V_{ds}
- device conductance $G = I_{AC} / U_{AC}$



see also Topinka *et al.*, Nature (2001)
see also Crook *et al.*, Science (2006)

4 – Scanning gate experiment : parameters

QPC parameters :



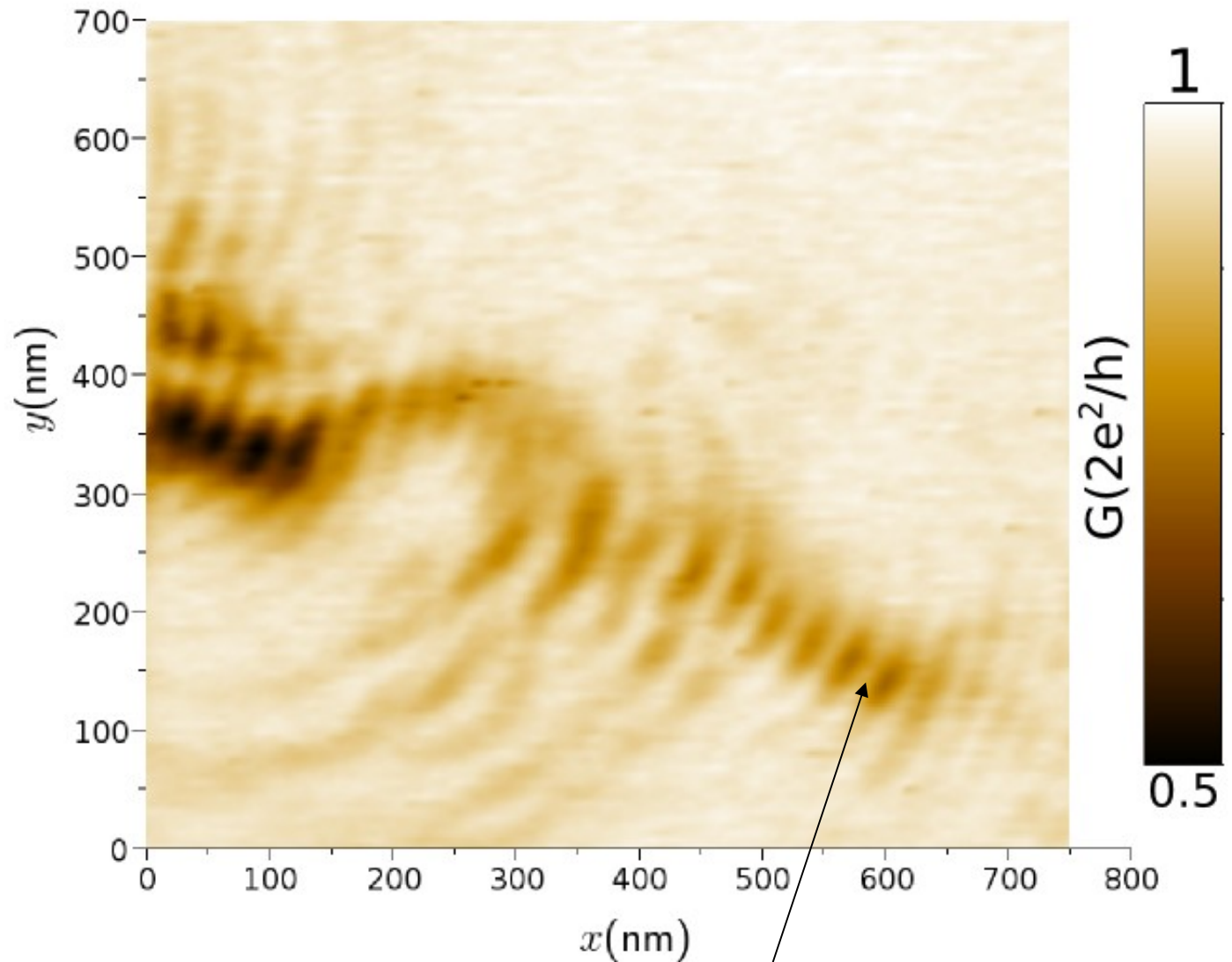
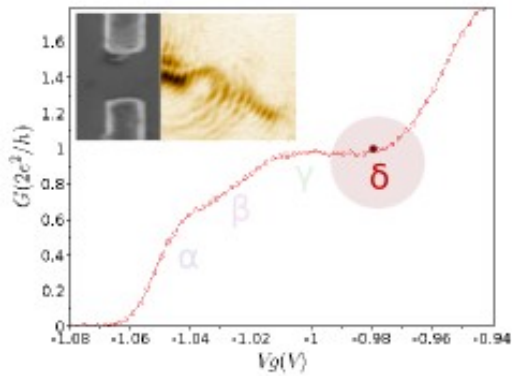
Tip parameters :

$$V_{\text{tip}} = -6 \text{ V}$$

$$Z_{\text{tip}} = 40 \text{ nm above the surface}$$

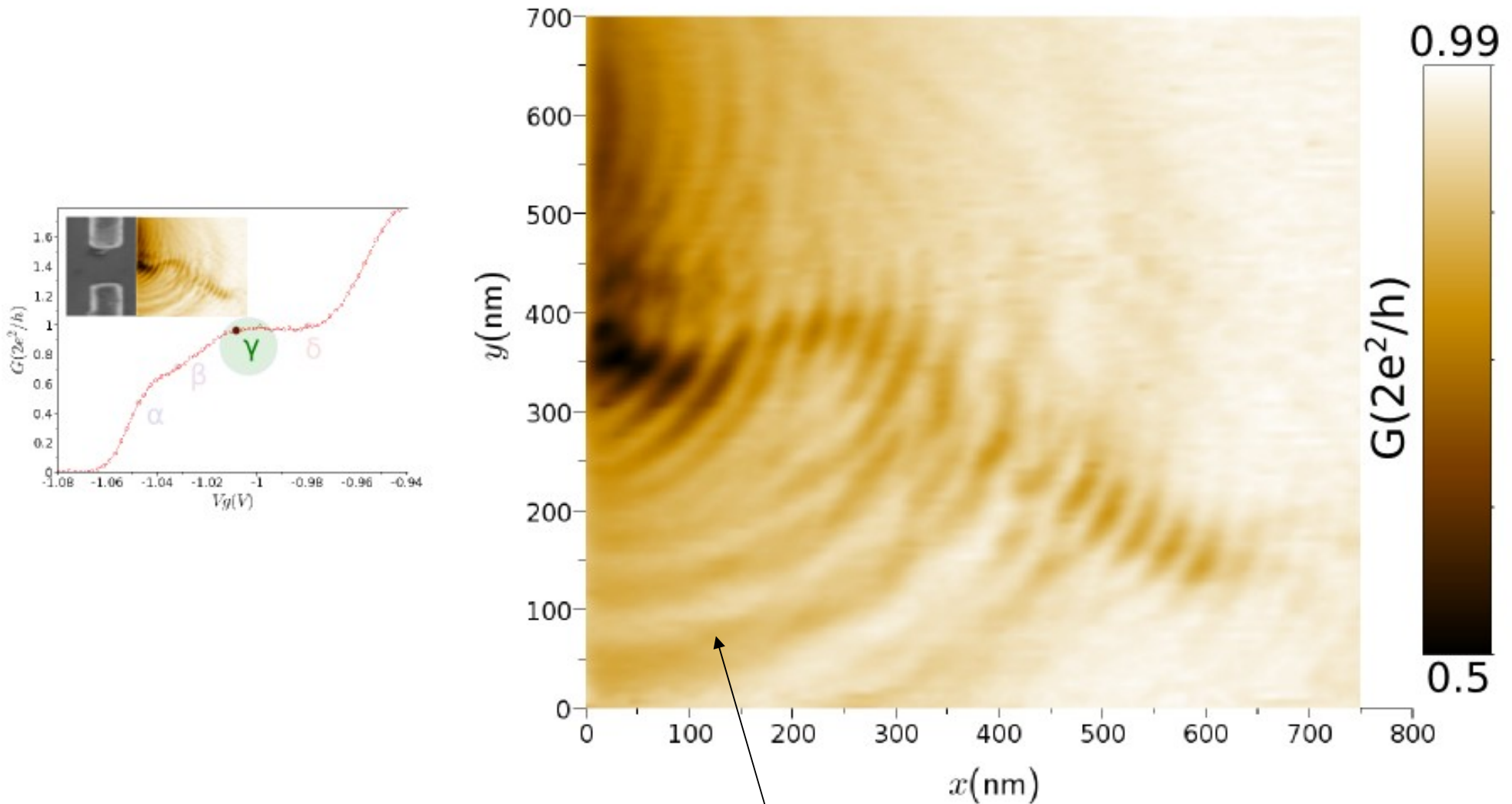
$$H_{\text{tip}} = 140 \text{ nm including 2DEG depth}$$

4 – Scanning gate experiment : horizontal maps



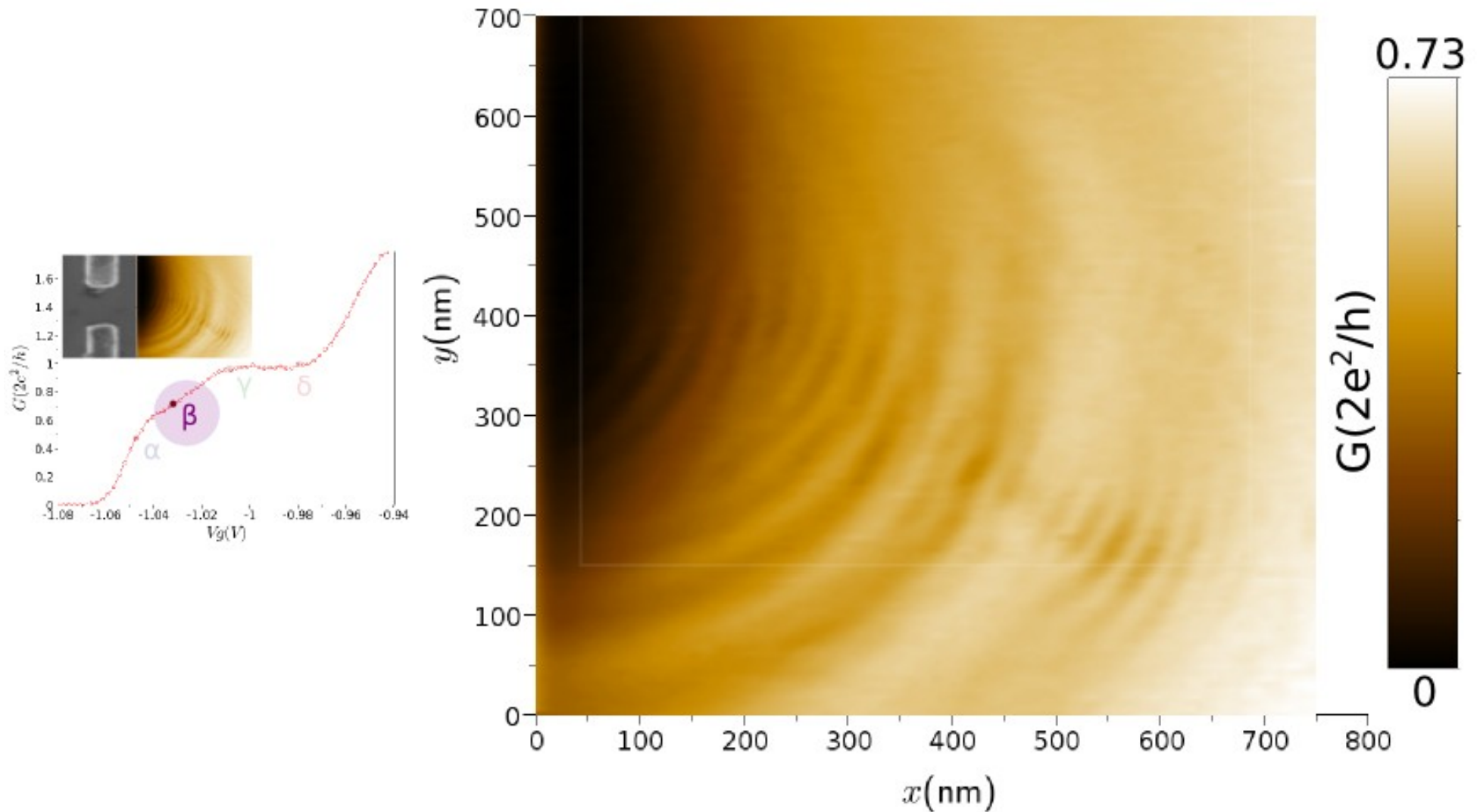
SGM maps reveal electron flow and interference fringes

