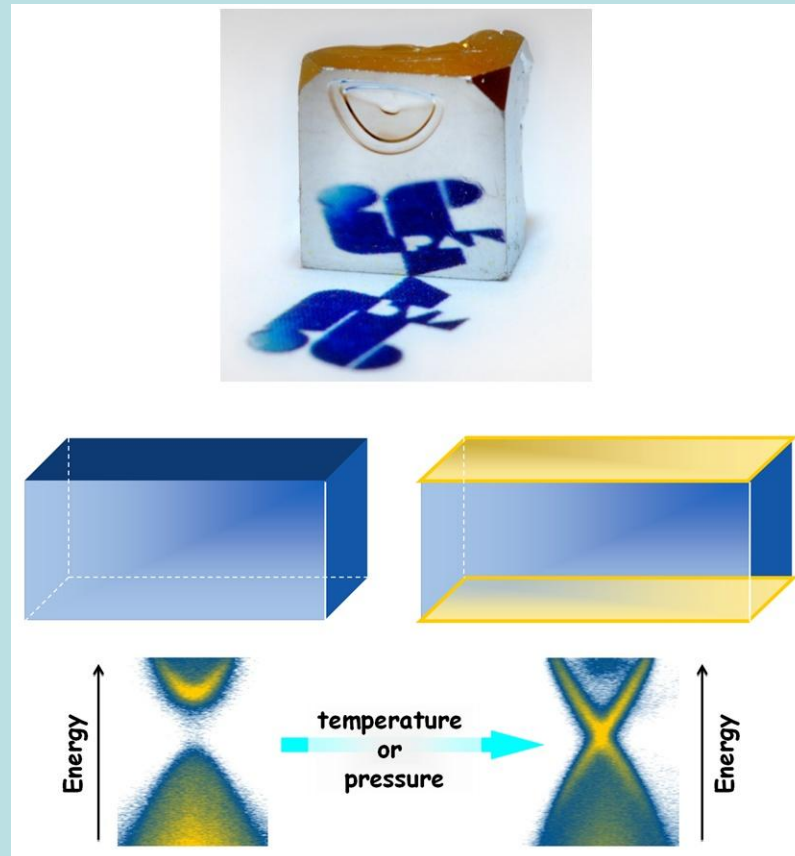




# Topological crystalline insulators

Tomasz Story

Institute of Physics, Polish Academy of Sciences, Warsaw



# Topological crystalline insulators - outline

1. Introduction – topological crystalline insulators (TCI) vs topological insulators (TI)
2. IV-VI semiconductors as topological insulators
3.  $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$  monocrystals – growth , structural, chemical and electric characterization
4. Angle- and spin-resolved photoemission experiments
5. Electronic band structure calculations
6. Magneto-transport studies
7. Summary and future outlook

# **Pb<sub>1-x</sub>Sn<sub>x</sub>Se as topological crystalline insulator**

**Crystal growth: A. Szczerbakow (IP PAS)**

**Structural and chemical characterization:**

**W. Domuchowski, E. Łusakowska, A. Reszka (IP PAS)**

**Magneto-transport studies – K. Dybko, M. Szot (IP PAS)**

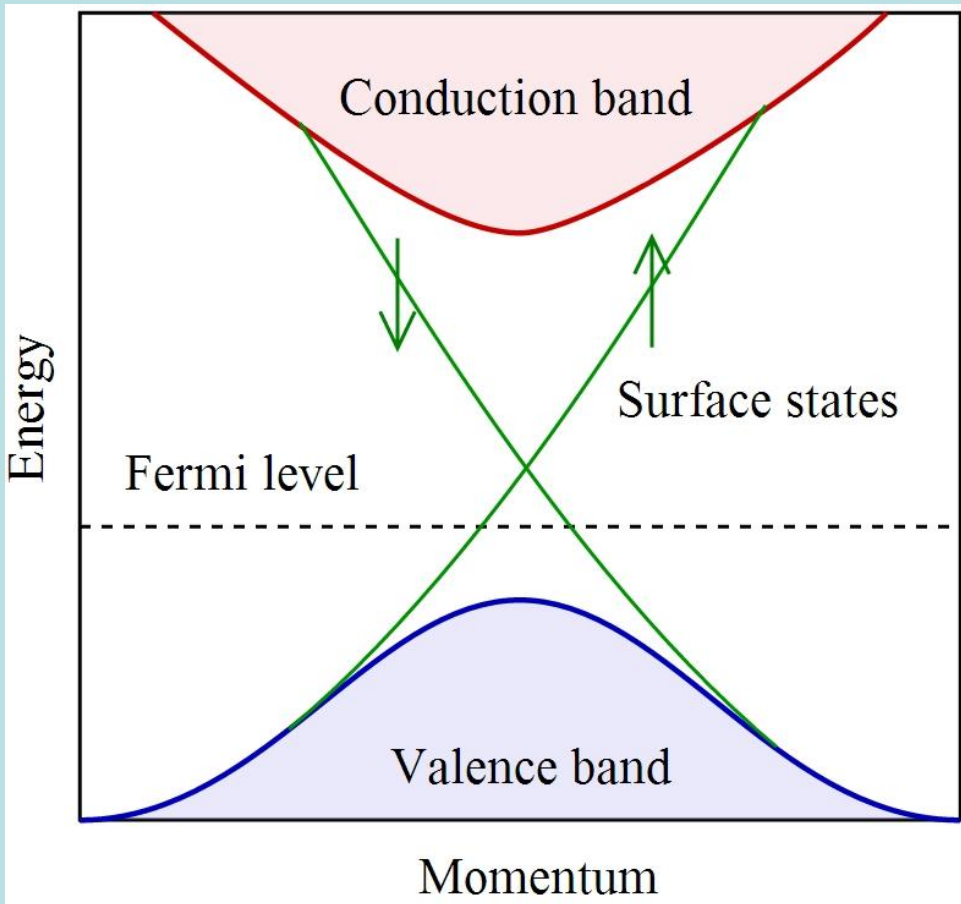
**Band structure calculations – R. Buczko (IP PAS)**

**Photoemission measurements at Lund University (synchrotron facility) and KTH Stockholm (laser facility):**

**P. Dziawa, B.J. Kowalski (IP PAS), T. Balasubramanian (Lund),  
M.H. Berntsen, O. Tjernberg, B.M. Wojek (KTH)**

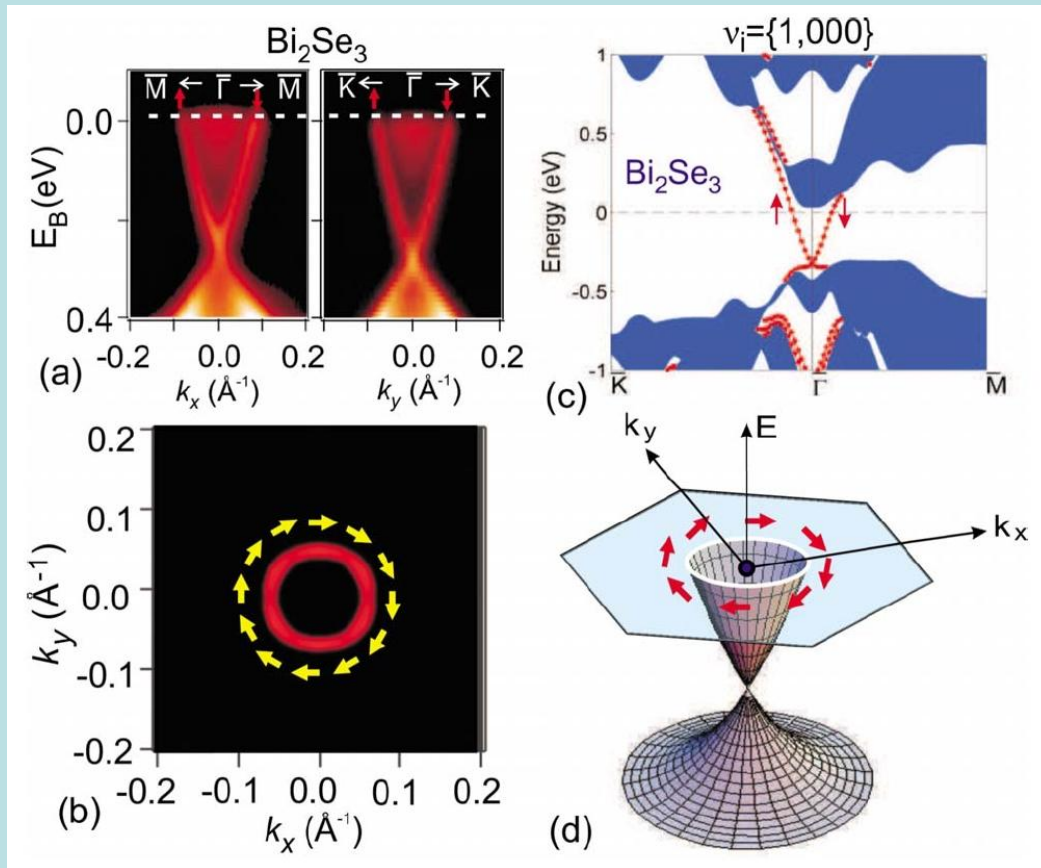
**TS**

# Topological insulators: key physical factors



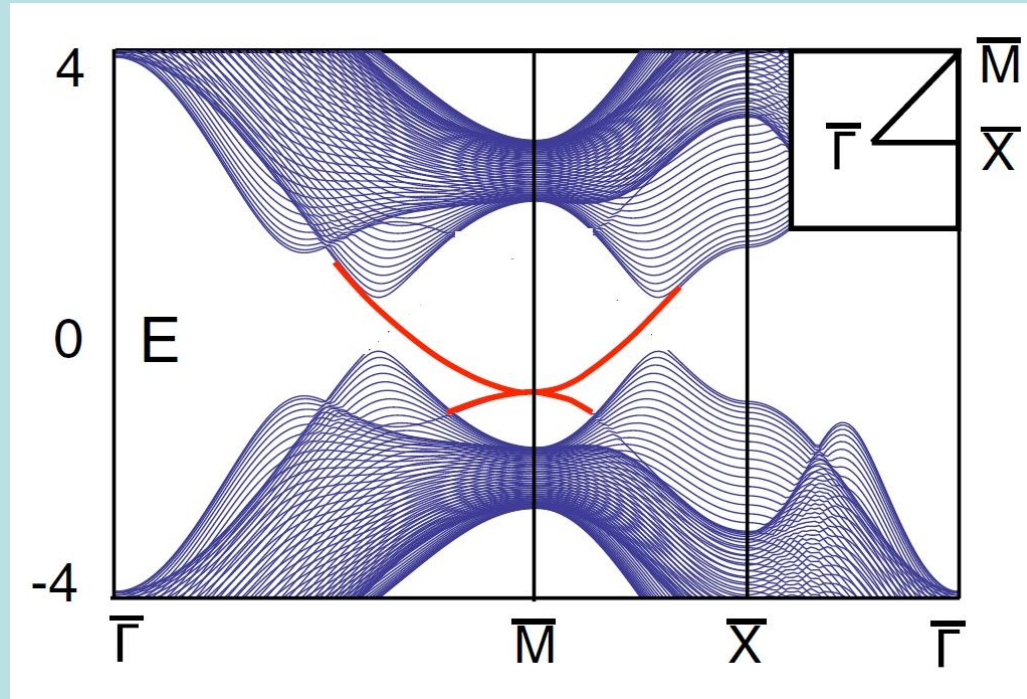
- **Inverted c-band and v-band symmetry**
- **Odd number of Dirac cones**
- **Strong spin-orbit coupling  $E_{so} \approx E_G$**
- **Metallic, helical Dirac electronic surface states**
- **Topological protection**

# Topological insulators - materials



- **3D**
- $\text{Bi}_{1-x}\text{Sb}_x$
- $\text{Bi}_2\text{Se}_3$
- $\text{Bi}_2\text{Te}_3$
  
- **2D**
- $\text{HgTe/CdTe}$  QW

# Topological crystalline insulators: theoretical idea

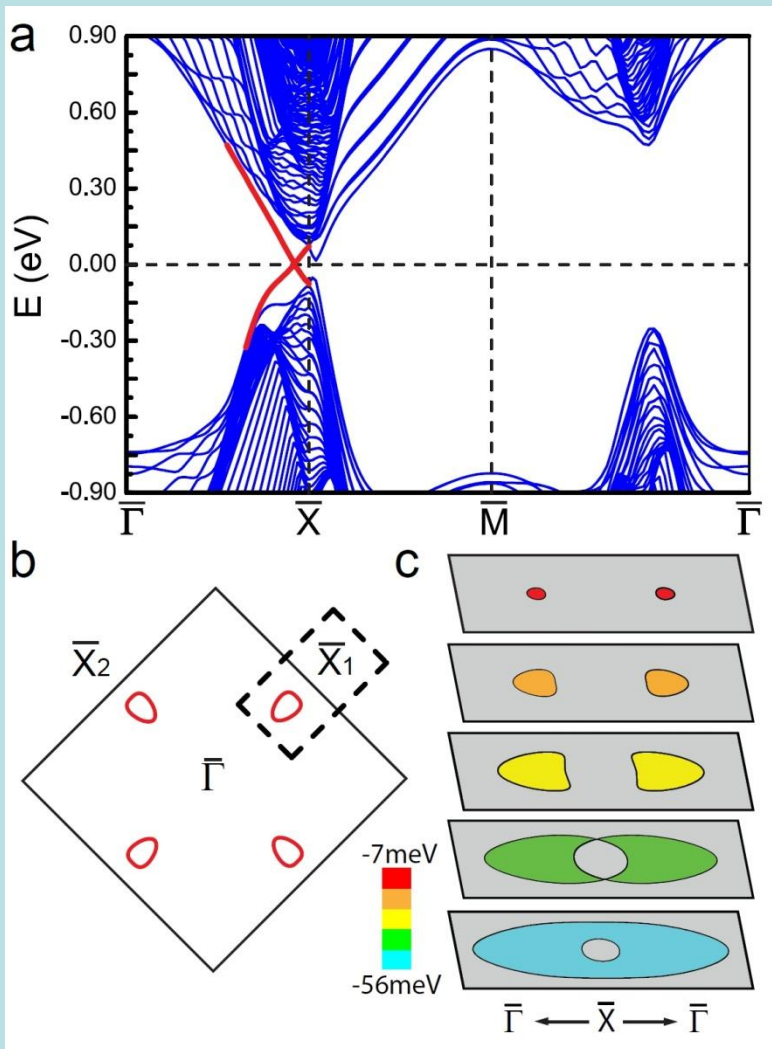


Theoretical analysis of electronic band structure of tetragonal crystal with 4-fold surface symmetry. Topologically protected surface TCI states (red) are expected even in materials with no spin-orbit coupling.