4 – Scanning gate experiment : horizontal maps



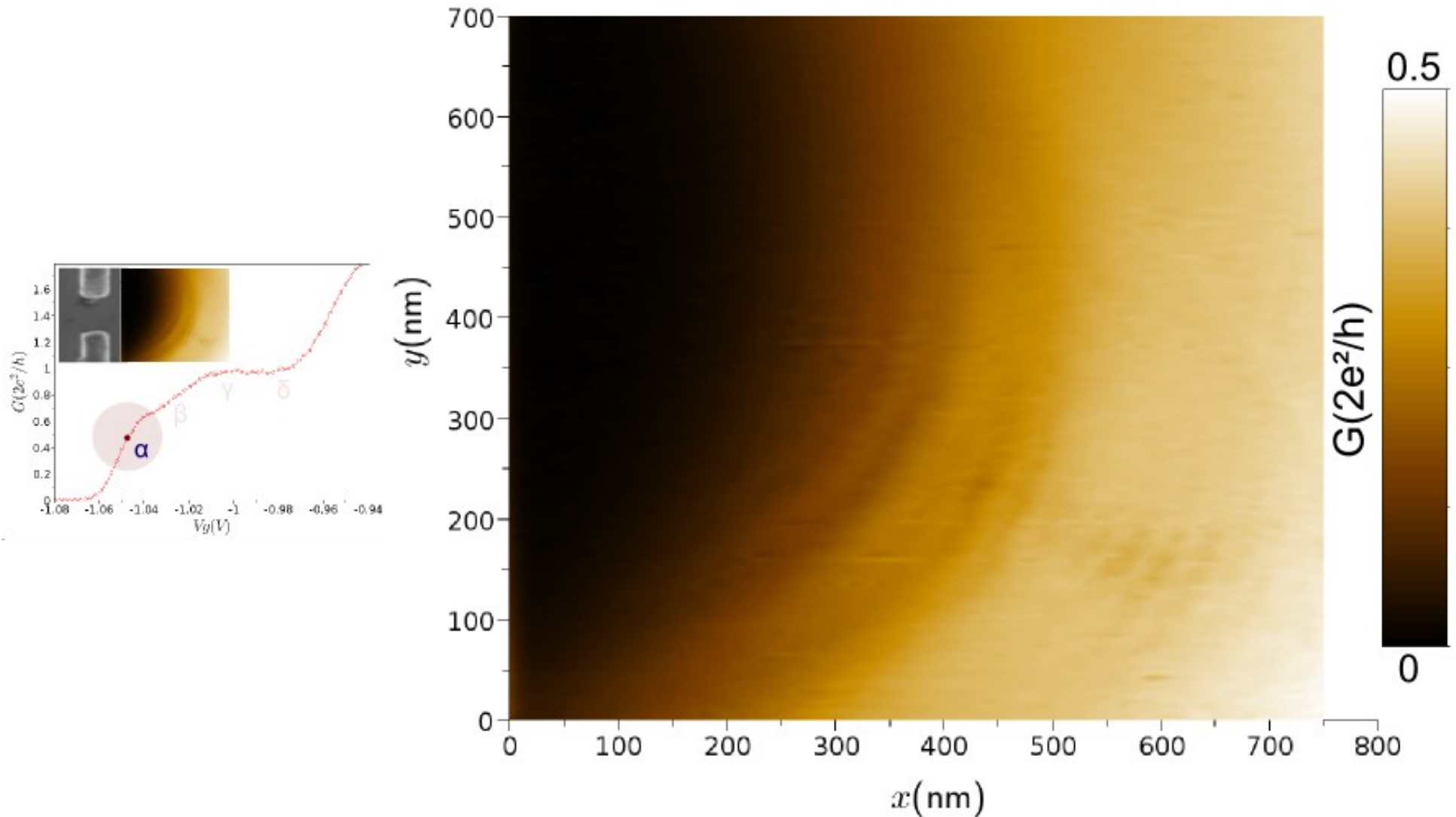
Another kind of conductance oscillations appears below $G=2e^2/h$

4 – Scanning gate experiment : horizontal maps



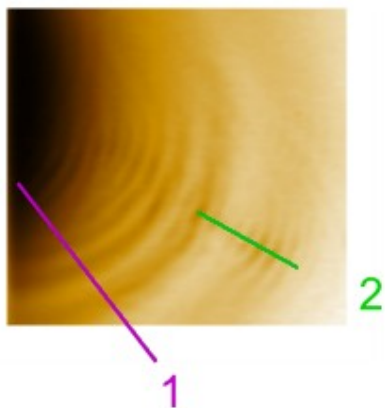
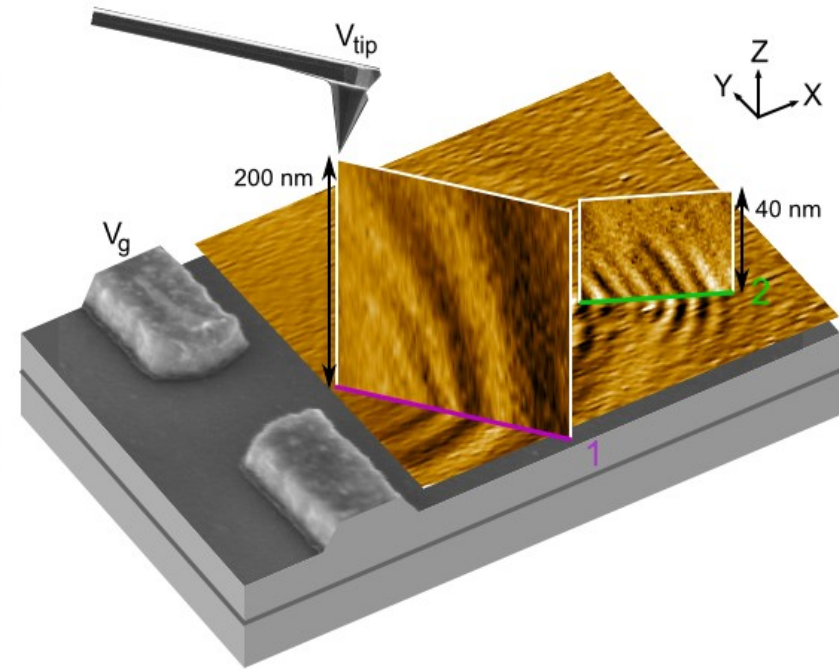
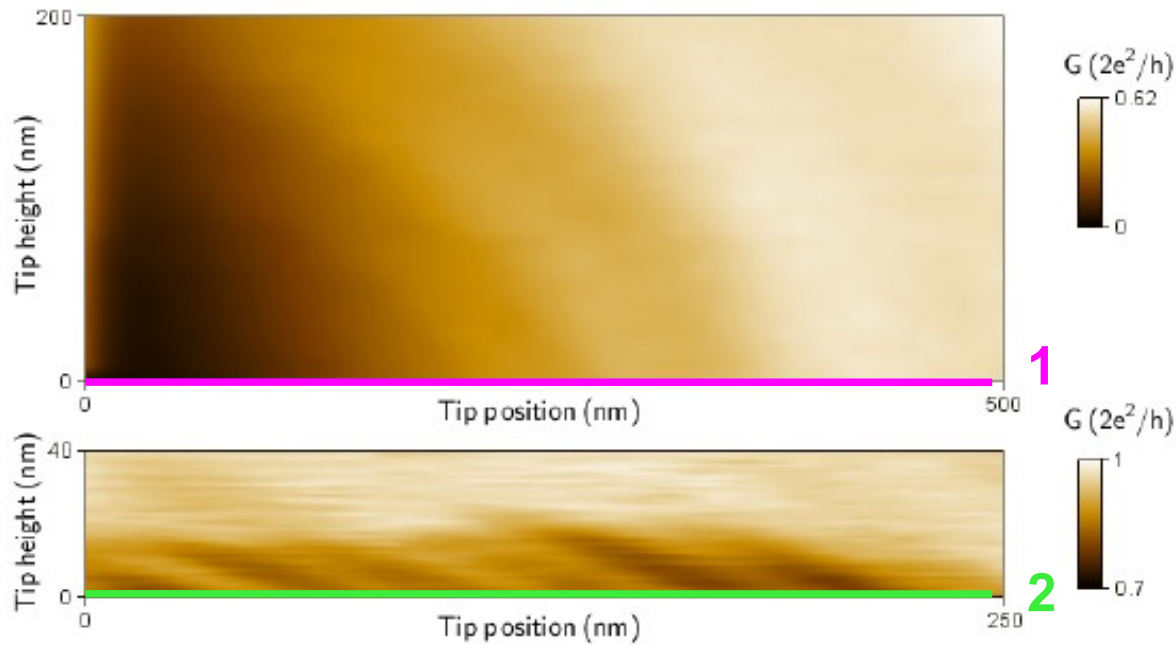
Conductance oscillations below $G=2e^2/h$ have increasing spacing with tip distance

4 – Scanning gate experiment : horizontal maps



Oscillations are still visible below $0.5 \times 2e^2/h$ before the QPC channel is closed

4 – Scanning gate experiment : vertical maps



Line 1 :