L. Fu, Phys. Rev. Lett. 106, 106802 (2011).

# Topological crystalline insulators

## SnTe - theoretical analysis

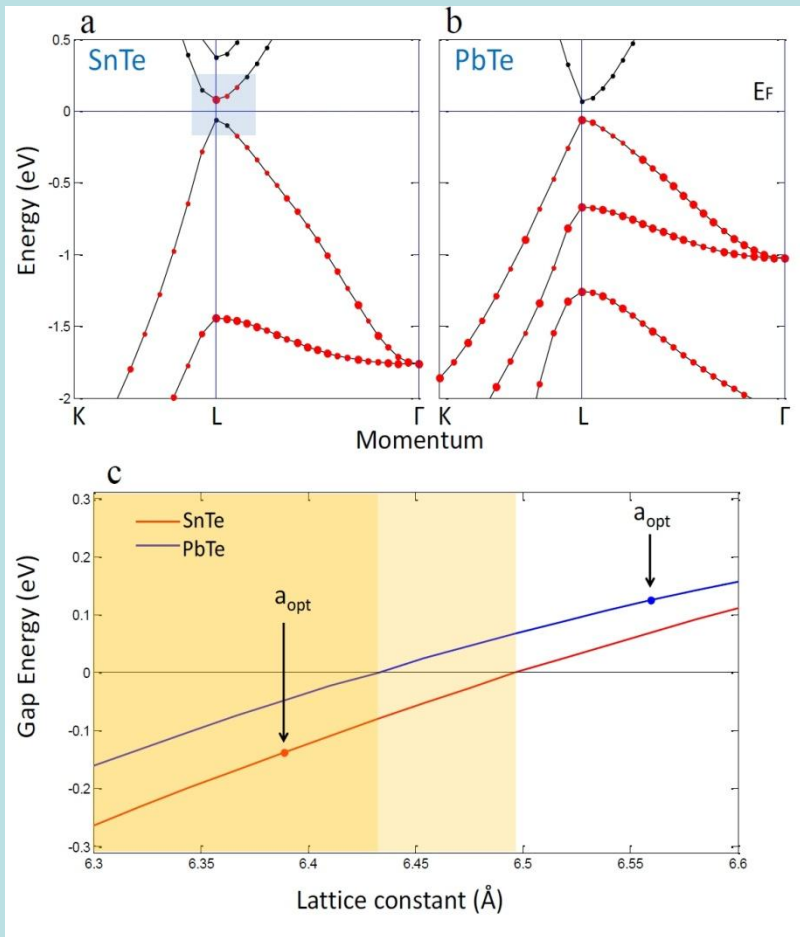


SnTe - TCI states with 4 Dirac cones nearby X-points of the surface Brillouin zone

Lifshitz transition -  
Topological changes of Fermi surface

T.H. Hsieh et al, Nature Commun. **3**, 982 (2012).

# Topological crystalline insulators: SnTe vs PbTe – theoretical analysis



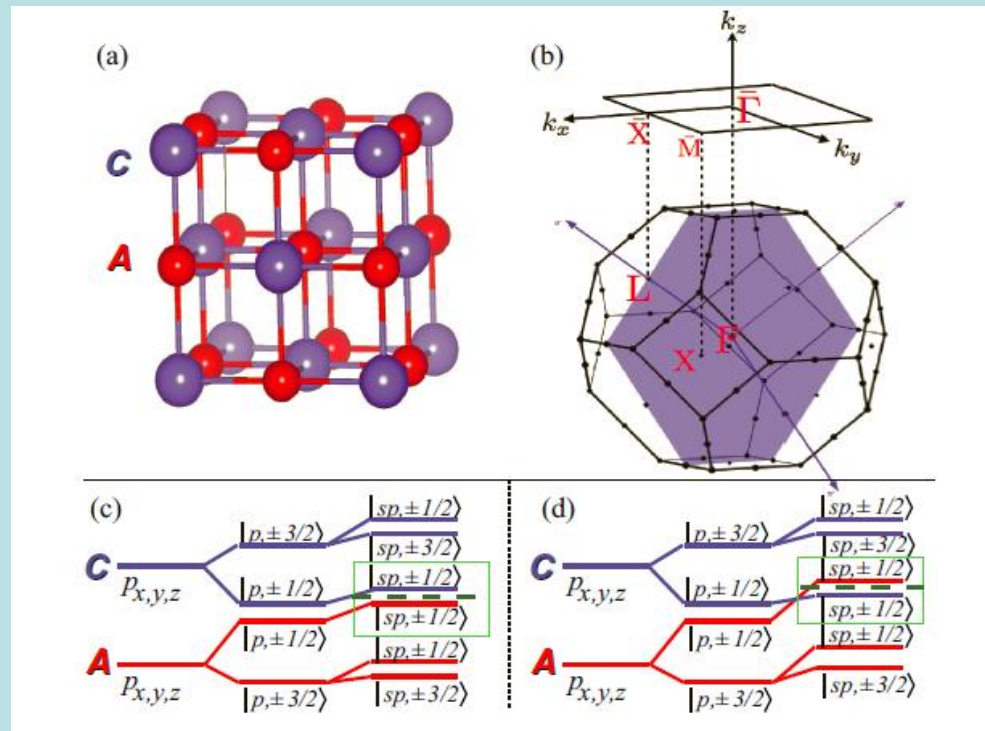
PbTe – trivial band insulator  
 $E_G > 0$

SnTe – topological insulator (TCI)  
 $E_G < 0$

T.H. Hsieh et al,  
Nature Commun. 3, 982 (2012).



# Band inversion in IV-VI semiconductors

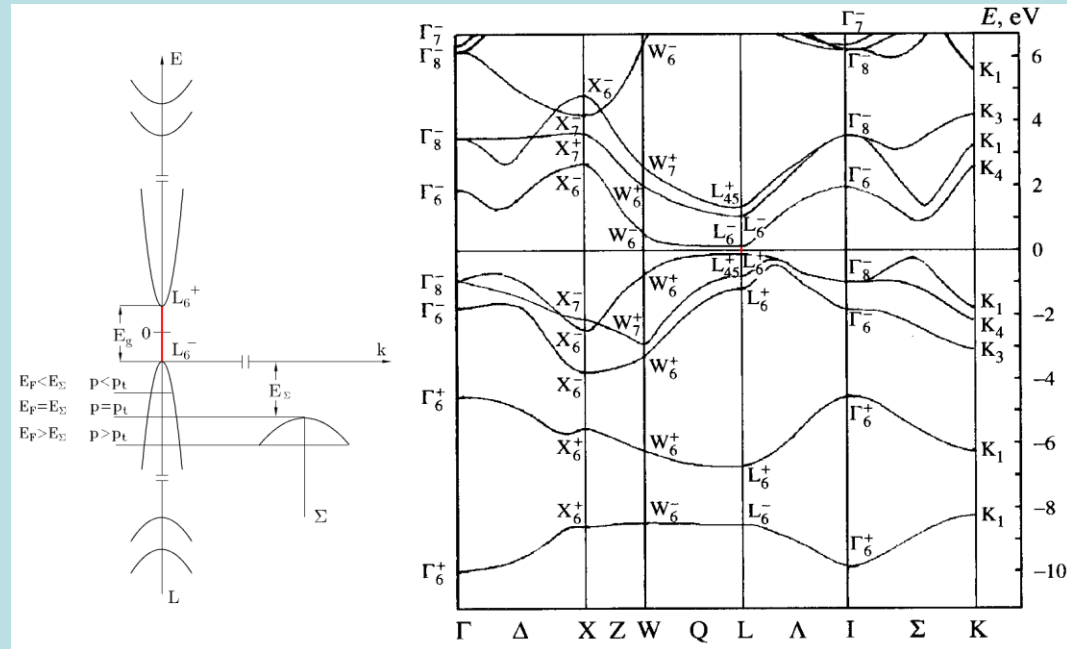
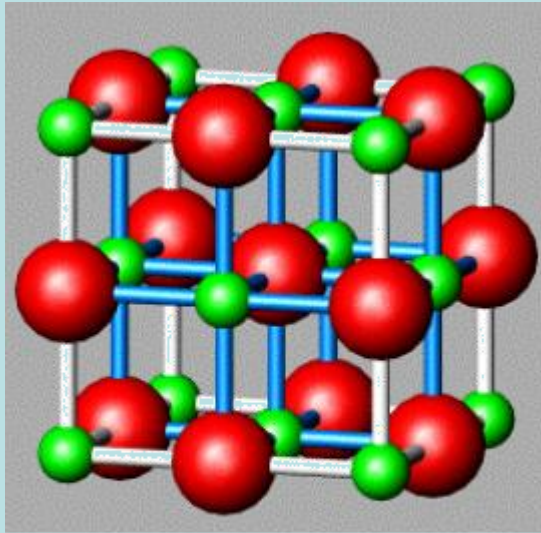


# IV-VI semiconductor family

						2 <b>He</b> Helium 4.003
	5 <b>B</b> Boron 10.811	6 <b>C</b> Carbon 12.0107	7 <b>N</b> Nitrogen 14.00674	8 <b>O</b> Oxygen 15.9994	9 <b>F</b> Fluorine 18.9984032	10 <b>Ne</b> Neon 20.1797
	13 <b>Al</b> Aluminum 26.981538	14 <b>Si</b> Silicon 28.0855	15 <b>P</b> Phosphorus 30.973761	16 <b>S</b> Sulfur 32.066	17 <b>Cl</b> Chlorine 35.4527	18 <b>Ar</b> Argon 39.948
30 <b>Zn</b> Zinc 65.39	31 <b>Ga</b> Gallium 69.723	32 <b>Ge</b> Germanium 72.61	33 <b>As</b> Arsenic 74.92160	34 <b>Se</b> Selenium 78.96	35 <b>Br</b> Bromine 79.904	36 <b>Kr</b> Krypton 83.80
48 <b>Cd</b> Cadmium 112.411	49 <b>In</b> Indium 114.818	50 <b>Sn</b> Tin 118.710	51 <b>Sb</b> Antimony 121.760	52 <b>Te</b> Tellurium 127.60	53 <b>I</b> Iodine 126.90447	54 <b>Xe</b> Xenon 131.29
80 <b>Hg</b> Mercury 200.59	81 <b>Tl</b> Thallium 204.3833	82 <b>Pb</b> Lead 207.2	83 <b>Bi</b> Bismuth 208.98038	84 <b>Po</b> Polonium (209)	85 <b>At</b> Astatine (210)	86 <b>Rn</b> Radon (222)
112  (277)	113	114				

- **Binary compounds:**
- **PbTe, PbSe, PbS, SnTe, GeTe**
- **Substitutional solid solutions:**
- **$Pb_{1-x}Sn_xTe$ ,  $Pb_{1-x}Sn_xSe$**
- **Diluted magnetic semiconductors:**
- **$Sn_{1-x}Mn_xTe$ ,  $Ge_{1-x}Mn_xTe$**

# IV-VI semiconductors



Rock-salt crystal structure.

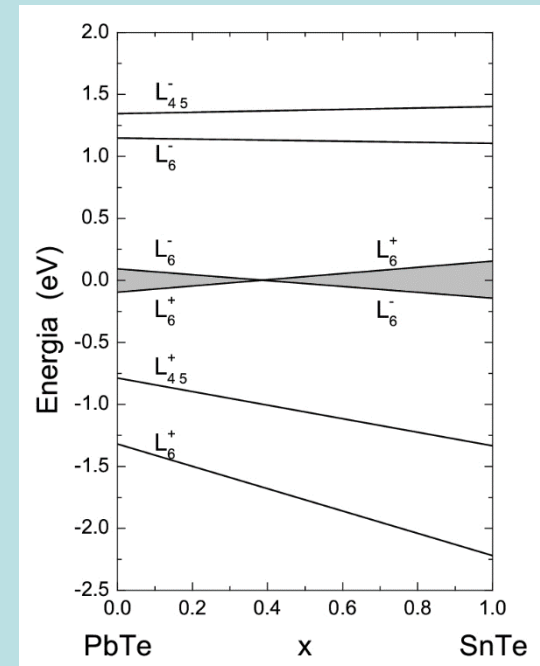
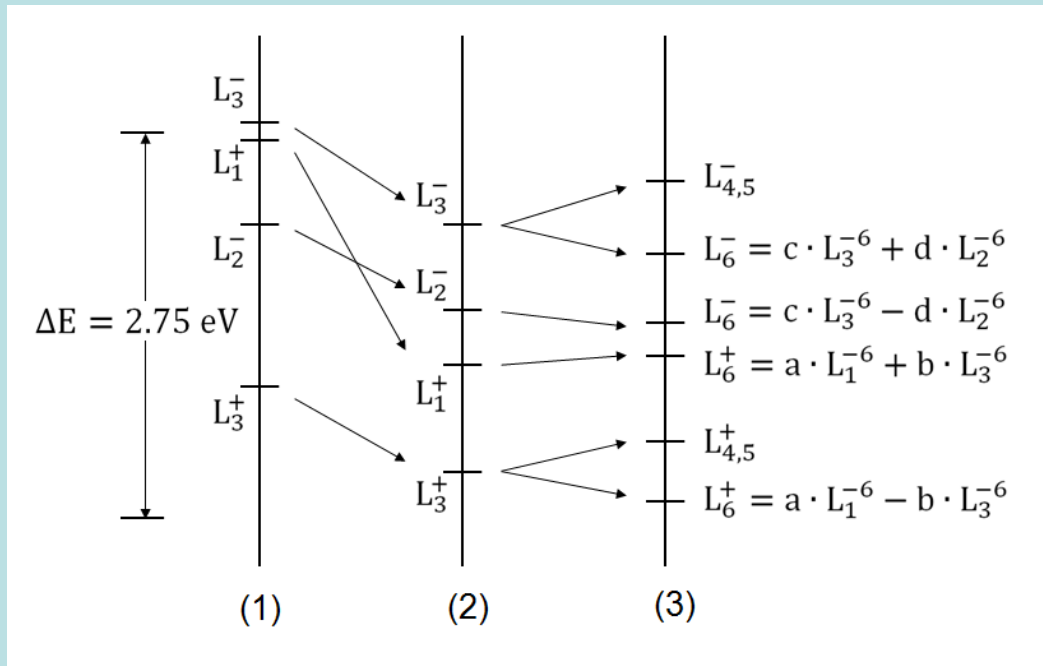
Narrow-gap materials (0-0.3 eV) with a direct gap at 4 equivalent L-points .

Strong (1 eV) relativistic interactions (spin-orbit and Darwin terms).

Small effective masses and high mobilities of electrons and holes.

Materials for thermoelectric generators and mid-infrared lasers and detectors.

# Electron band structure of IV-VI semiconductors

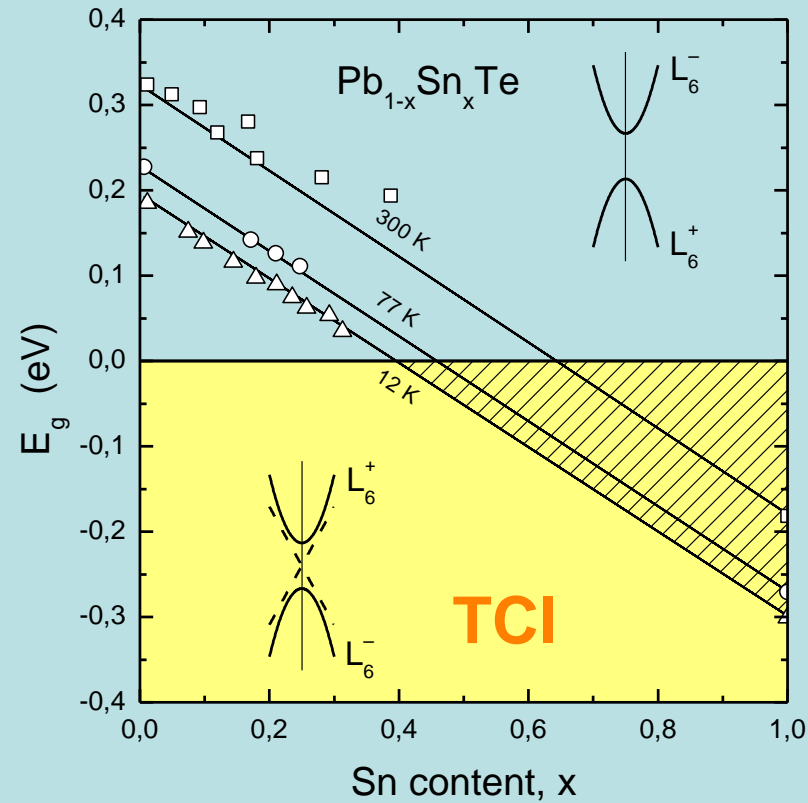


## Relativistic interactions in PbTe and $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$

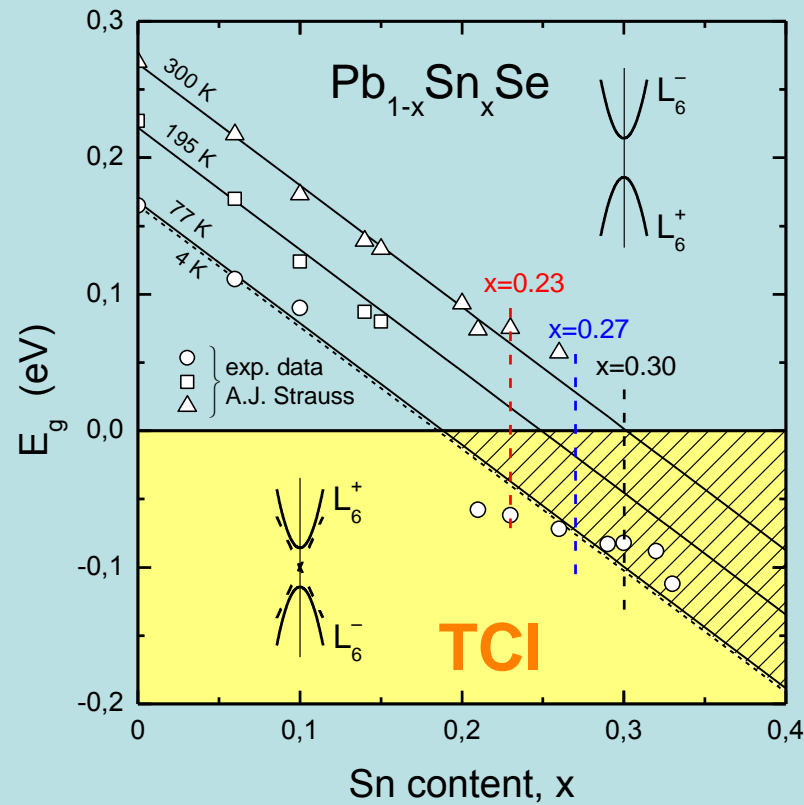
$$\hat{H} = \frac{\hat{p}^2}{2m_0} + U - \frac{\hat{p}^4}{8m_0^3c^2} + \frac{\hbar^2}{8m_0^3c^2} \nabla^2 U + \frac{\hbar}{4m_0^3c^2} \hat{\sigma}(\nabla U \times \hat{p})$$

# $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$ substitutional solid solutions

R. Dornhaus, G. Nimtz, and B. Schlicht,  
Springer Tracts in Modern Physics vol. 98, Narrow-Gap Semiconductors  
(Springer, Berlin, 1983)



# $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$ substitutional solid solutions

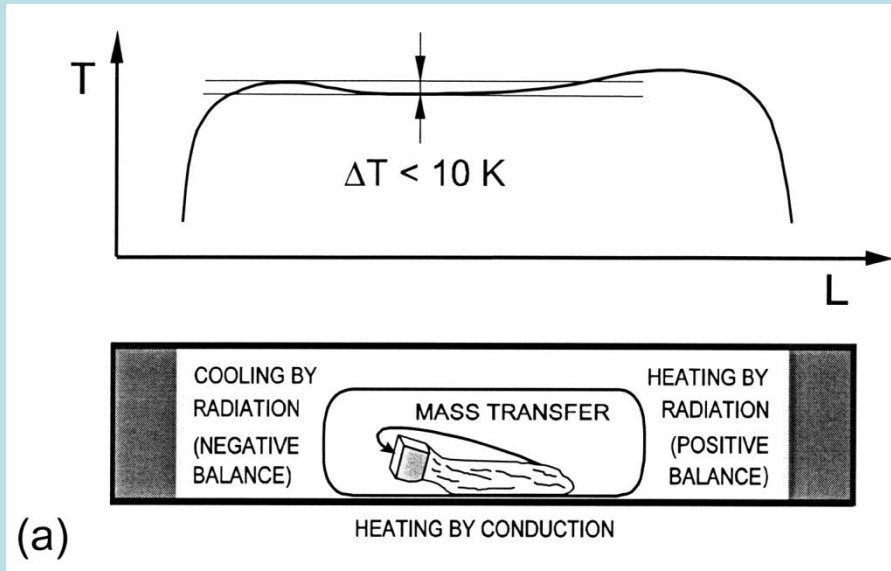


# Idea of our TCI project

- **Pb<sub>1-x</sub>Sn<sub>x</sub>Se monocrystals (0.18<x<0.3) to observe temperature-driven topological phase transition from trivial insulator to the TCI state**
- **n-type crystals required for  $x > x_c$  (TCI states occupied)**
- **cleaving at UHV conditions as a versatile method of preparing high crystal quality, atomically clean (001) surfaces**
- **no surface reconstruction expected**
- **only Pb<sub>1-x</sub>Sn<sub>x</sub>Se crystals fulfil all these conditions**
- **Pb<sub>1-x</sub>Sn<sub>x</sub>Te ( $x > x_c$ ) and SnTe crystals are heavily p-type doped by electrically active native defects (metal vacancies).**

# Growth of $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$ and $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$ bulk monocrystals

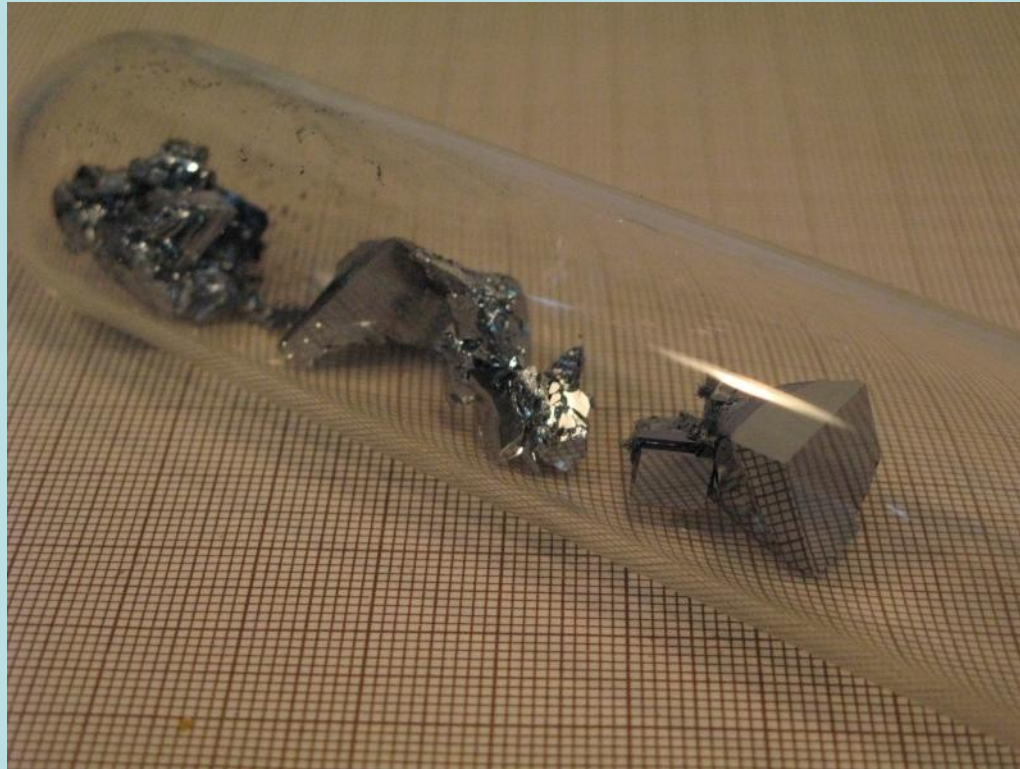
- Self-selecting vapor growth (SSVG) – A. Szczerbakow
- Natural (001) crystal facets – cleavage planes
- Stoichiometry control of n – and p-type conductivity
- Highly homogeneous chemical composition of solid solutions