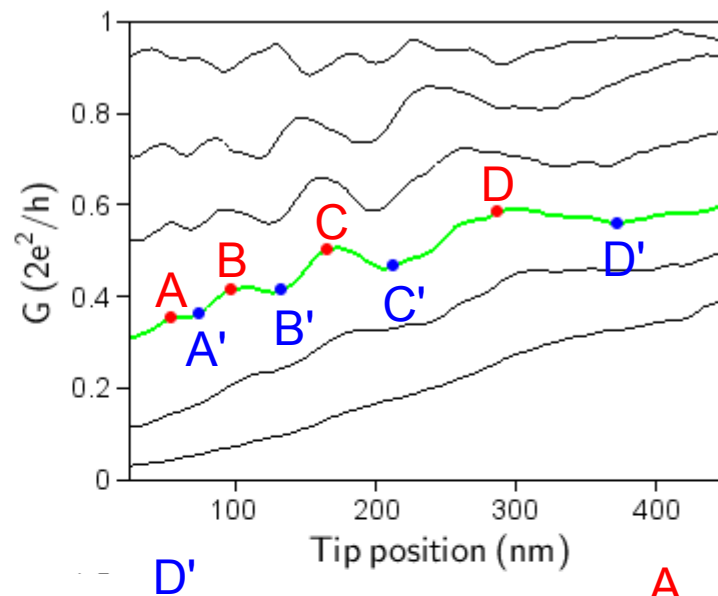
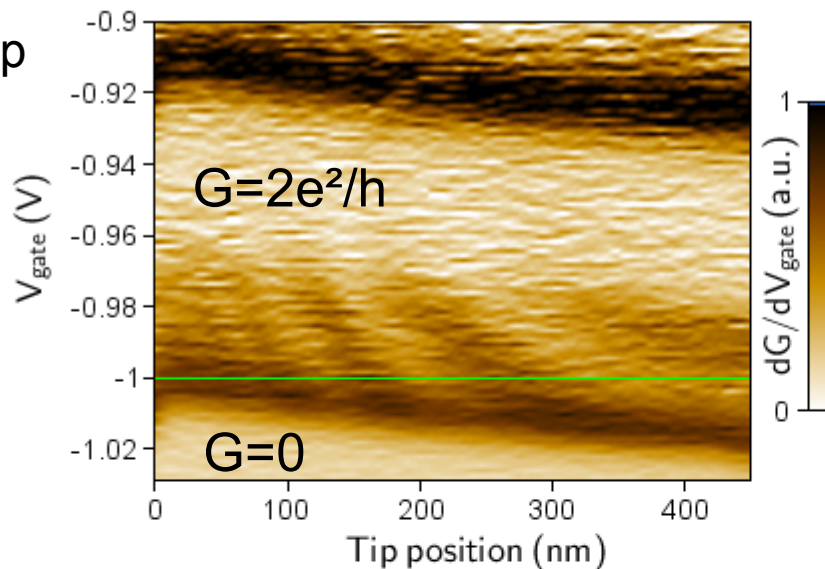
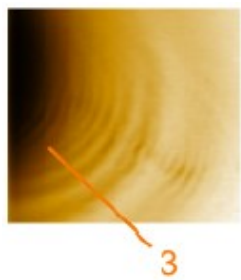
- circular rings extend isotropically around the QPC
- they do not depend on 2DEG potential below the tip
- they induce a direct tuning of the QPC potential

Line 2 :

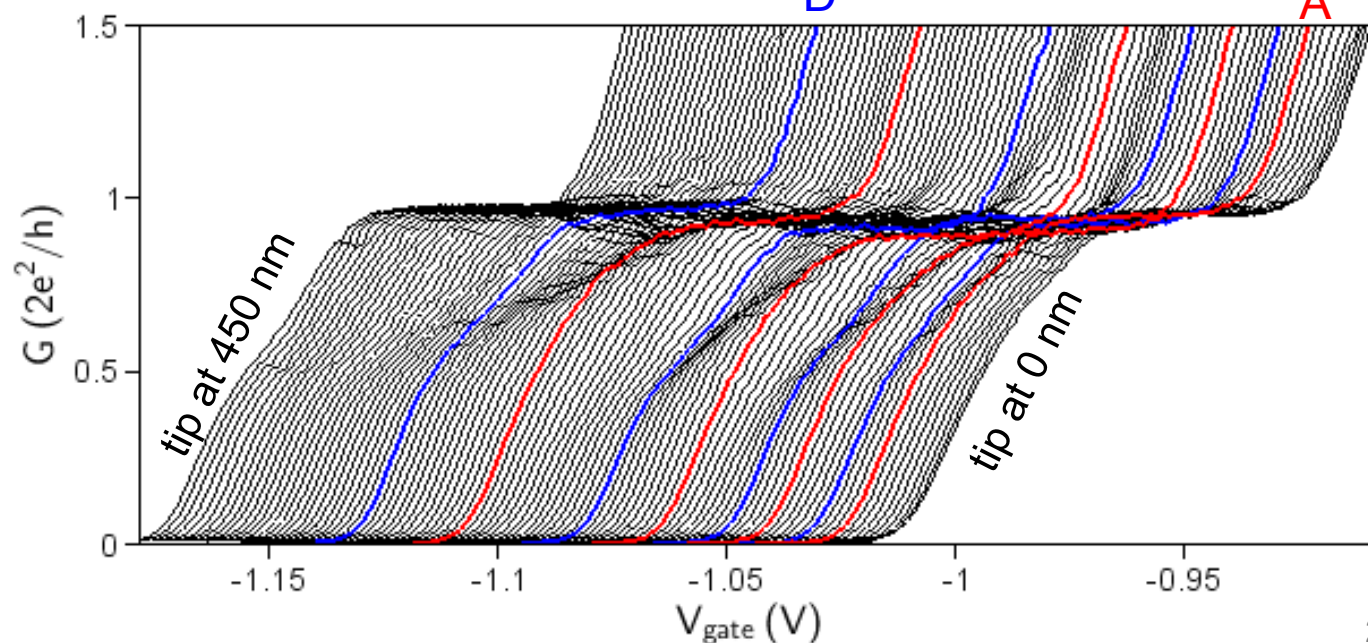
- interferences and back-scattering disappear simultaneously
- the 2DEG should be depleted below the tip

4 – Scanning gate experiment : the 0.7 anomaly

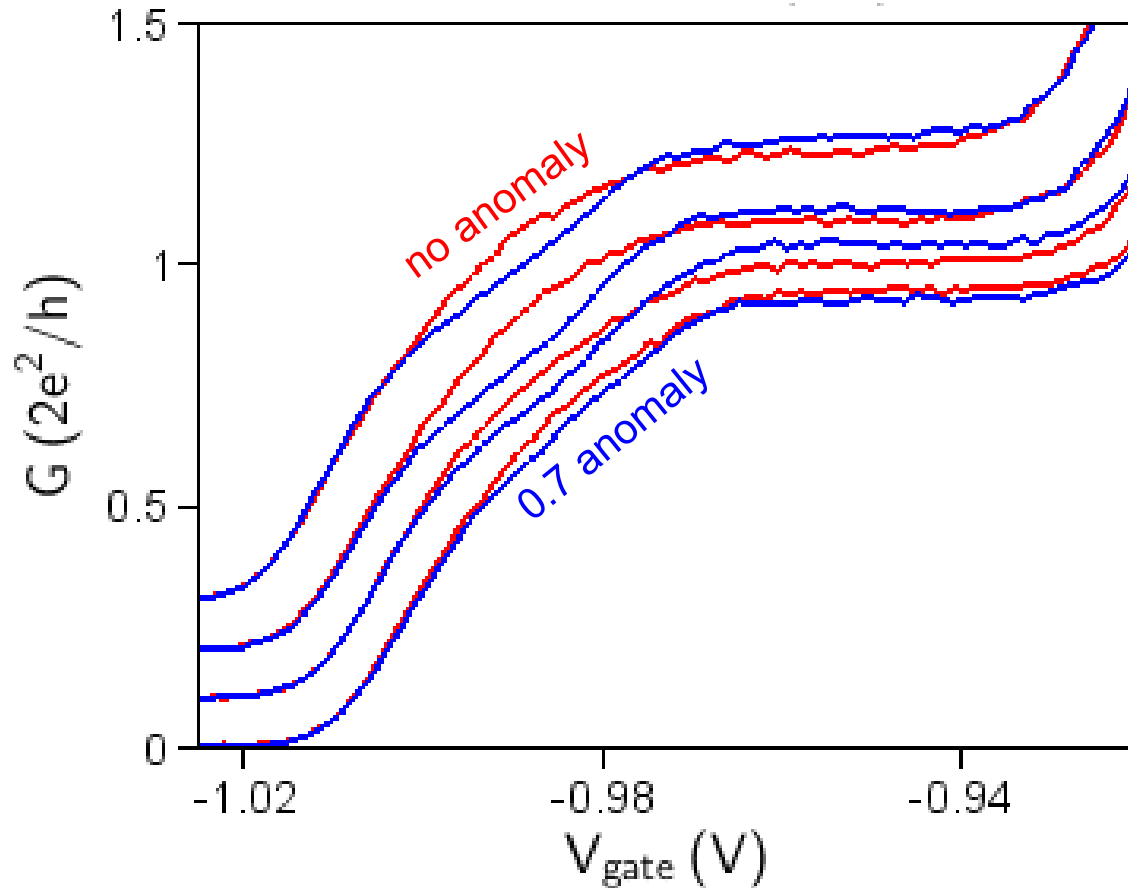
Gate voltage sweep
on single scan line



Conductance oscillations
correspond to a modulation
of the 0.7 anomaly



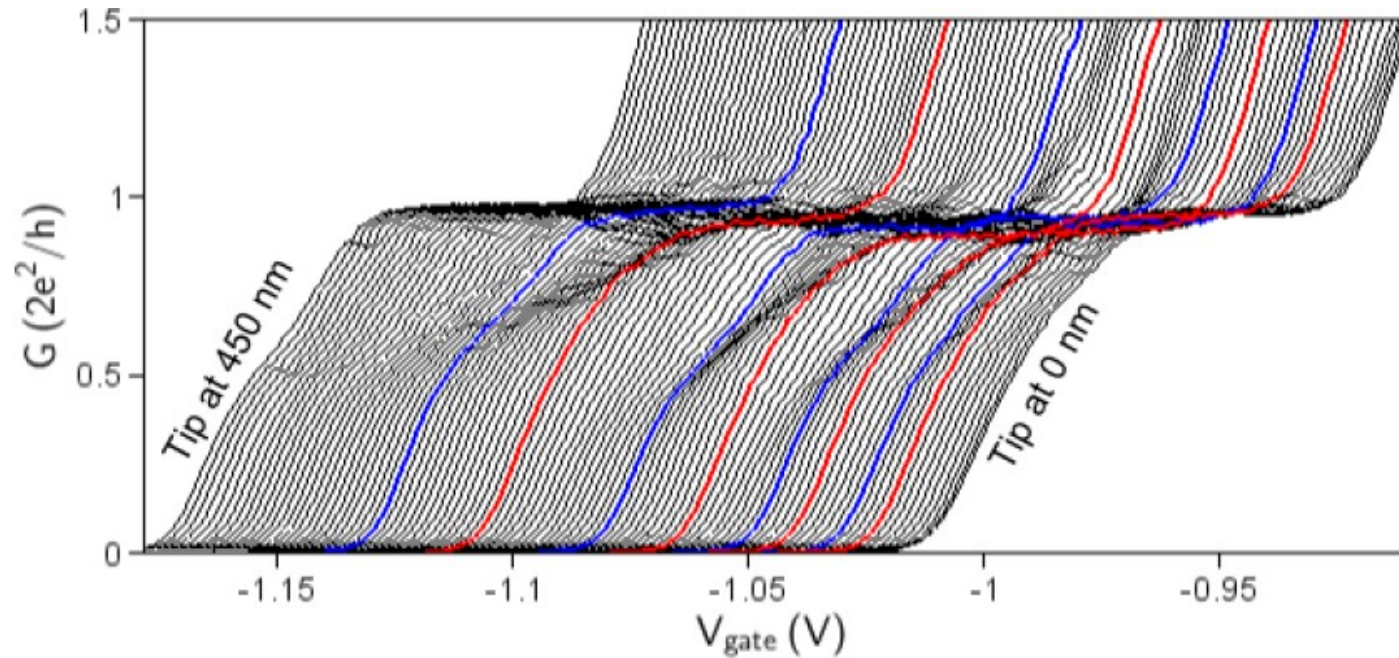
4 – Scanning gate experiment : the 0.7 anomaly