A. Szczerbakow et al.:  
J. Cryst. Growth 139, 172 (1994);  
Prog. Cryst. Growth Charact. Mater. 51, 81 (2005).

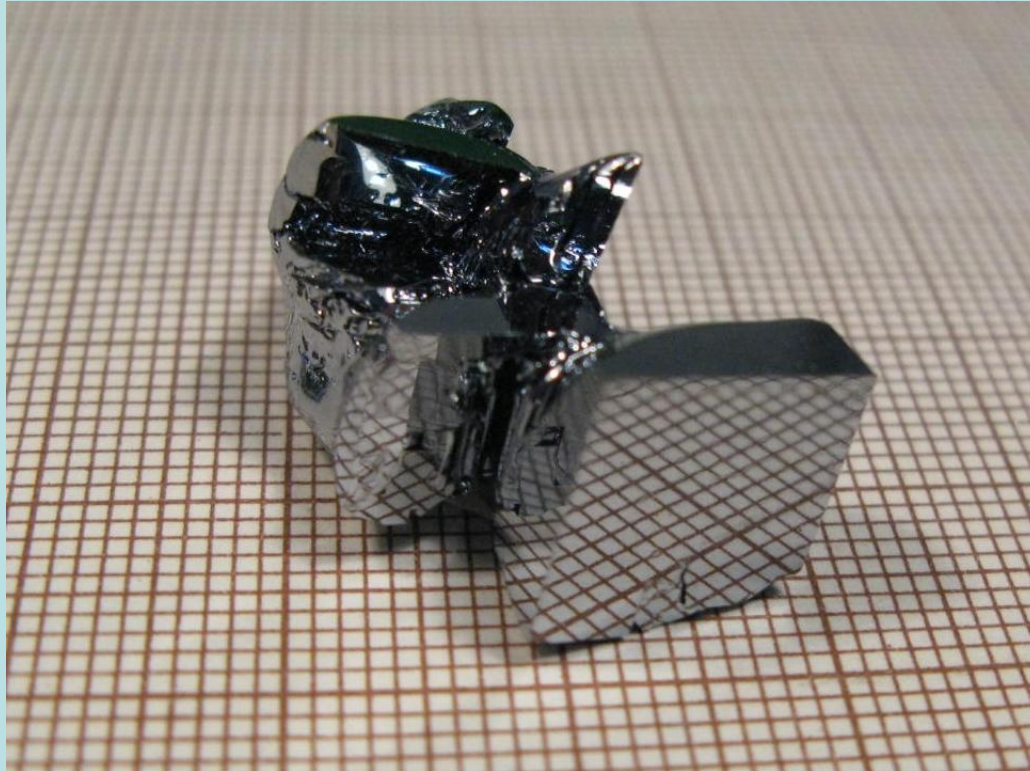


# Growth of bulk PbSnSe crystals by SSVG method



- A. Szczerbakow,  $\text{Pb}_{0.76}\text{Sn}_{0.24}\text{Se}$  monocrystal

# $\text{Pb}_{0.77}\text{Sn}_{0.23}\text{Se}$ monocrystal grown by self-selecting vapor growth

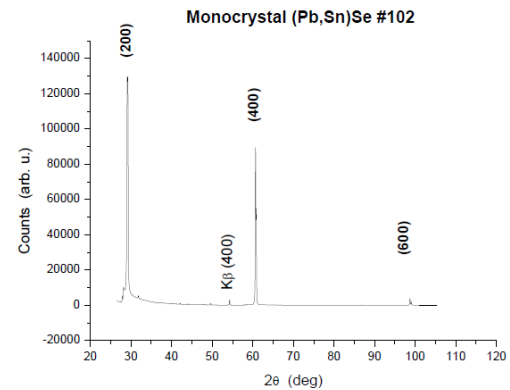
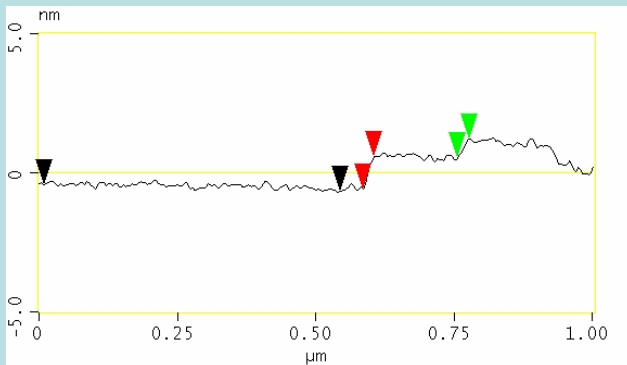
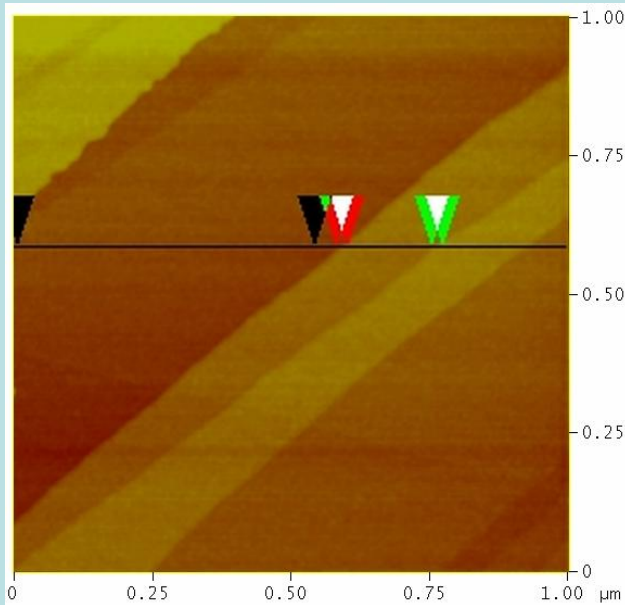


# Structural and chemical characterization

X-ray diffraction (XRD)

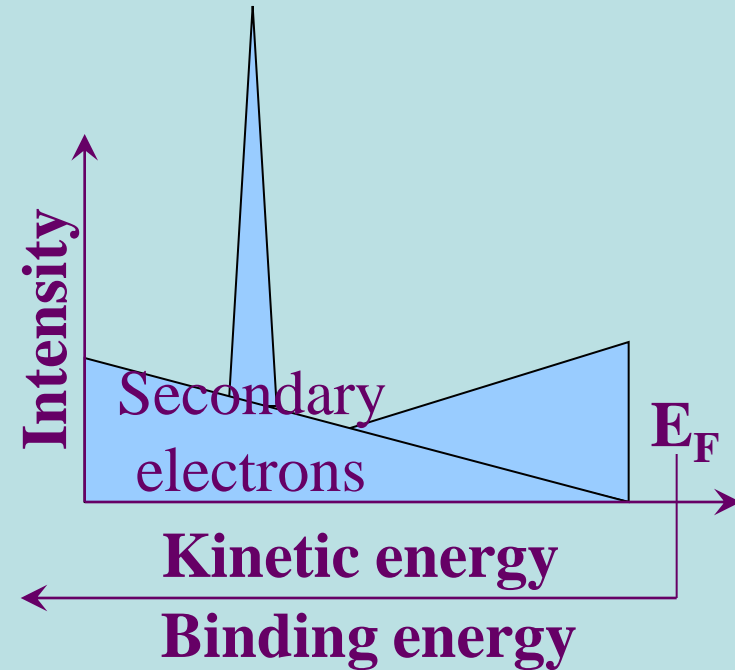
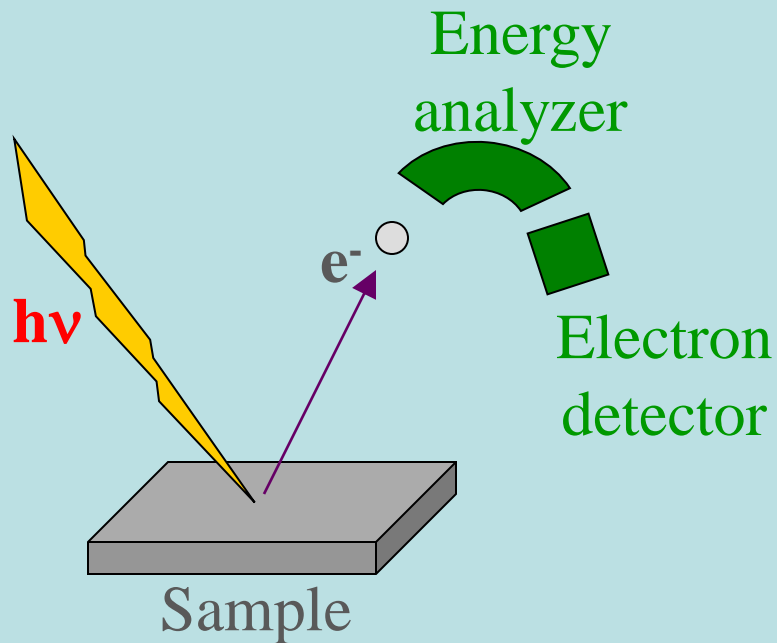
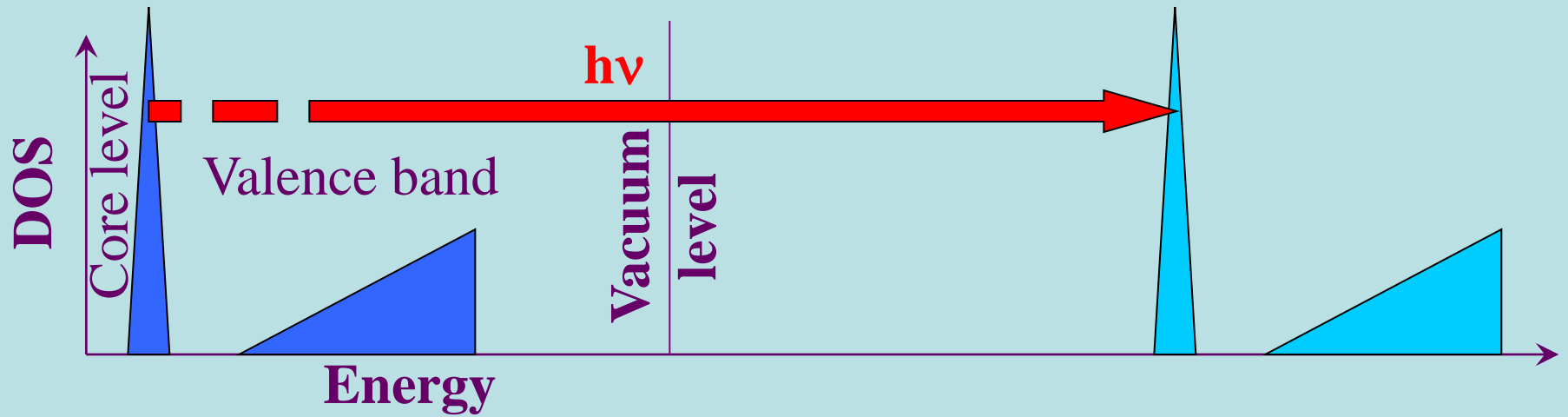
EDX chemical analysis

Surface morphology analysis  
by AFM microscopy

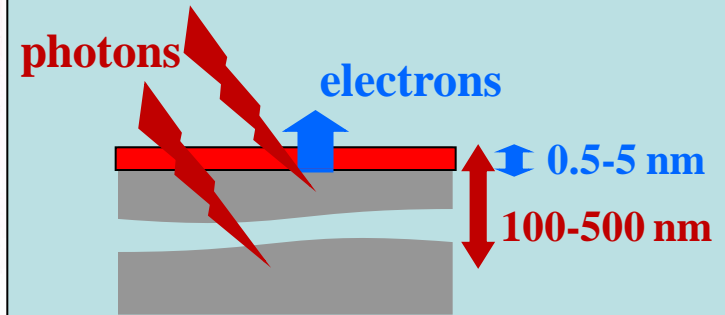
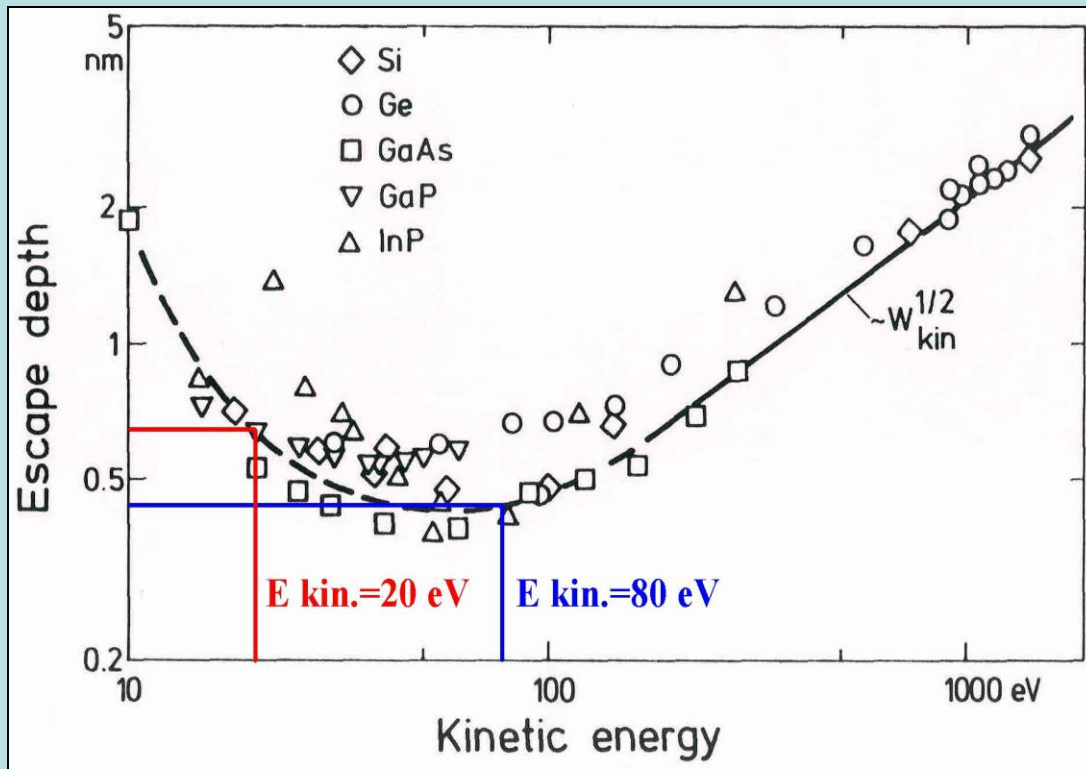




# Photoemission electron spectroscopy

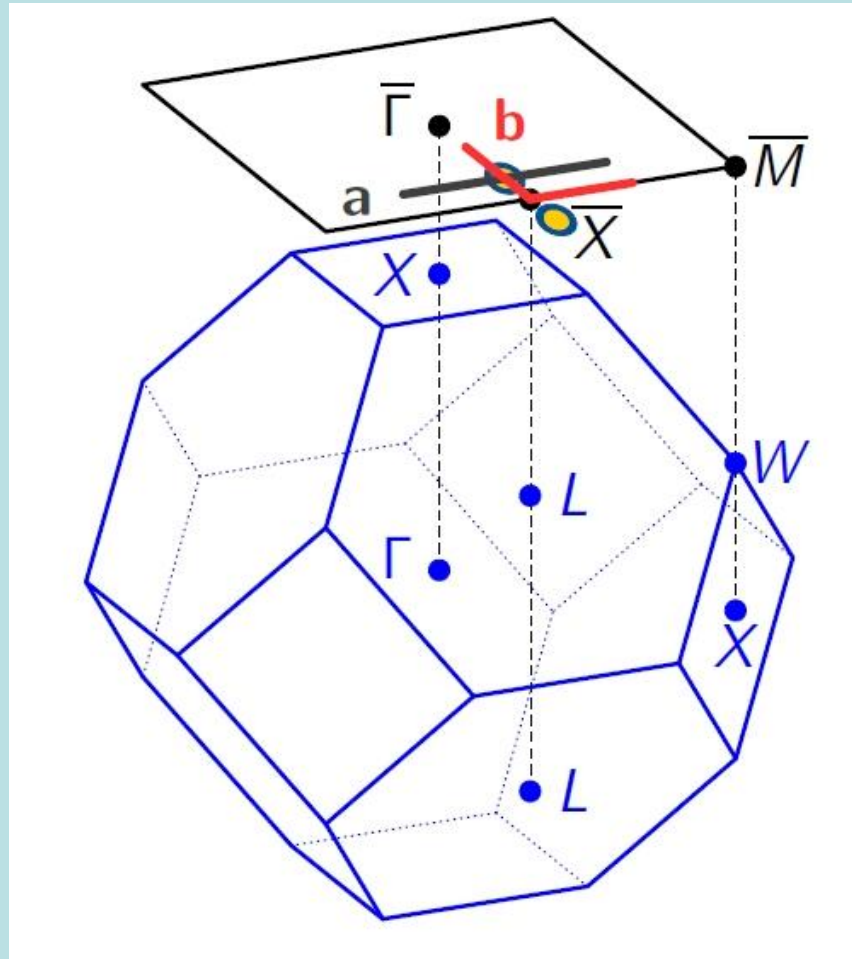


# Photoemission – crystal surface sensitive technique



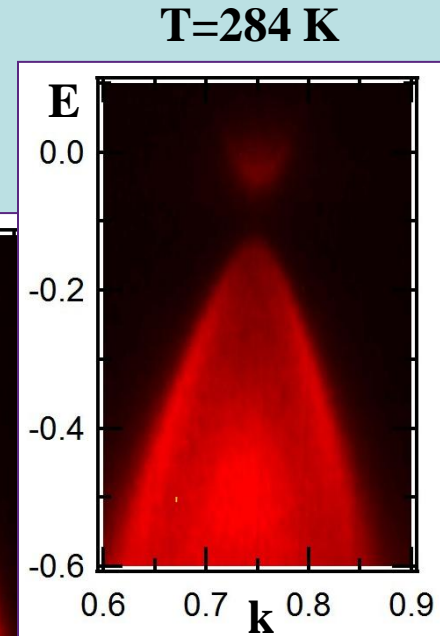
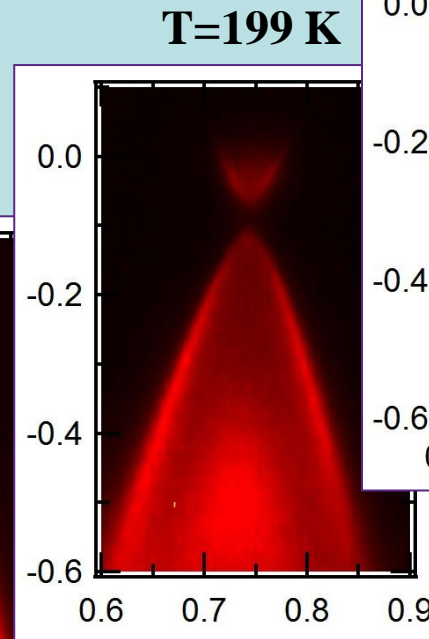
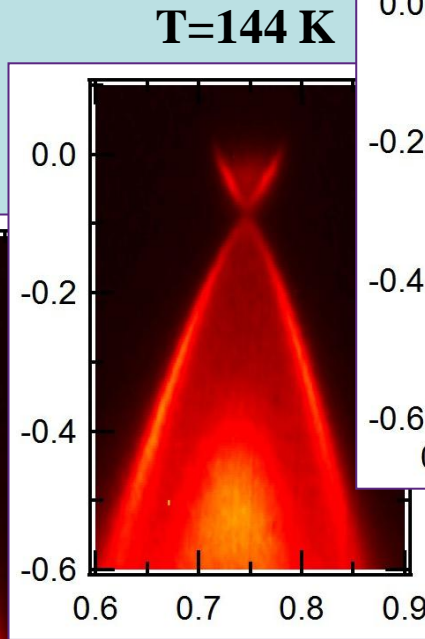
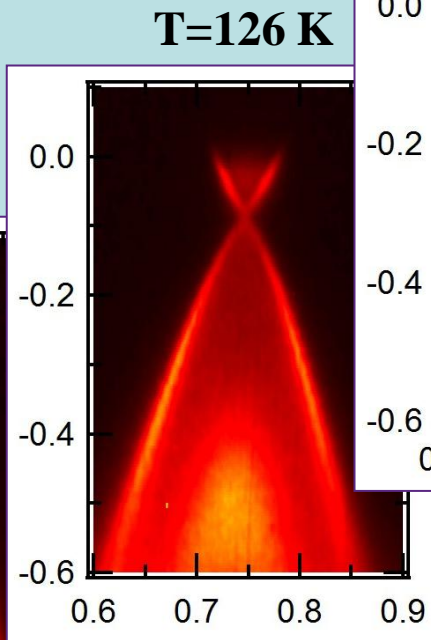
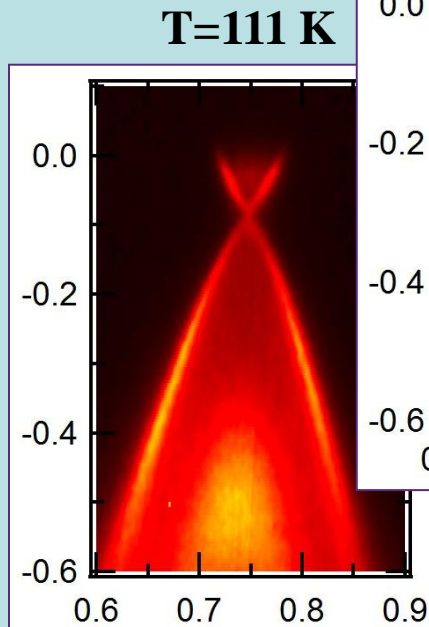
W. Mönch „Semiconductor surfaces and interfaces” 1993

# Brillouin zone for (001) surface



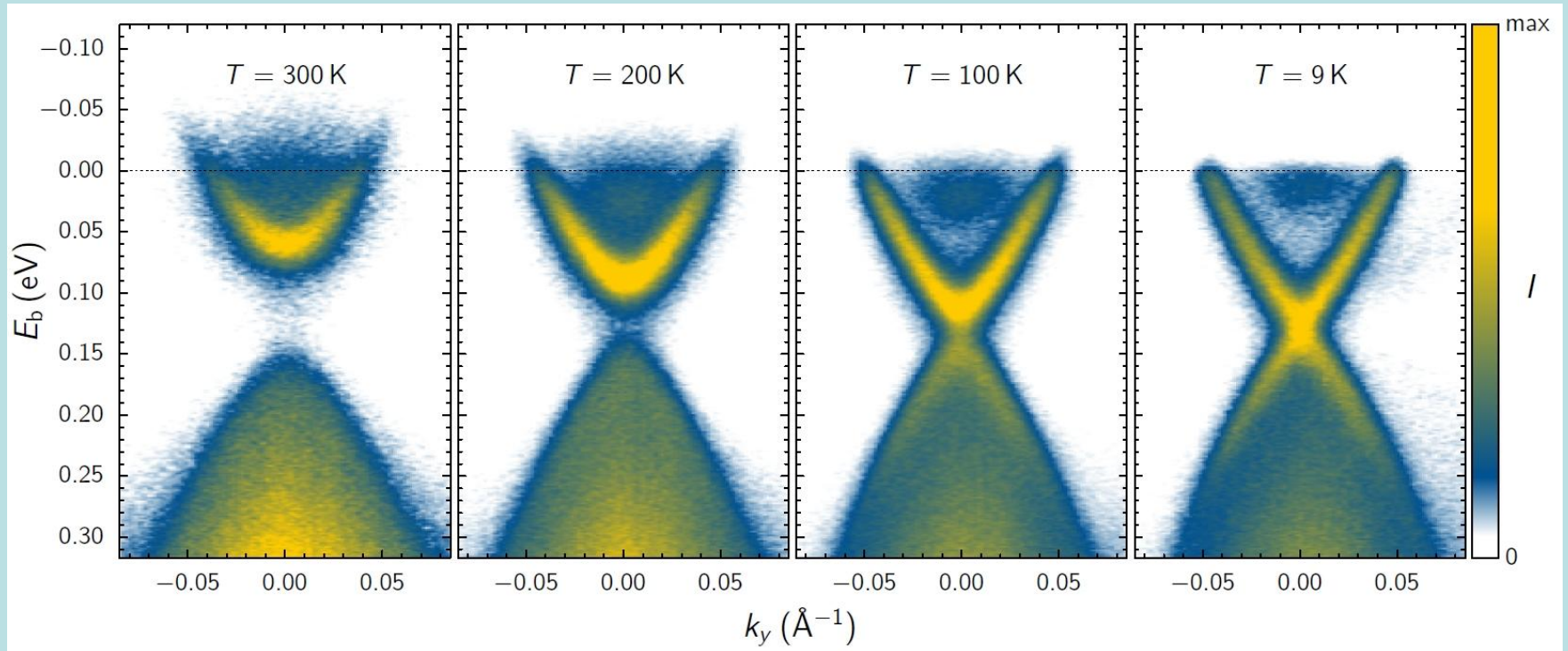
# Electron band structure ARPES studies of $\text{Pb}_{0.77}\text{Sn}_{0.23}\text{Se}$

$E_G$  vs.  $T$



# Electron band structure of $\text{Pb}_{0.77}\text{Sn}_{0.23}\text{Se}$

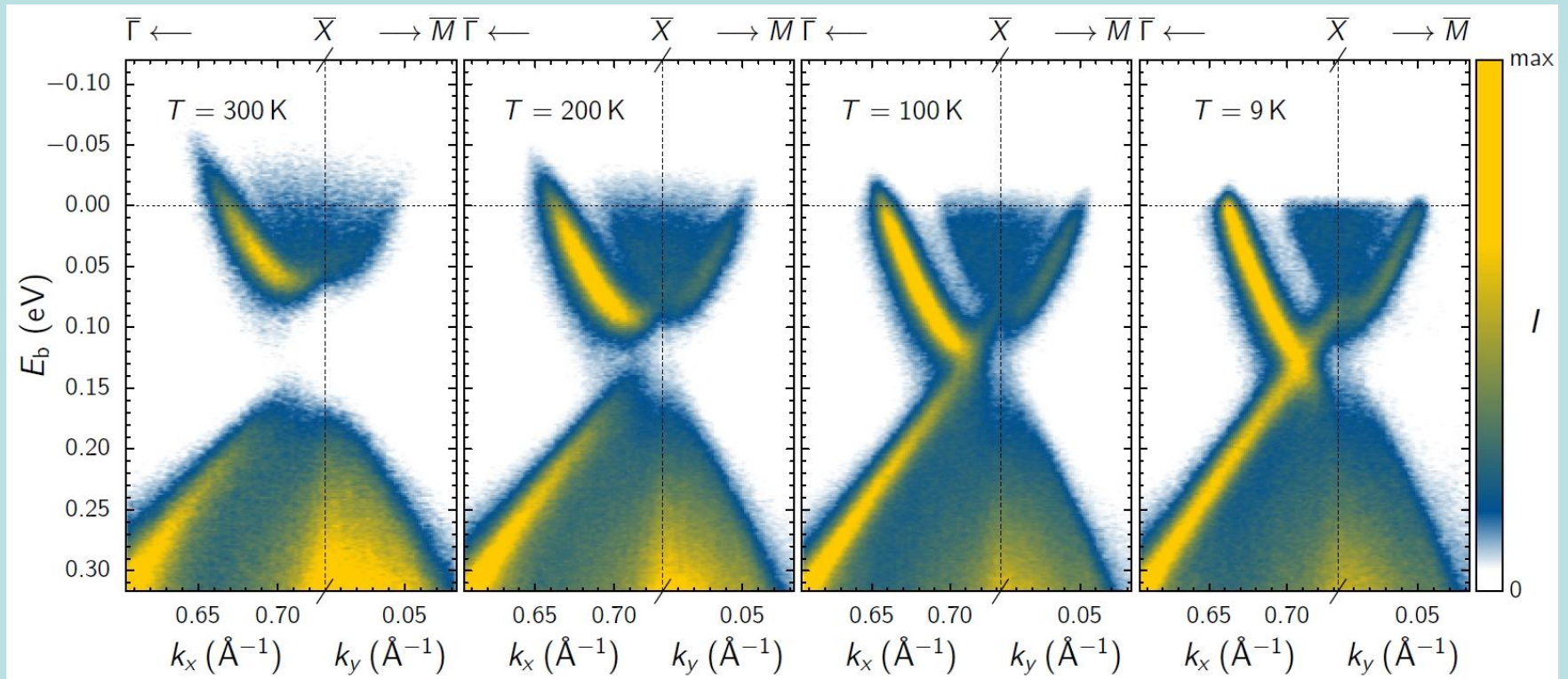
## ARPES experimental studies



- **Energy dispersion relation for temperature varying across band inversion point**

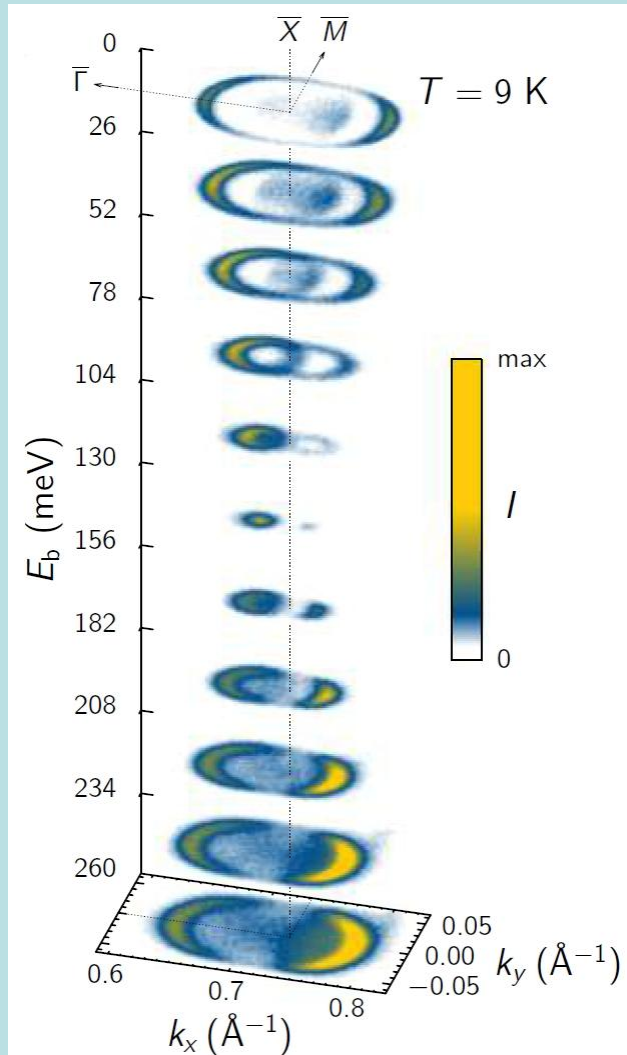


# Electron band structure of $\text{Pb}_{0.77}\text{Sn}_{0.23}\text{Se}$ ARPES experimental studies



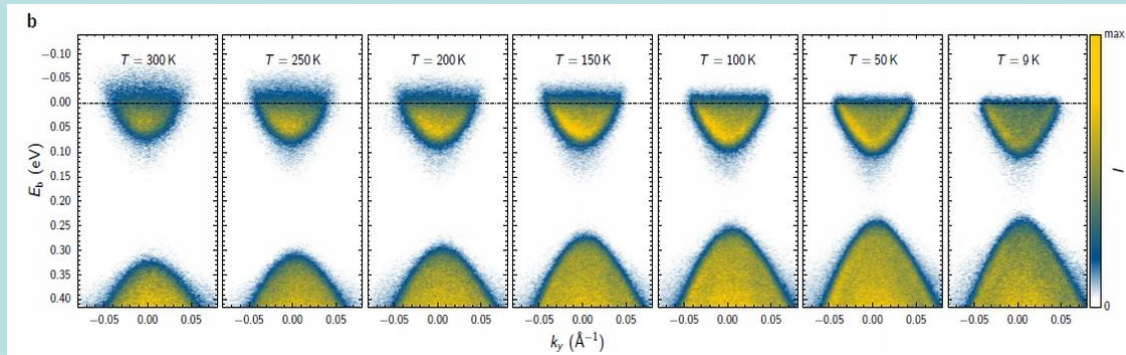
- Energy dispersion  $E(k)$  for X- $\bar{\Gamma}$  and X- $\bar{M}$  directions in surface Brillouin zone