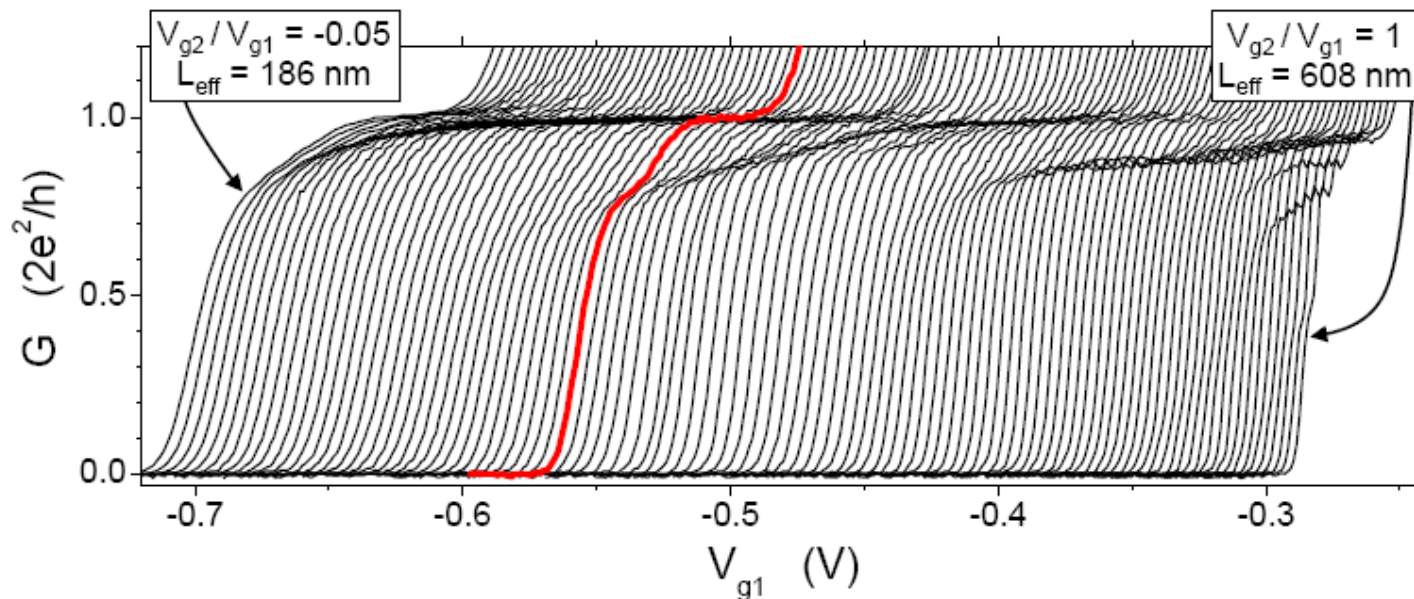
- conductance **maxima** correspond to **red curves** without anomaly
- conductance **minima** correspond to **blue curves** with 0.7 anomaly

=> The tip position controls the appearance of the 0.7 anomaly

4 – Scanning gate experiment : the 0.7 anomaly

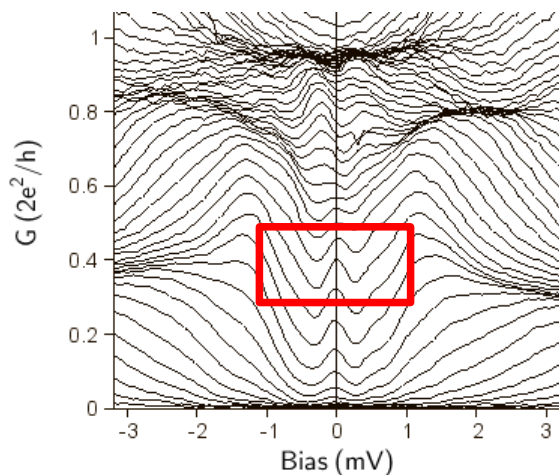


Scanning gate experiment

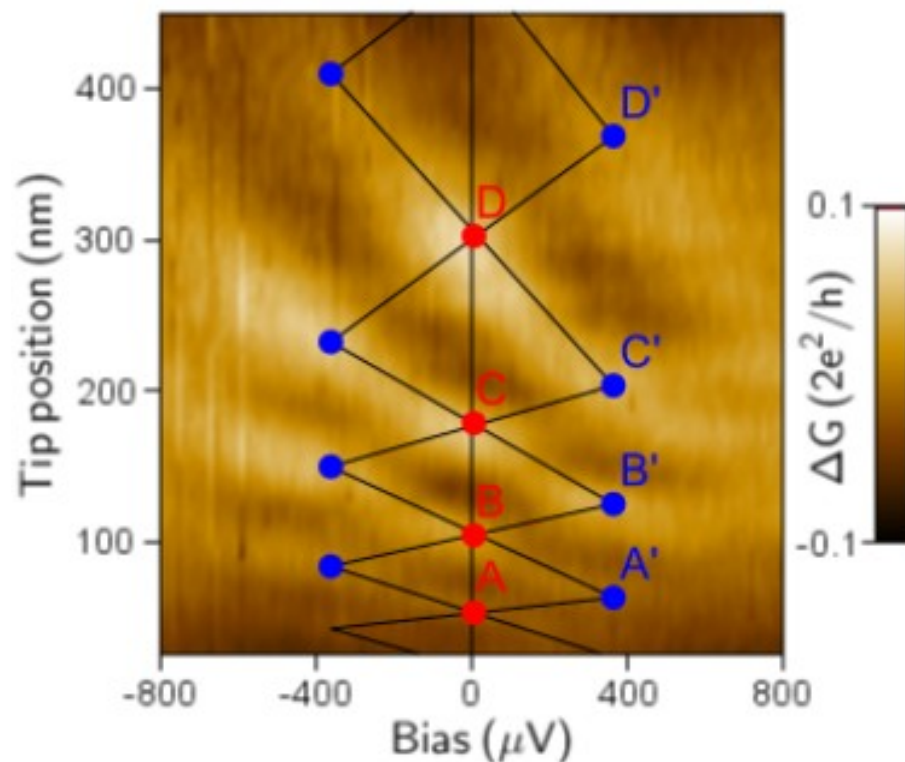
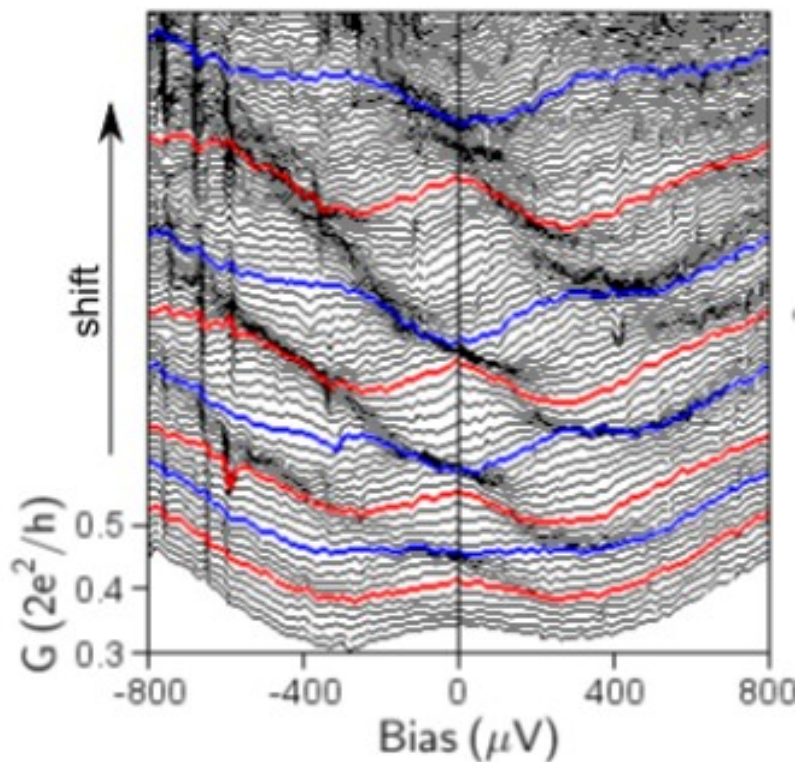
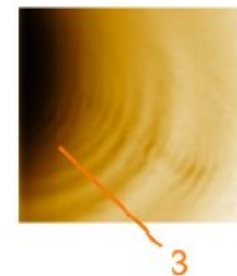


Tunable length experiment

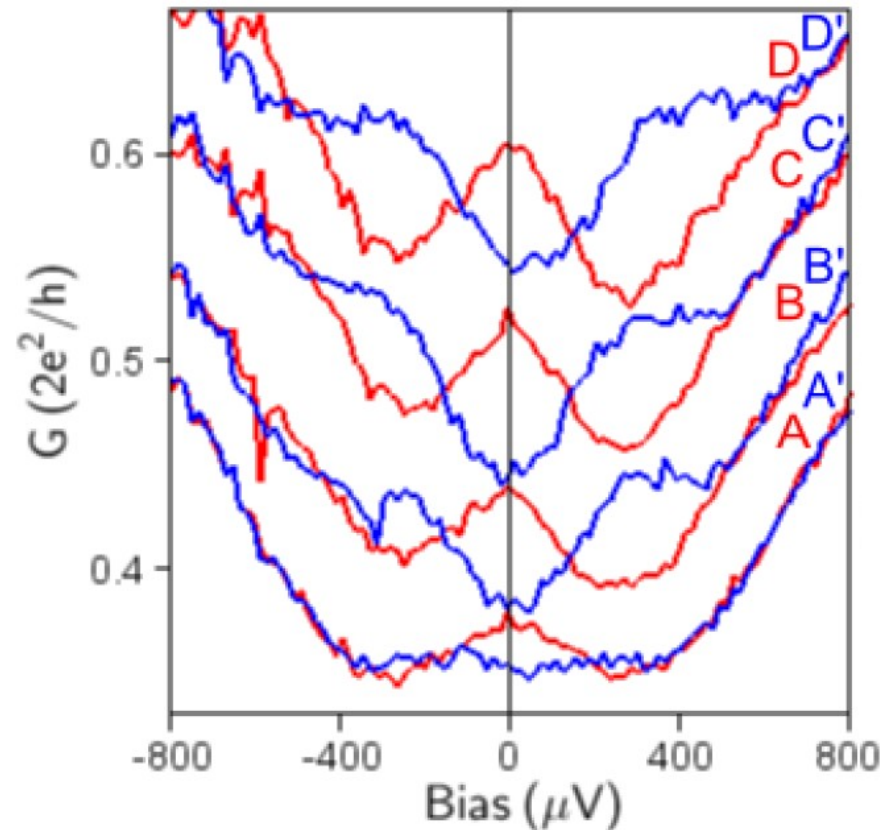
4 – Scanning gate experiment : the zero-bias anomaly



Source-drain bias sweep
at fixed gate voltage
on a single scan line



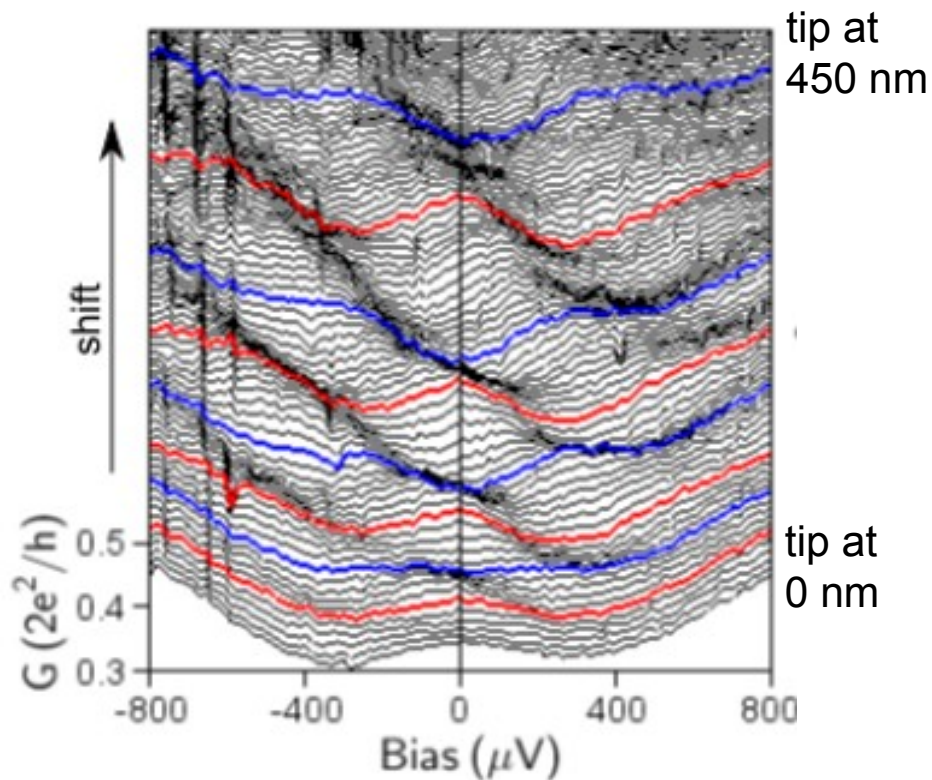
4 – Scanning gate experiment : the zero-bias anomaly



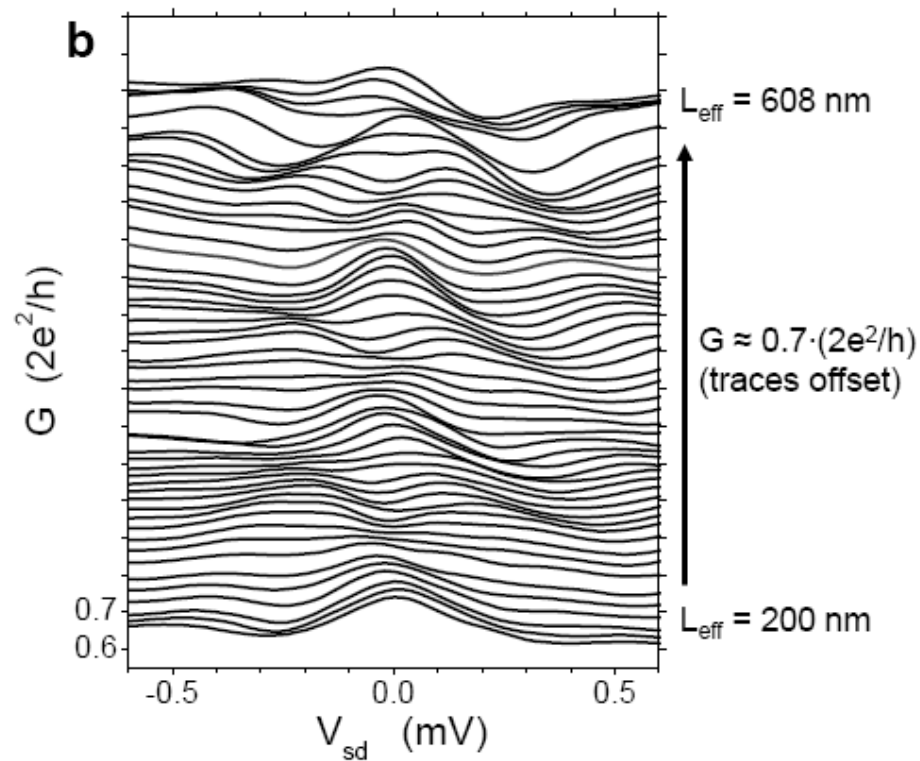
- conductance **maxima** correspond to **red curves** with a zero-bias peak
- conductance **minima** correspond to **blue curves** with finite-bias peaks

=> The tip position controls the appearance of the zero-bias anomaly

4 – Scanning gate experiment : the zero-bias anomaly

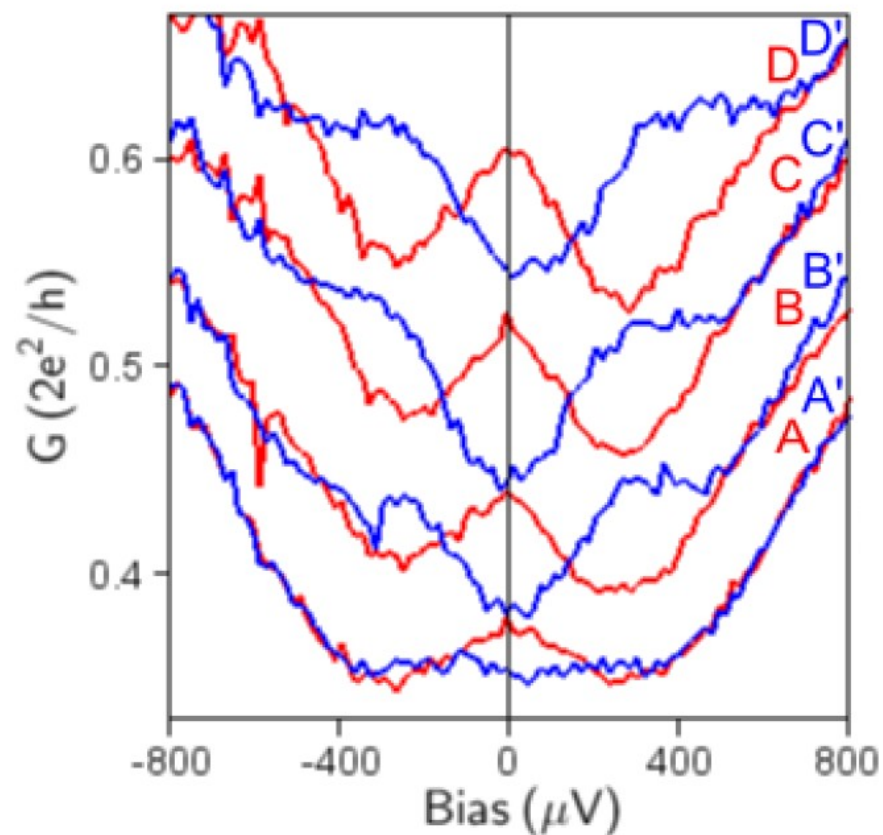
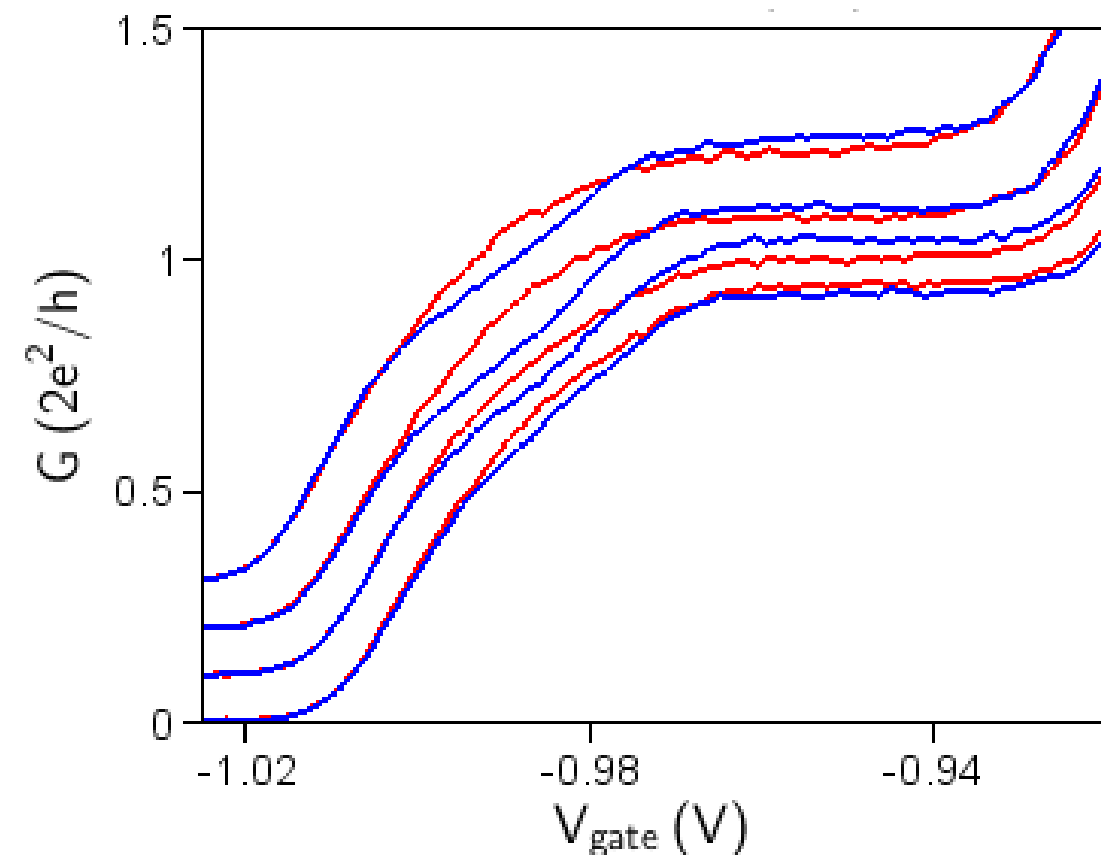