# Electron band structure of $\text{Pb}_{0.77}\text{Sn}_{0.23}\text{Se}$ ARPES experimental studies

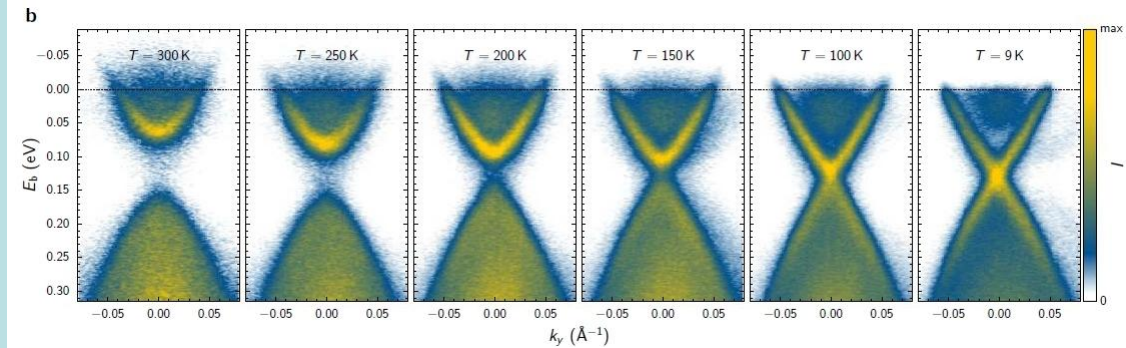


- Fermi surface cuts  $E(k_x, k_y)$  for varying binding energy  $E_b$

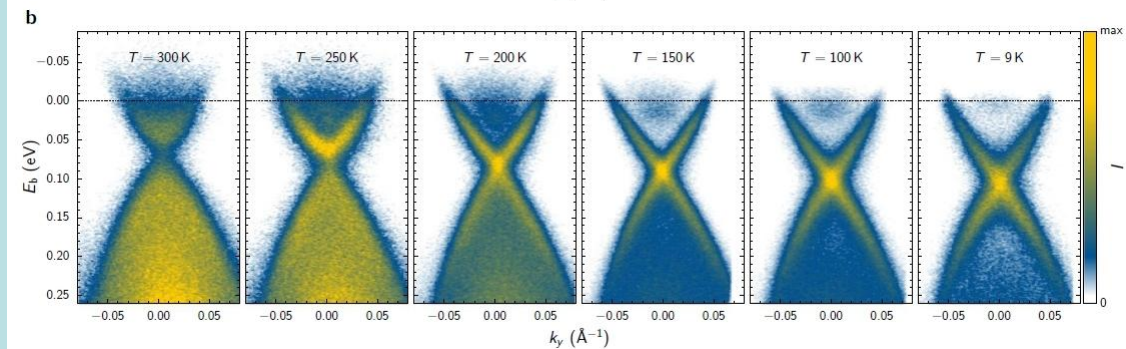
# Trivial insulator (PbSe) vs topological crystalline insulator ( $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$ )



**PbSe ( $x=0$ )**



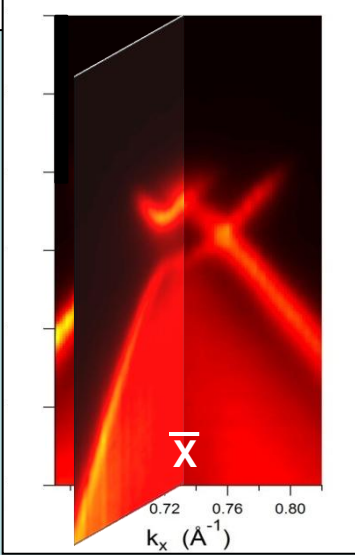
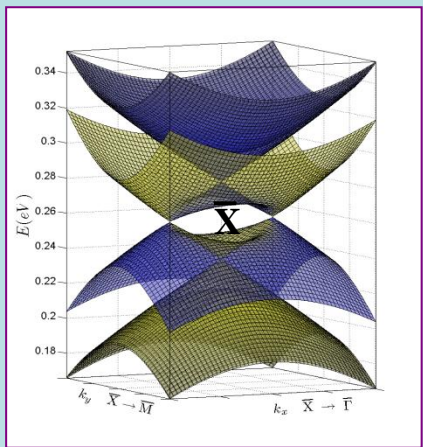
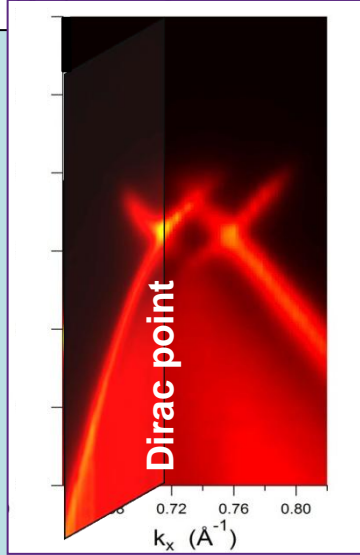
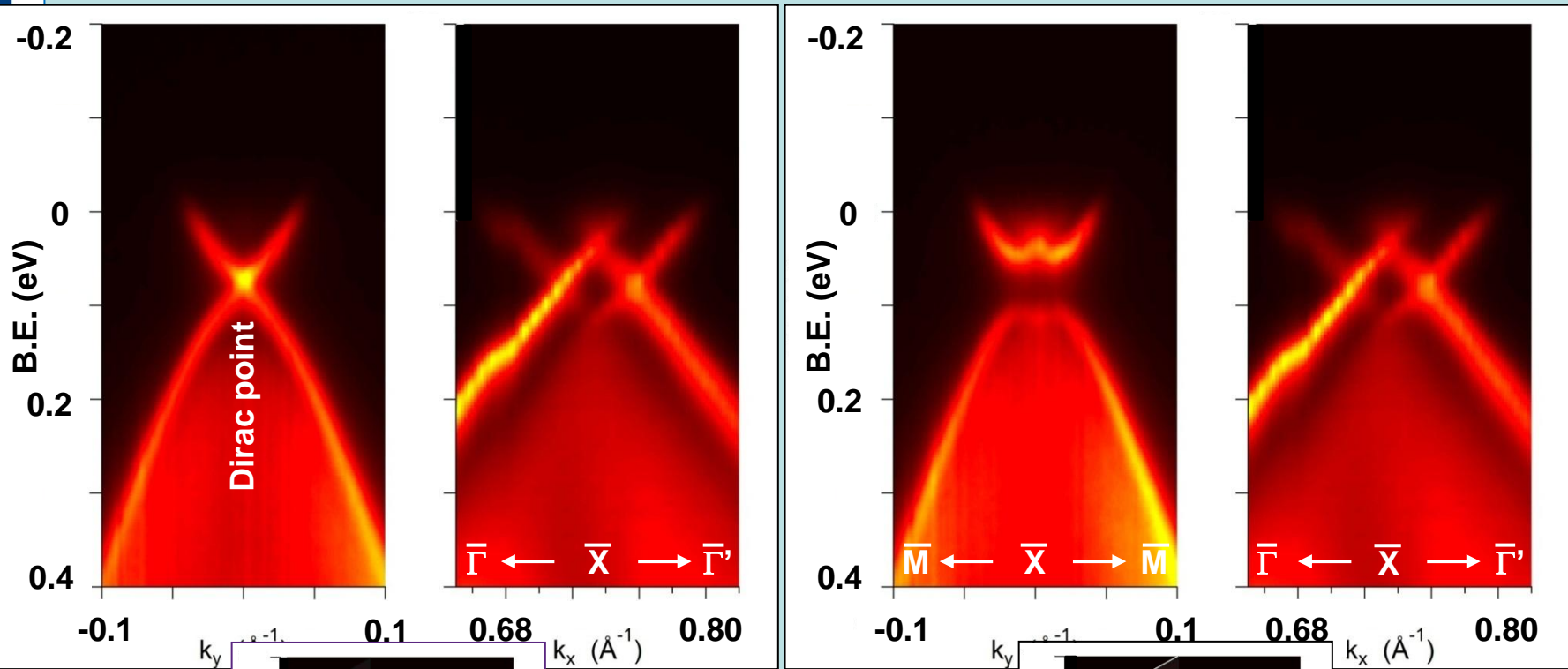
**$x=0.23$**



**$x=0.30$**

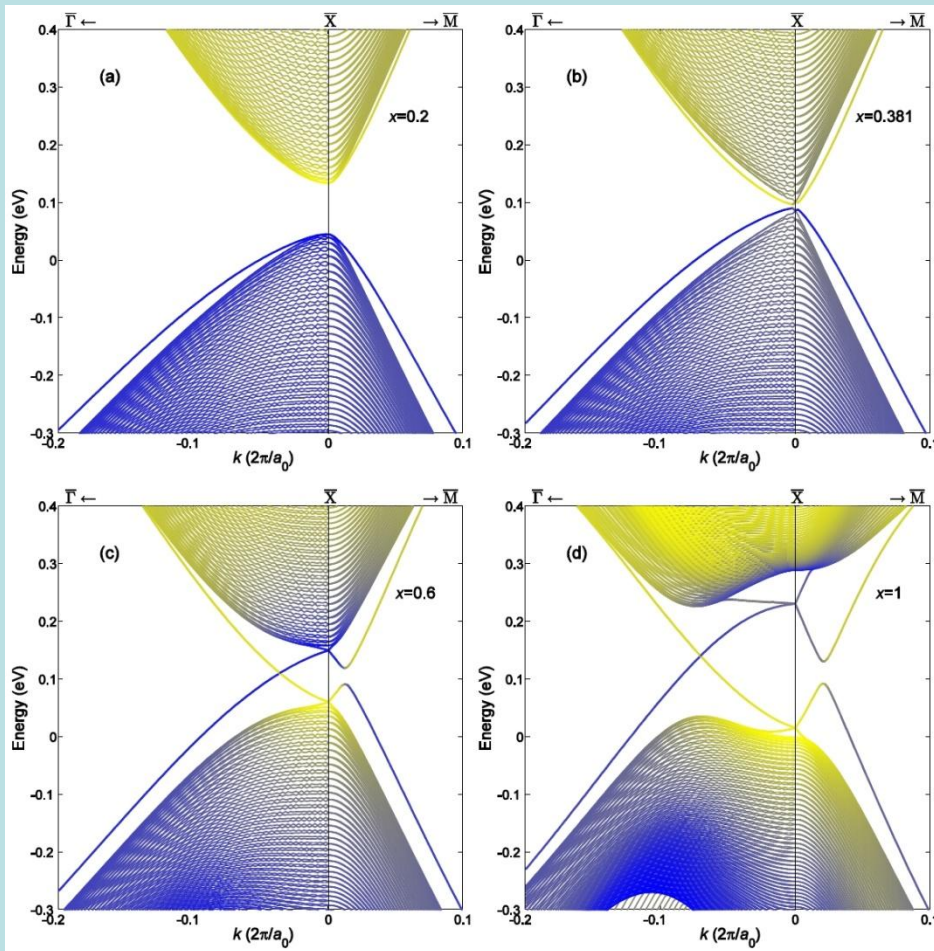
**B.M. Wojek et al. 2012**

# Pb<sub>0.67</sub>Sn<sub>0.33</sub>Se, T=87 K, hν=18.5 eV



Theory-  
R. Buczko, P. Kacman, S. Safaei

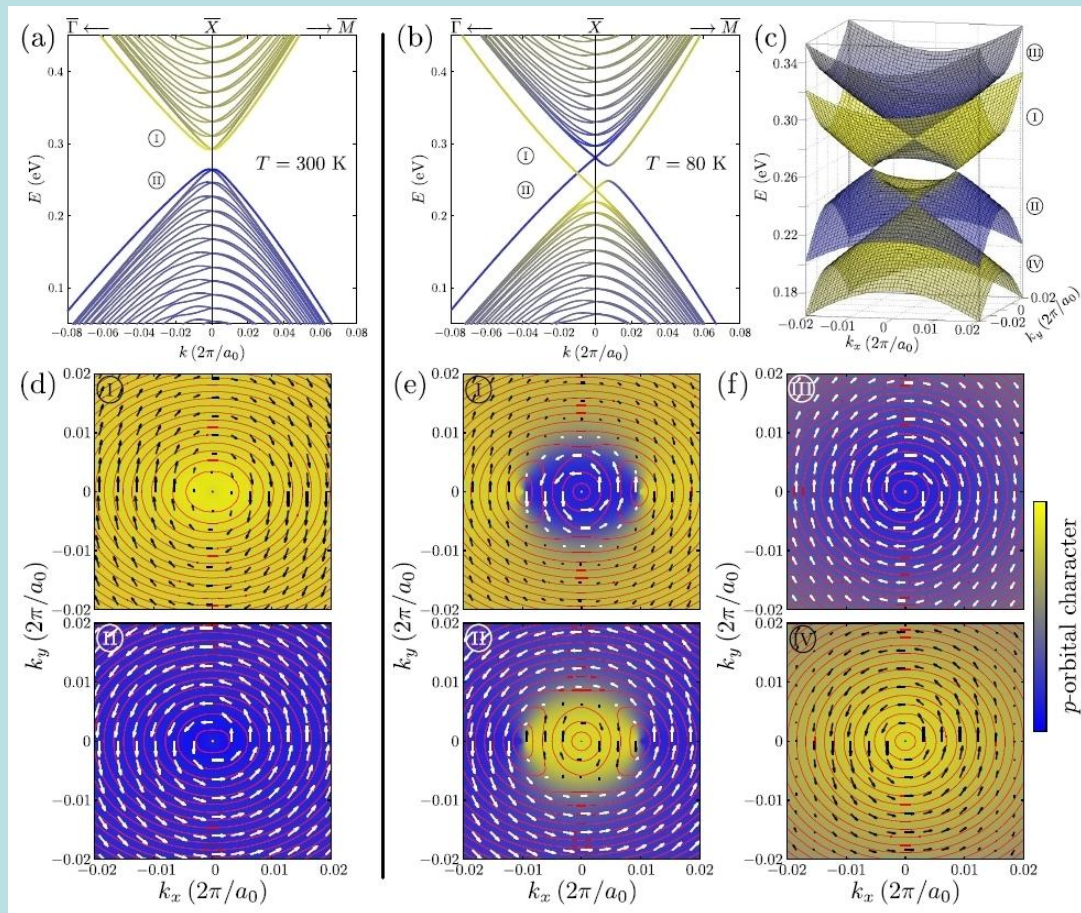
# Band structure of $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$ : tight binding calculations



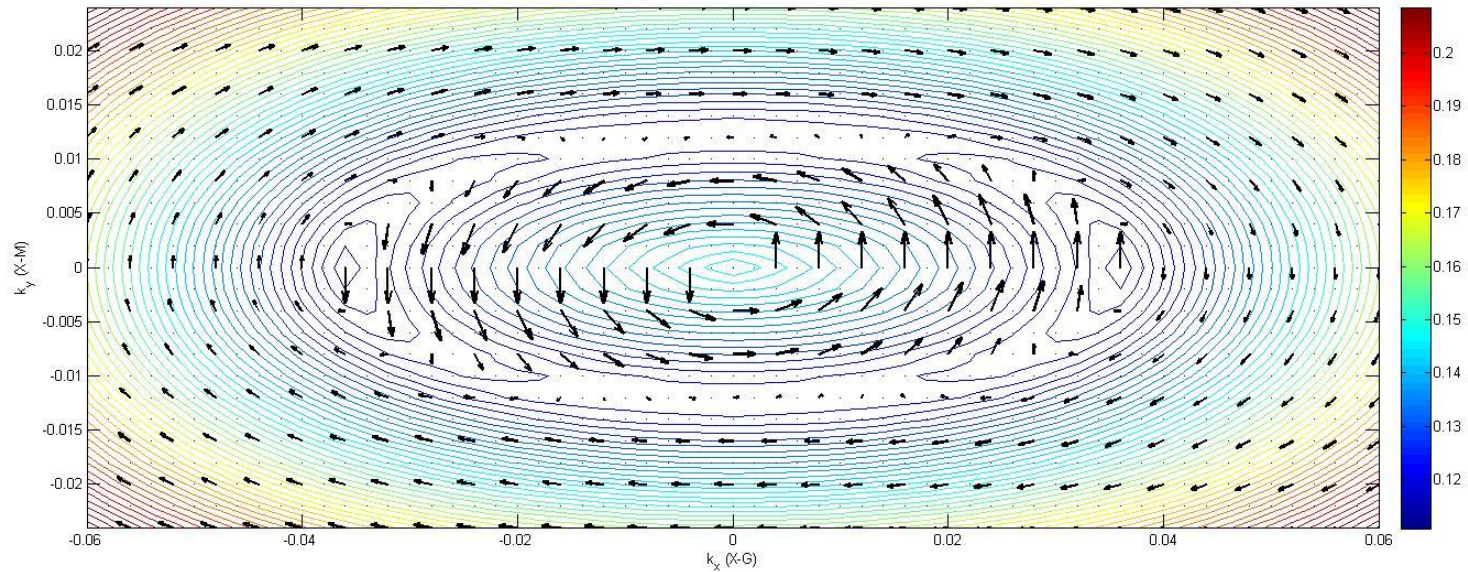
- $\text{PbSnTe}$  in band inversion region:
- A) band insulator
- B) zero bulk band gap
- C) inverted gap - TCI
- D) SnTe – TCI

Yellow – p-type cation orbitals  
Blue – p-type anion orbitals

# Spin polarization of TCI states: tight binding model – $\text{Pb}_{0.76}\text{Sn}_{0.24}\text{Se}$

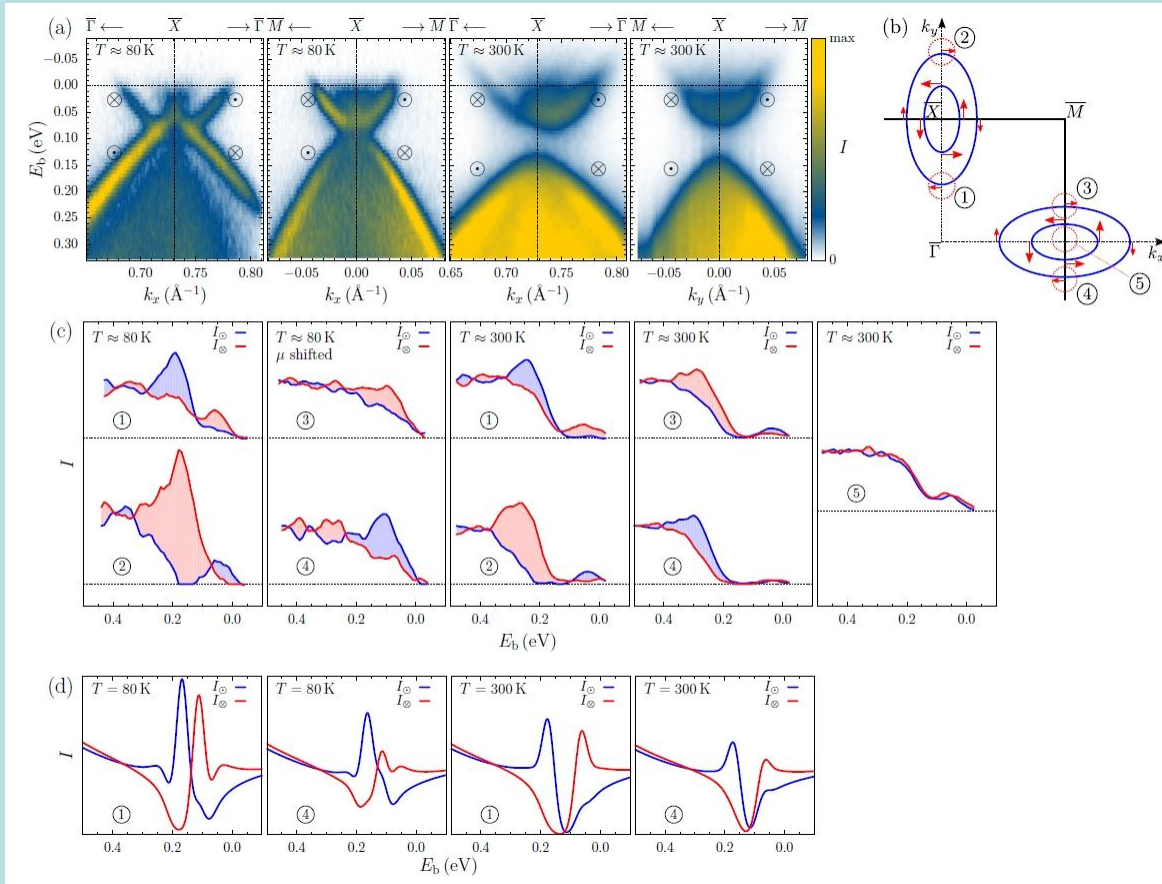


# Spin polarization of TCI states in SnTe



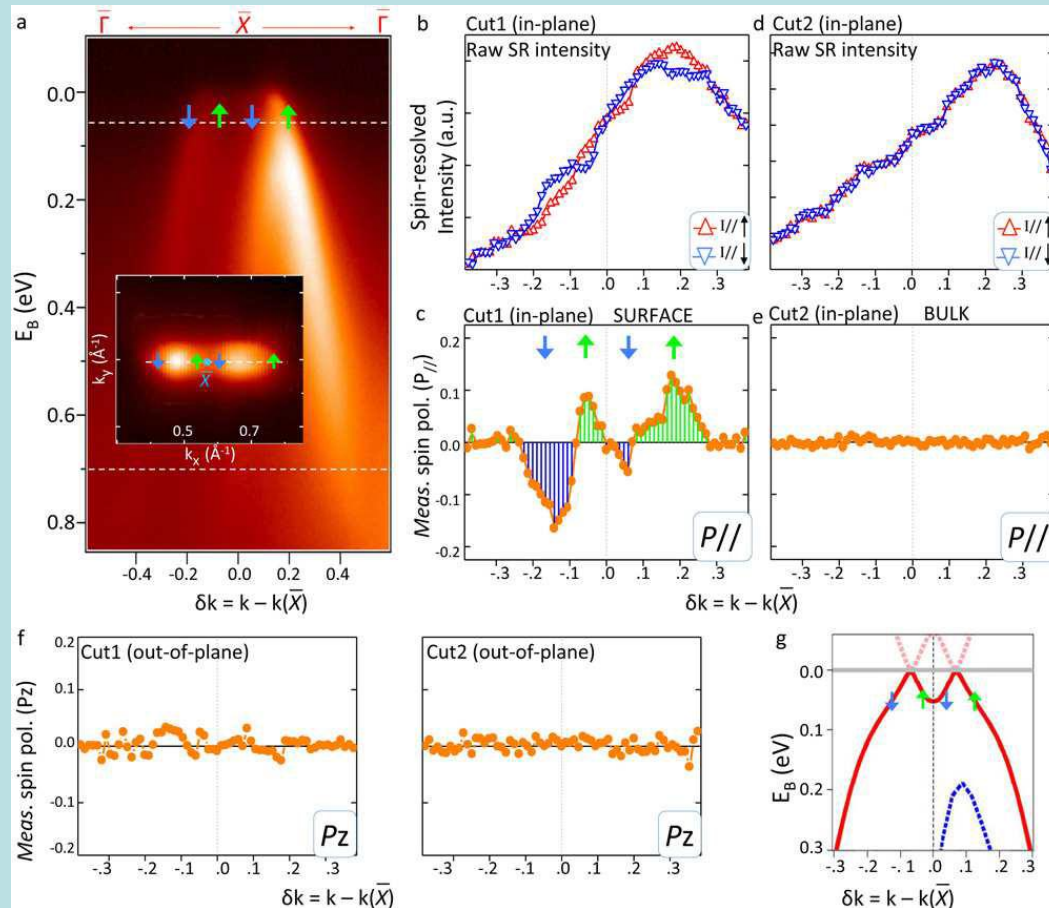
S. Safaei, P. Kacman, R. Buczko, Phys. Rev. B 88, 045305 (2013)  
tight binding calculations

# Spin polarization of TCI states: SRPES experiment – $\text{Pb}_{0.76}\text{Sn}_{0.24}\text{Se}$



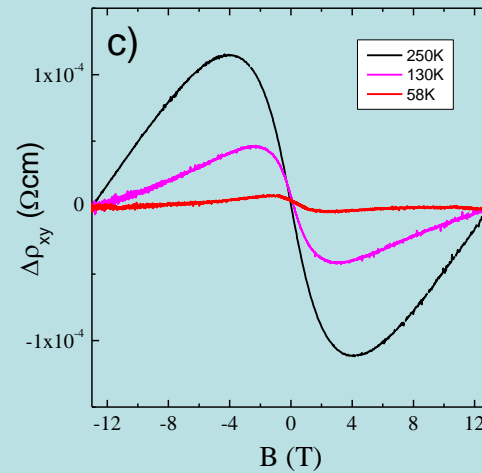
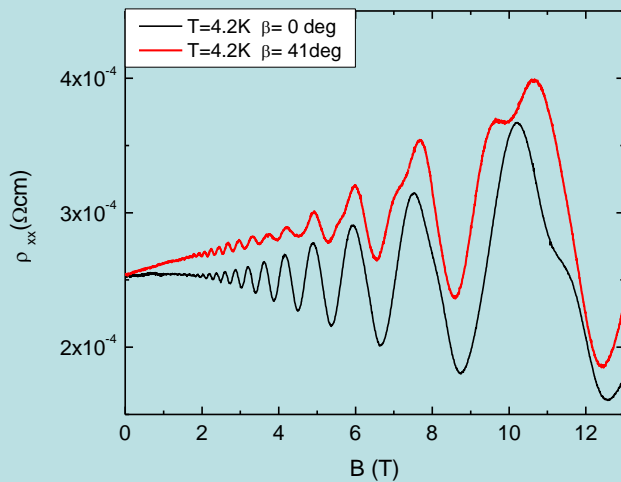
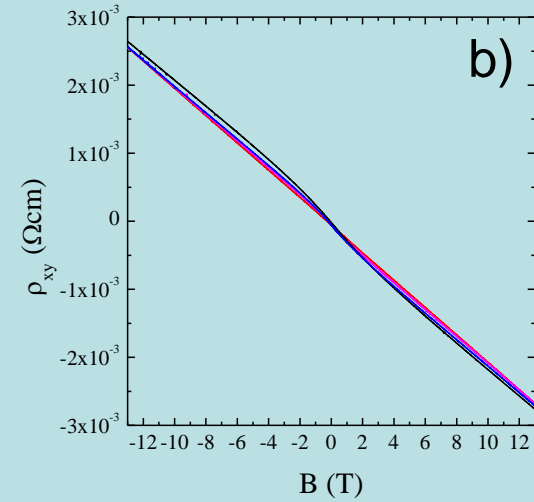
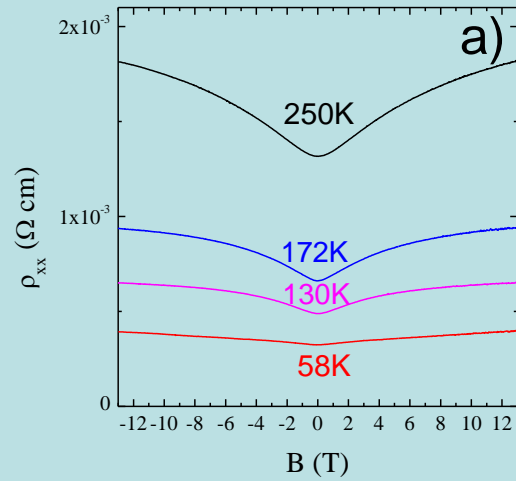