Scanning gate experiment



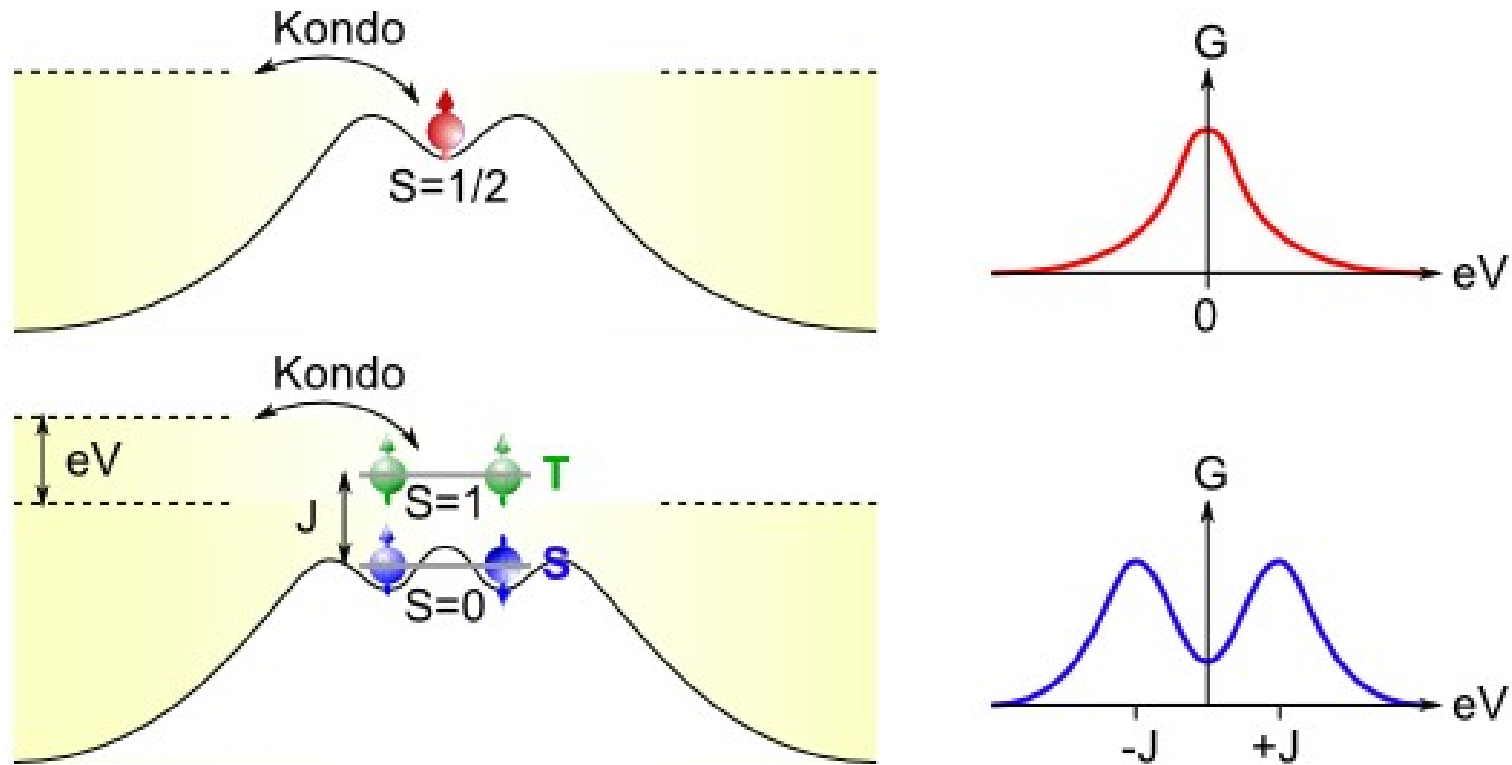
Tunable length experiment

4 – Scanning gate experiment : tunes both anomalies



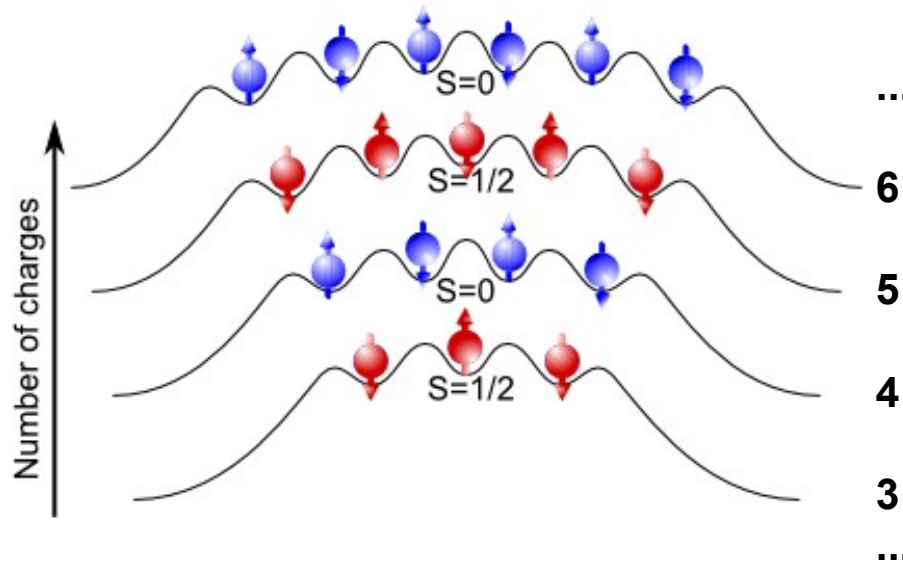
Conclusion : the **0.7 anomaly** corresponds to a **splitting** of the **zero-bias anomaly**

4 – Scanning gate experiment : interpretation



- The zero-bias anomaly is usually attributed to Kondo screening of a single **localized state**. A splitting of the zero bias peak can be explained by a two-impurity Kondo model:
- the **ground state** is a singlet that does not show Kondo effect
 - but the **excited state** is a triplet that shows out-of-equilibrium Kondo effect

4 – Scanning gate experiment : interpretation



Since :

4 successive zero-bias splittings correspond to 8 localized charges, we need a varying channel length.

But :

- in tunable length experiment, $L_{\text{effective}}$ varies from 200 to 600 nm
- in scanning gate experiment, $L_{\text{effective}}$ is constant at 250 nm

So :

Explanation is not as straightforward as for tunable length QPC. We need another explanation for increasing localized charges...

4 – Scanning gate experiment : interpretation

1D Wigner crystal predicted when $E_{\text{kinetic}} < E_{\text{Coulomb}}$

$$\text{i.e. } r_s = (2 n_{1D} a_B)^{-1} > 1$$

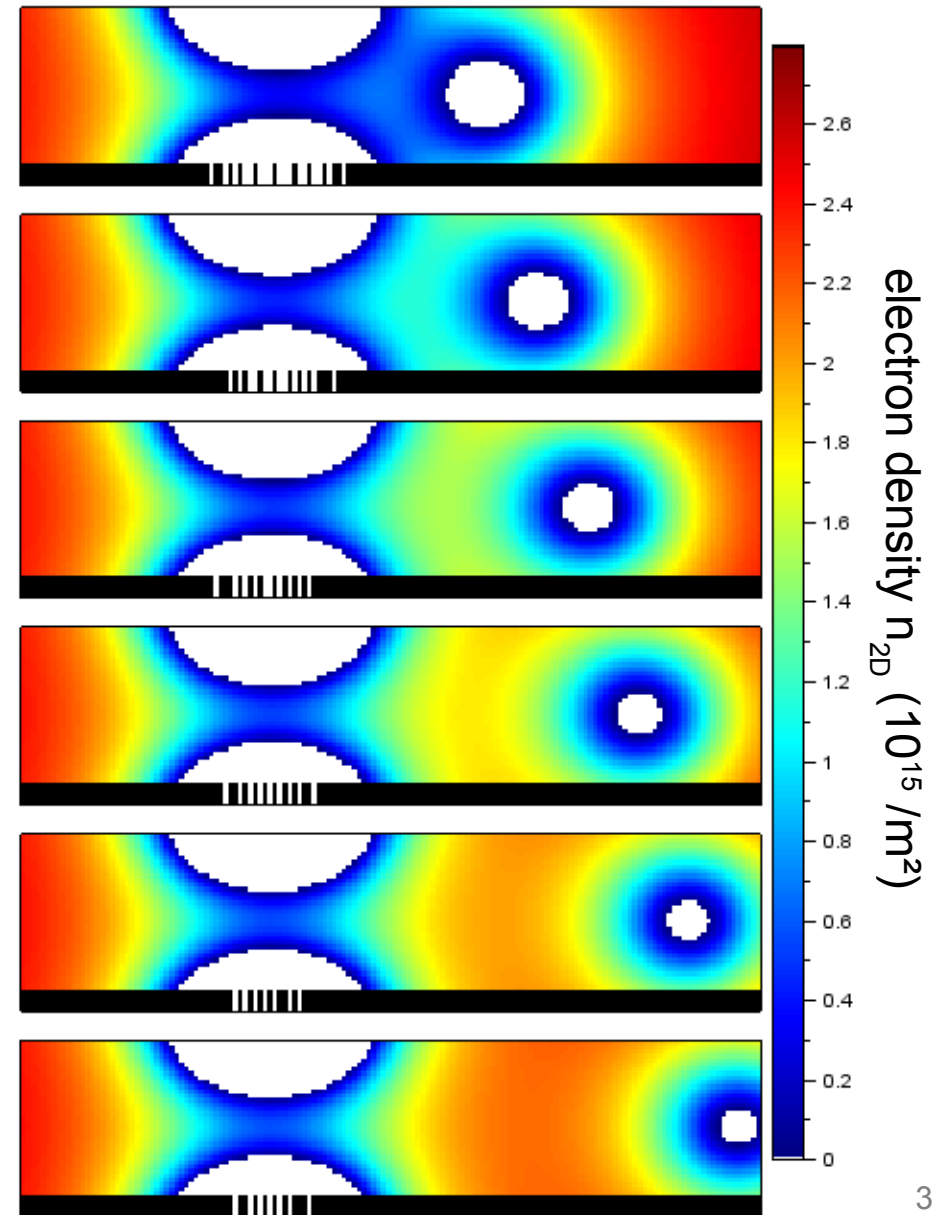
where :

n_{1D} is the 1D electron density

a_B is the effective Bohr radius (10 nm for GaAs)