# Spin polarization of TCI states: SRPES experiment – $\text{Pb}_{0.6}\text{Sn}_{0.4}\text{Te}$

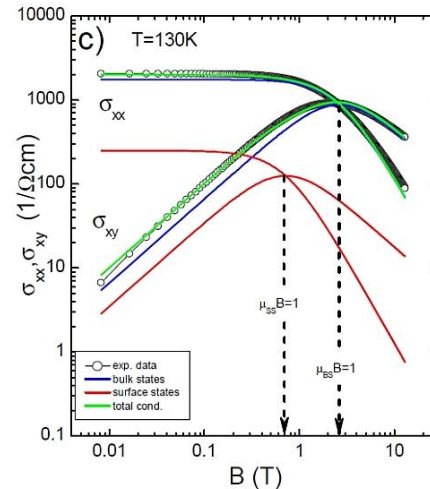
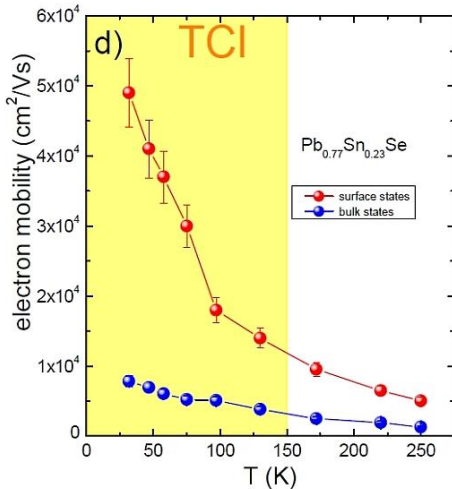
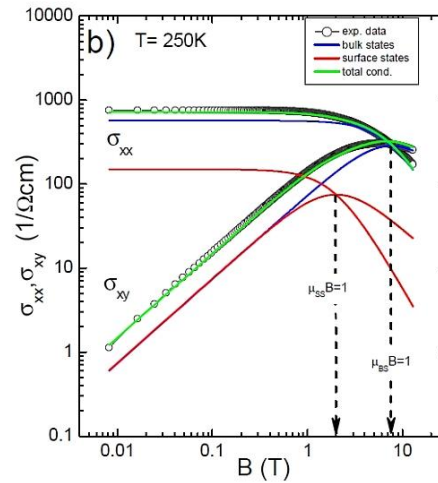
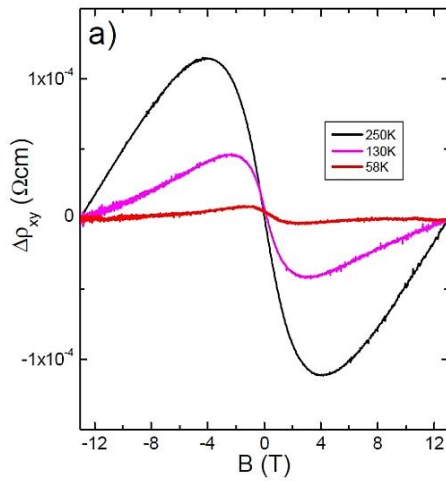


- S-Y Xu, ... M.Z. Hasan, Nat. Commun. **3**, 1192 (2012).

# $\text{Pb}_{0.77}\text{Sn}_{0.23}\text{Se}$ : magneto-transport



# Pb<sub>0.77</sub>Sn<sub>0.23</sub>Se: magneto-transport



Drude model for magneto-conductivity

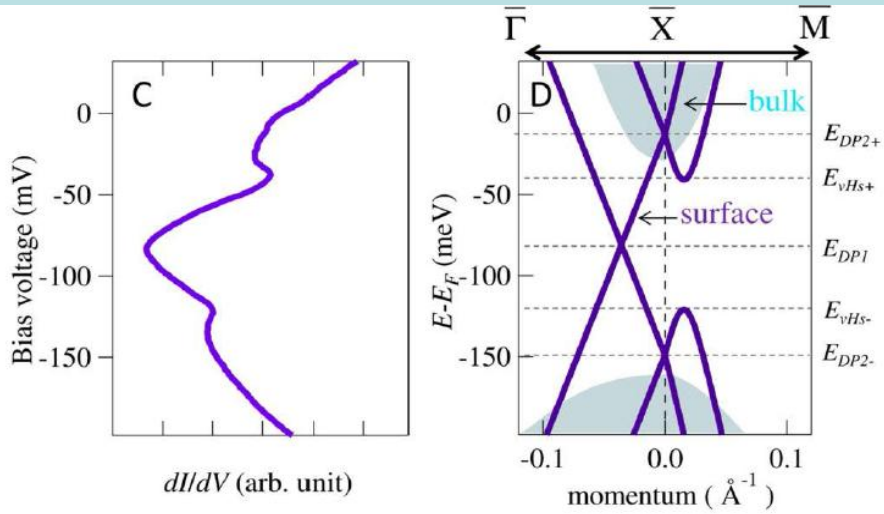
Two parallel conduction channels

Fitting of electron transport parameters

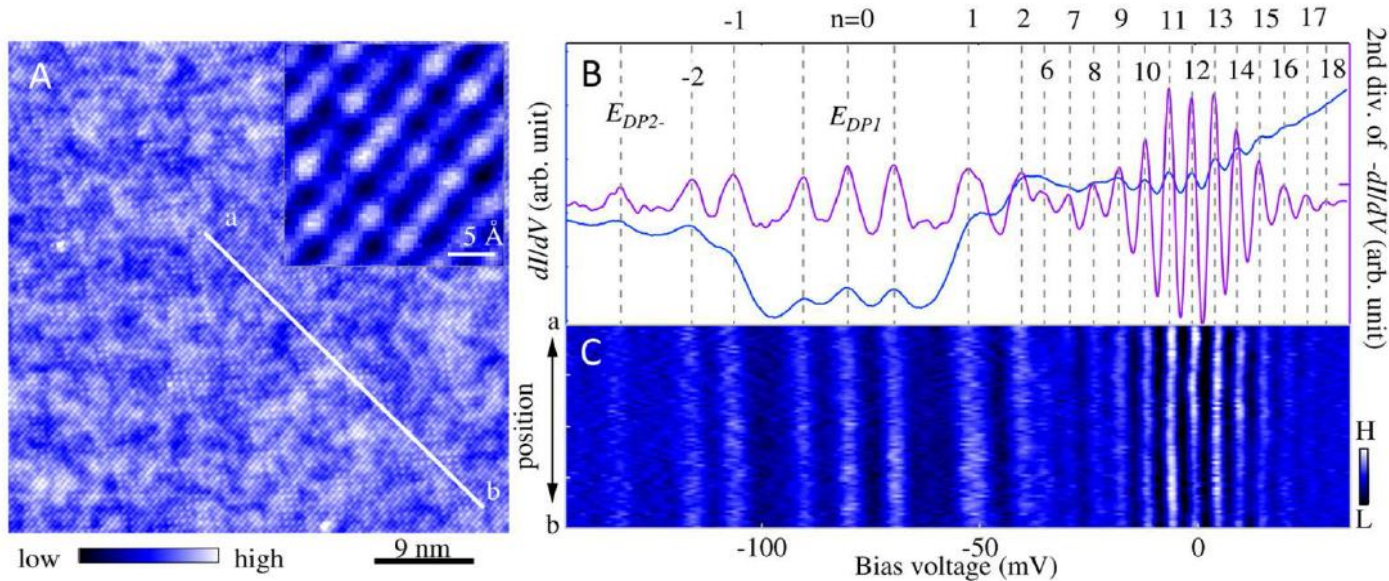
$\sigma_{BS}$ ,  $\mu_{BS}$ ,  $\sigma_{SS}$ ,  $\mu_{SS}$   
for bulk crystal and surface channels

K. Dybko et al. 2012

# STM $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$



Y. Okada et al., Science 2013



# TCl - materials

nature  
materials

LETTERS

PUBLISHED ONLINE: 30 SEPTEMBER 2012 | DOI: 10.1038/NMAT3449

## Topological crystalline insulator states in $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$

P. Dziawa<sup>1</sup>, B. J. Kowalski<sup>1</sup>, K. Dybko<sup>1</sup>, R. Buczko<sup>1</sup>, A. Szczerbakow<sup>1</sup>, M. Szot<sup>1</sup>, E. Łusakowska<sup>1</sup>,  
T. Balasubramanian<sup>2</sup>, B. M. Wojek<sup>3</sup>, M. H. Berntsen<sup>3</sup>, O. Tjernberg<sup>3\*</sup> and T. Story<sup>1\*</sup>

nature  
physics

LETTERS

PUBLISHED ONLINE: 30 SEPTEMBER 2012 | DOI: 10.1038/NPHYS2442

## Experimental realization of a topological crystalline insulator in SnTe

Y. Tanaka<sup>1</sup>, Zhi Ren<sup>2</sup>, T. Sato<sup>1\*</sup>, K. Nakayama<sup>1</sup>, S. Souma<sup>3</sup>, T. Takahashi<sup>1,3</sup>, Kouji Segawa<sup>2</sup>  
and Yoichi Ando<sup>2\*</sup>

nature  
COMMUNICATIONS

ARTICLE

Received 6 Aug 2012 | Accepted 8 Oct 2012 | Published 13 Nov 2012

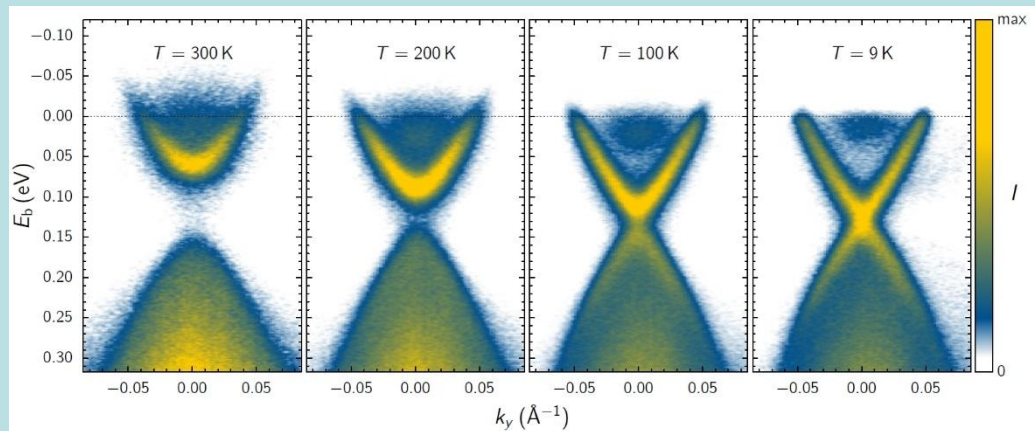
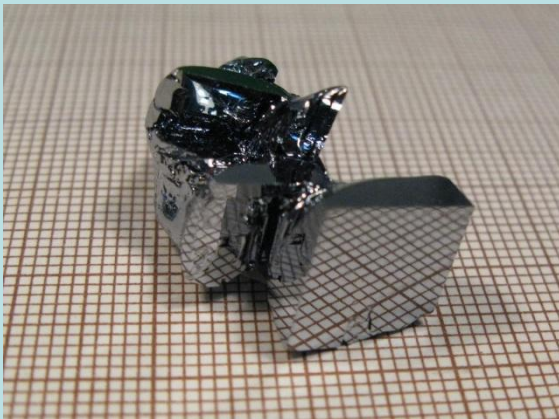
DOI: 10.1038/ncomms2191

## Observation of a topological crystalline insulator phase and topological phase transition in $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$

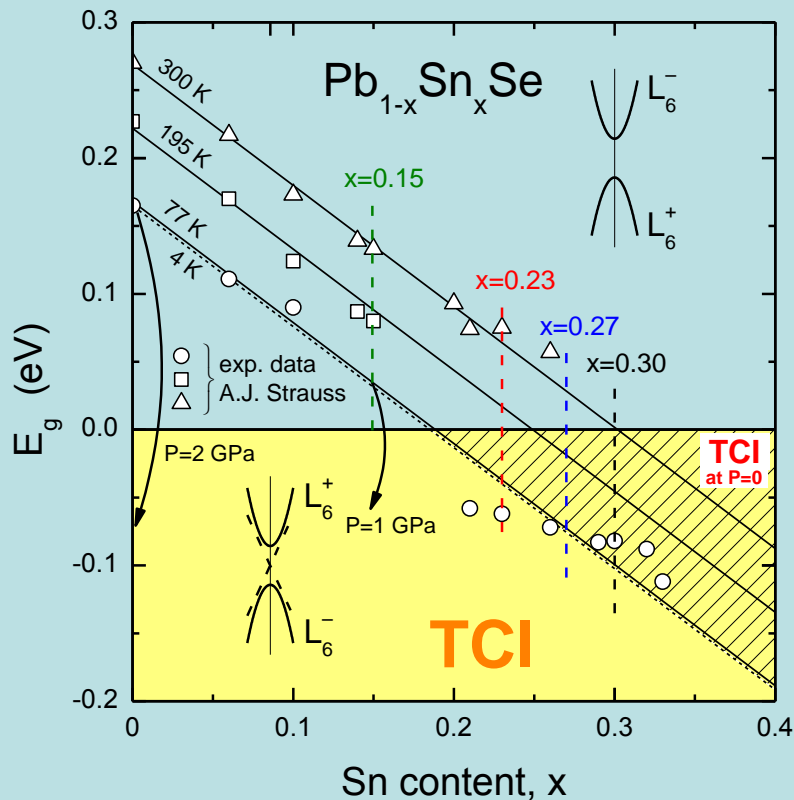
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# Summary

- Topological crystalline insulators (TCIs) are a new class of quantum materials in which the topological protection of metallic surface states is warranted not by time-reversal symmetry as in TI but by specific crystalline symmetries.
- $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$  – IV-VI narrow-gap semiconductor is a TCI, in which a temperature-driven topological phase transition is observed from a trivial insulator to a TCI due to band inversion.
- We discussed growth of monocrystals, electronic band structure investigations by angle- and spin-resolved photoemission spectroscopy (ARPES, SRPES), magneto-transport studies, and electronic band structure calculations of  $\text{Pb}_{1-x}\text{Sn}_x\text{Se}$  ( $x \leq 0.4$ ).



# Future outlook



Topological phase diagram study:  
 $Pb_{1-x}Sn_xSe$  i  $Pb_{1-x}Sn_xTe - (T, P)$

Controlling electrical and optical properties

Other surface sensitive experimental methods - STM

Co-existence of ferromagnetism and TCI state in  $Sn_{1-x}Mn_xTe$

TCI/ferromagnet and TCI/superconductor heterostructures

Influence of lattice distortion on TCI