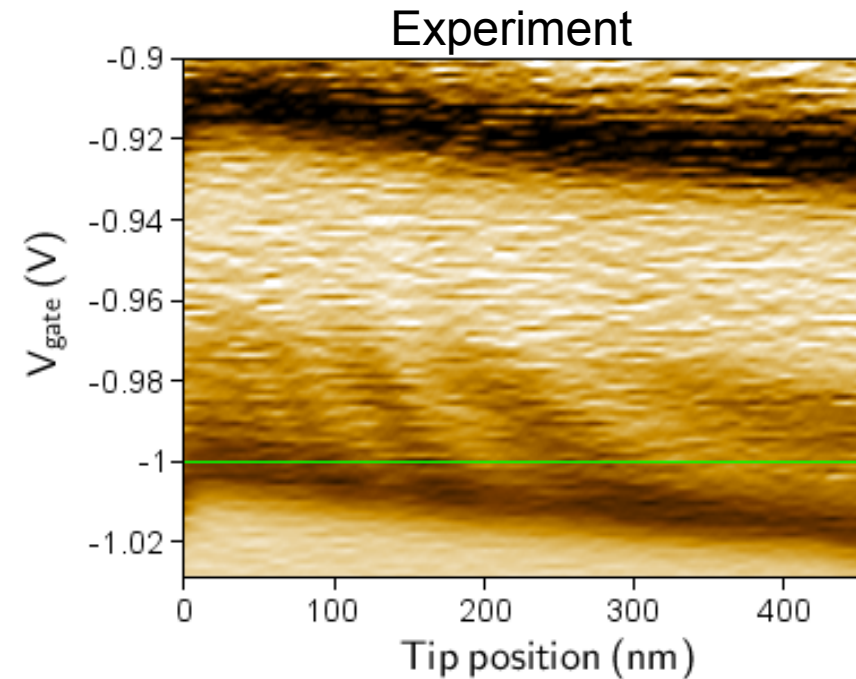
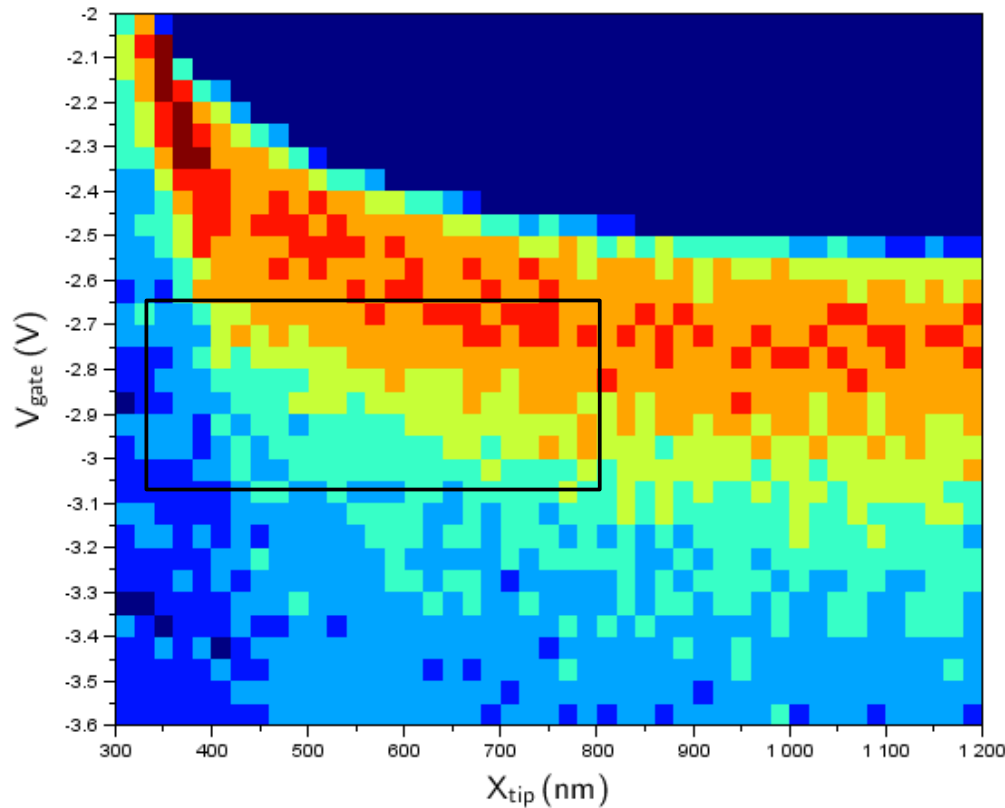
Simulation :

- gate and tip potentials
- local 2D electron density
- transverse integration
- local 1D electron density
- count electrons separated by more than $2 a_B$



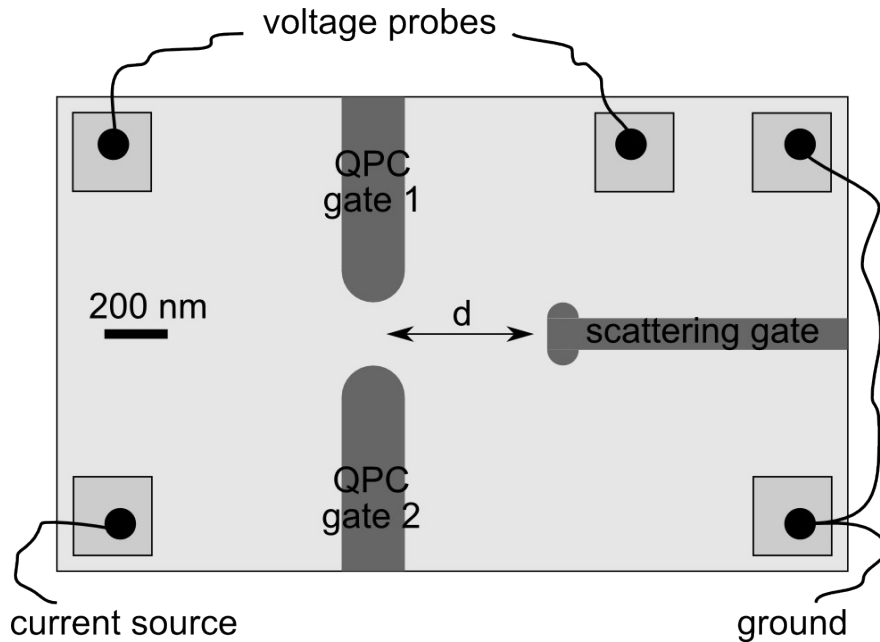
4 – Scanning gate experiment : interpretation

Number of electrons separated
by more than $2 a_B = 20 \text{ nm}$
(i.e. crystallized if $r_s^{\text{critical}} = 1$)



The number of crystallized electrons can be changed by a few units when scanning the tip or sweeping the gate voltage.

4 – Interferometers : principle

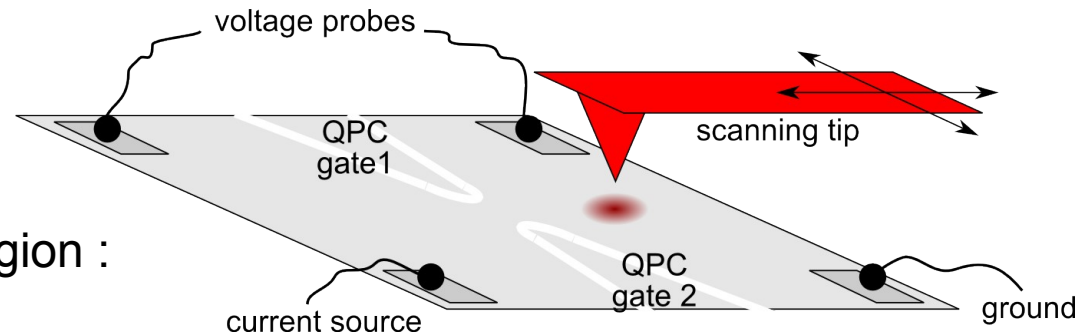


Interferometer = cavity between two barriers :
QPC at $\frac{1}{2}$ transmission + local potential barrier
(depleted region below the “scattering gate”)

Part of the electron flow is back-scattered
towards the QPC and then partially reflected
again to the right, such that interferences
build-up in the cavity.

The total transmission oscillates with the cavity
length d with period $\lambda_F/2$.

Alternatively, one can use a scanning gate
to have more flexibility on the scattering region :



4 – Interferometers : motivation

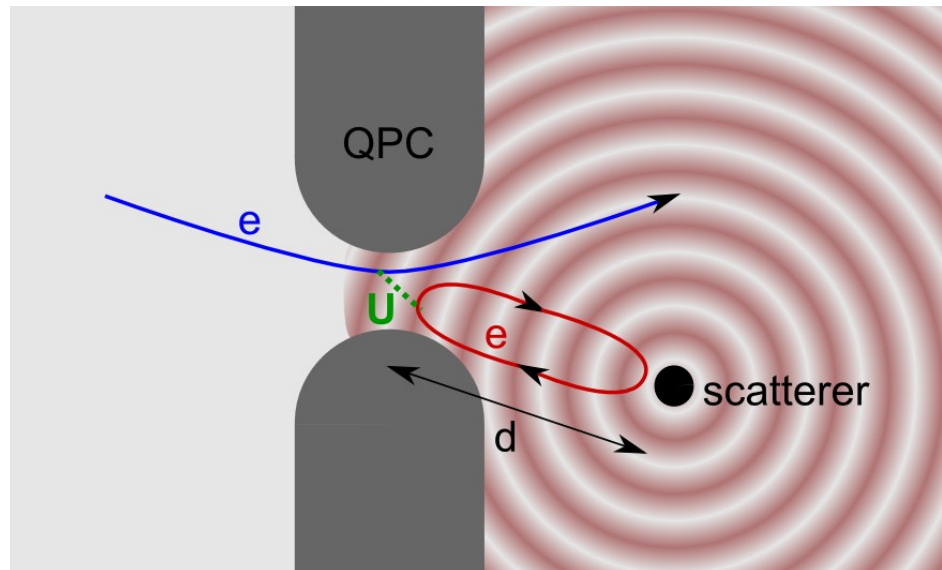
How to use interferometers to probe electron interactions in the QPC ?

Proposal by J.L. Pichard, D. Weinmann, R. Jalabert

Frey *et al.*, Phys. Rev. Lett. **100**, 226802 (2008)

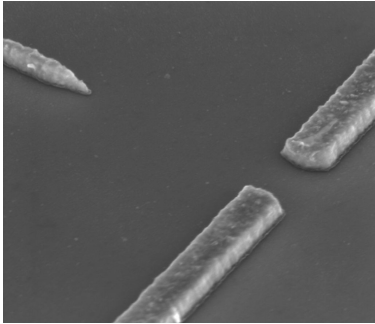
Weinmann *et al.*, Eur. Phys. J. B **66**, 239 (2008)

In addition to single-particle interferences, Friedel oscillations modulates the density in the QPC, and thus modulates electron transmission by Coulomb interactions.
Both effects have the same periodicity, but different spatial dependence.

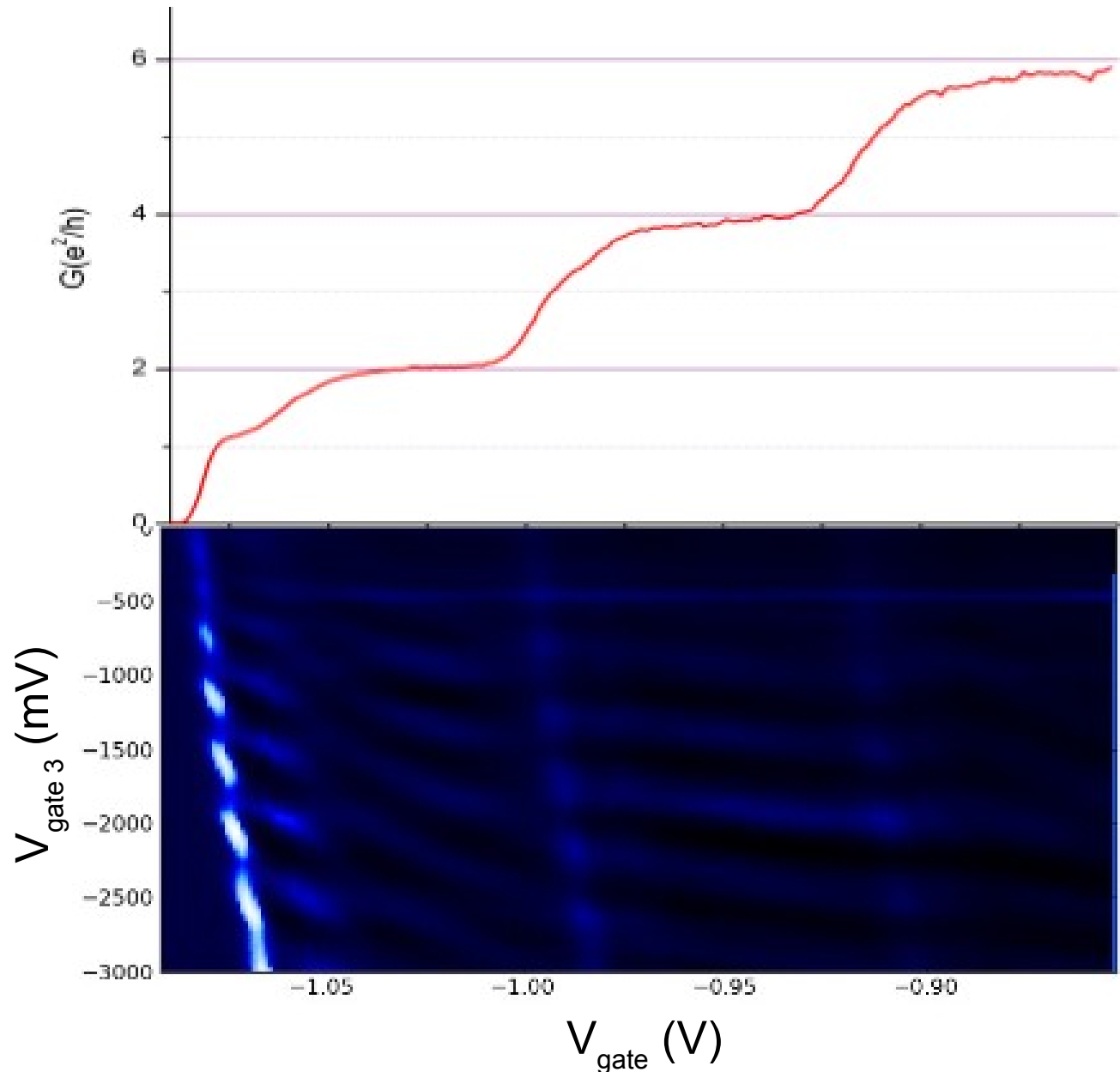


4 – Interferometers : results

1) Surface gate :

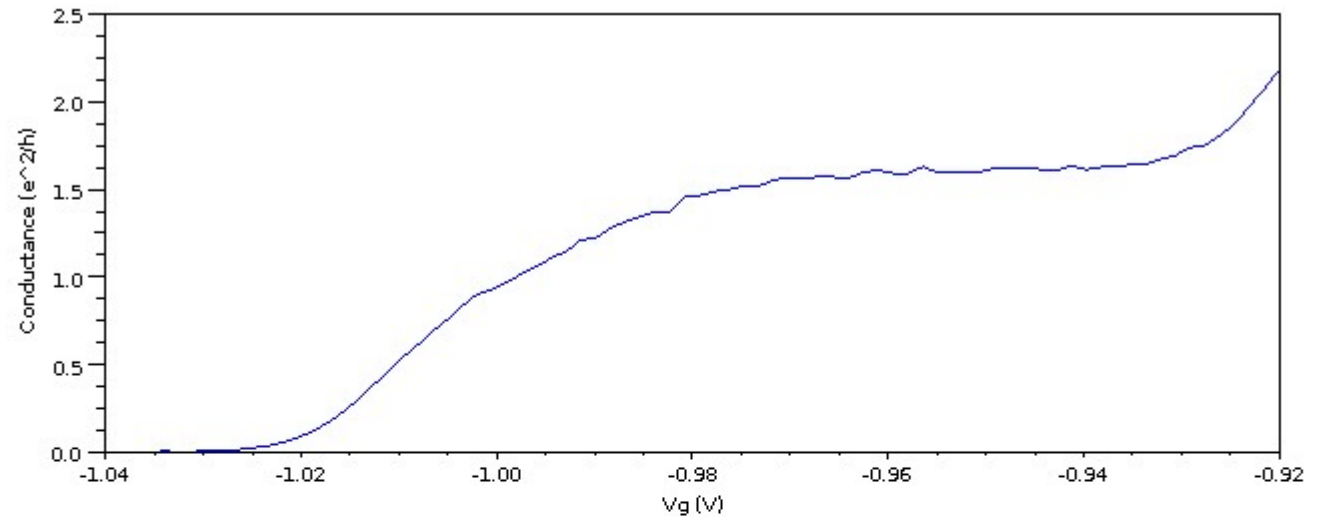
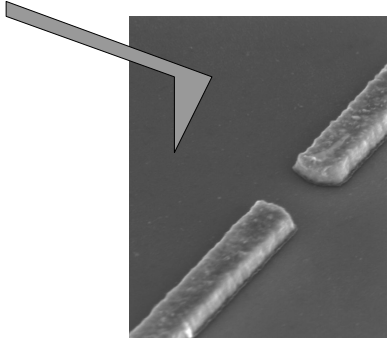


signal = $dG/dV_{\text{gate}3}$
(trans-conductance)

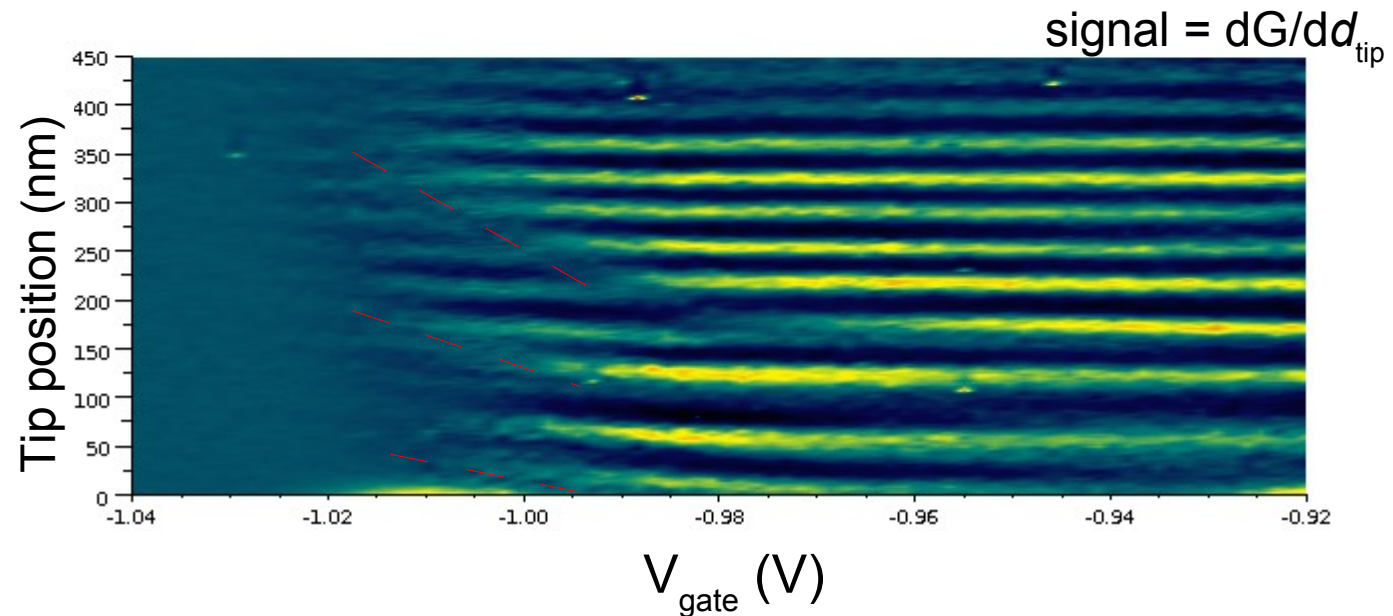


4 – Interferometers : results

2) Scanning gate :



Fringes below the plateau have a strange behavior : work still in progress...

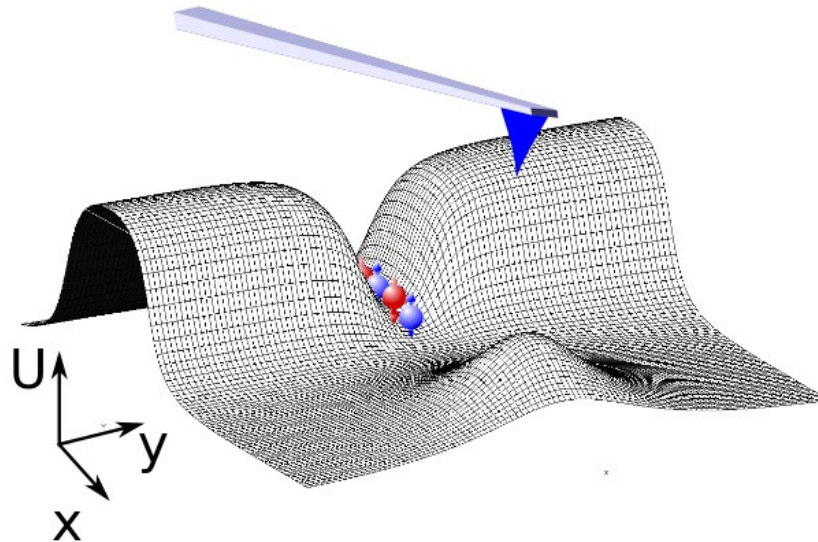


Conclusion

Scanning Gate Microscopy is a versatile tool to probe electrons in 2DEG nanostructures.

Although one of the most basic device, the quantum point contact is a very nice platform to study many-body physics.

The 0.7 and zero-bias anomalies may result from an interplay between Wigner crystallization and Kondo screening.



Preprint available on arXiv:1307.8328

Thank you for your attention !

